

# Understanding and preventing seismicity induced by fluid injection in Enhanced Geothermal Systems

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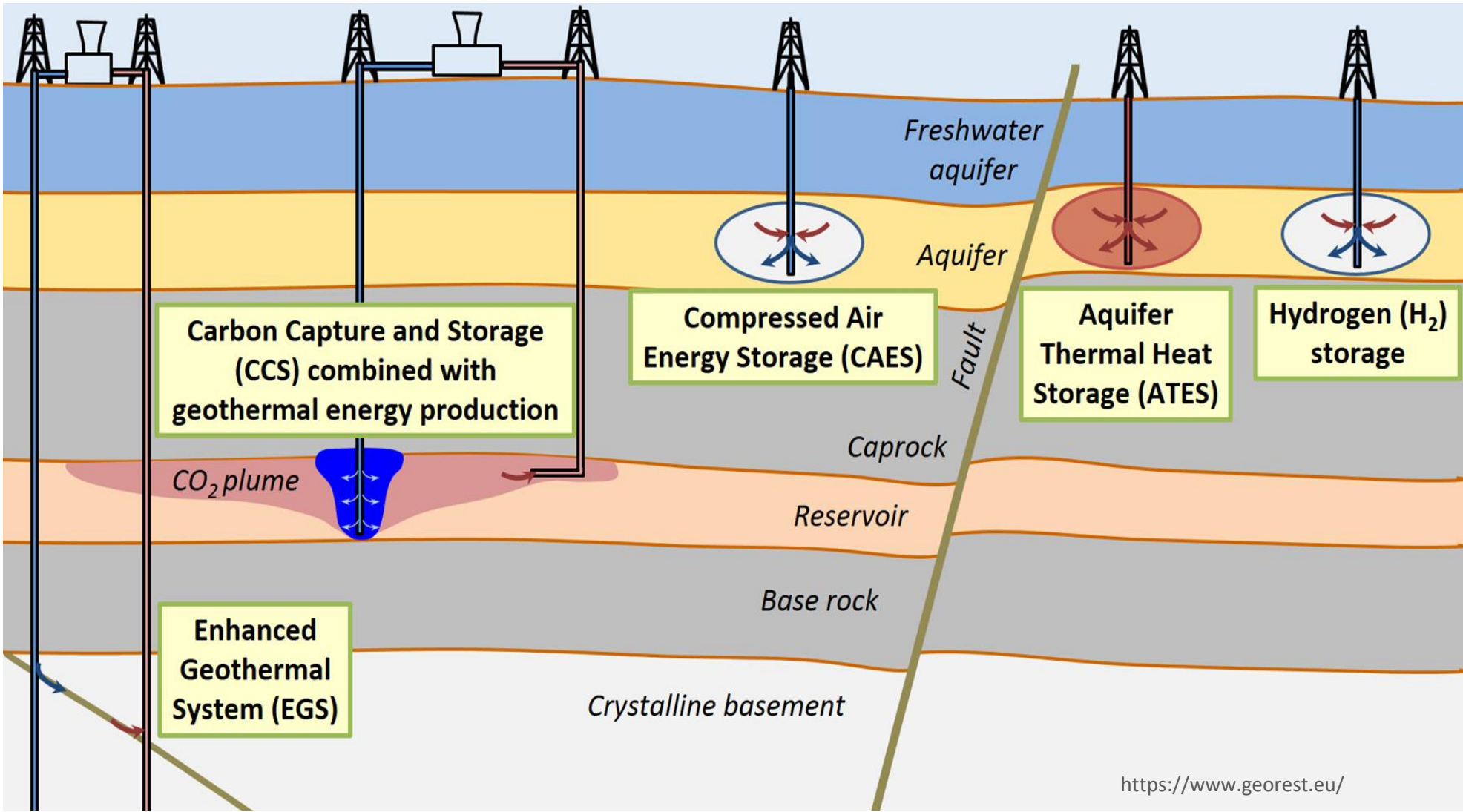


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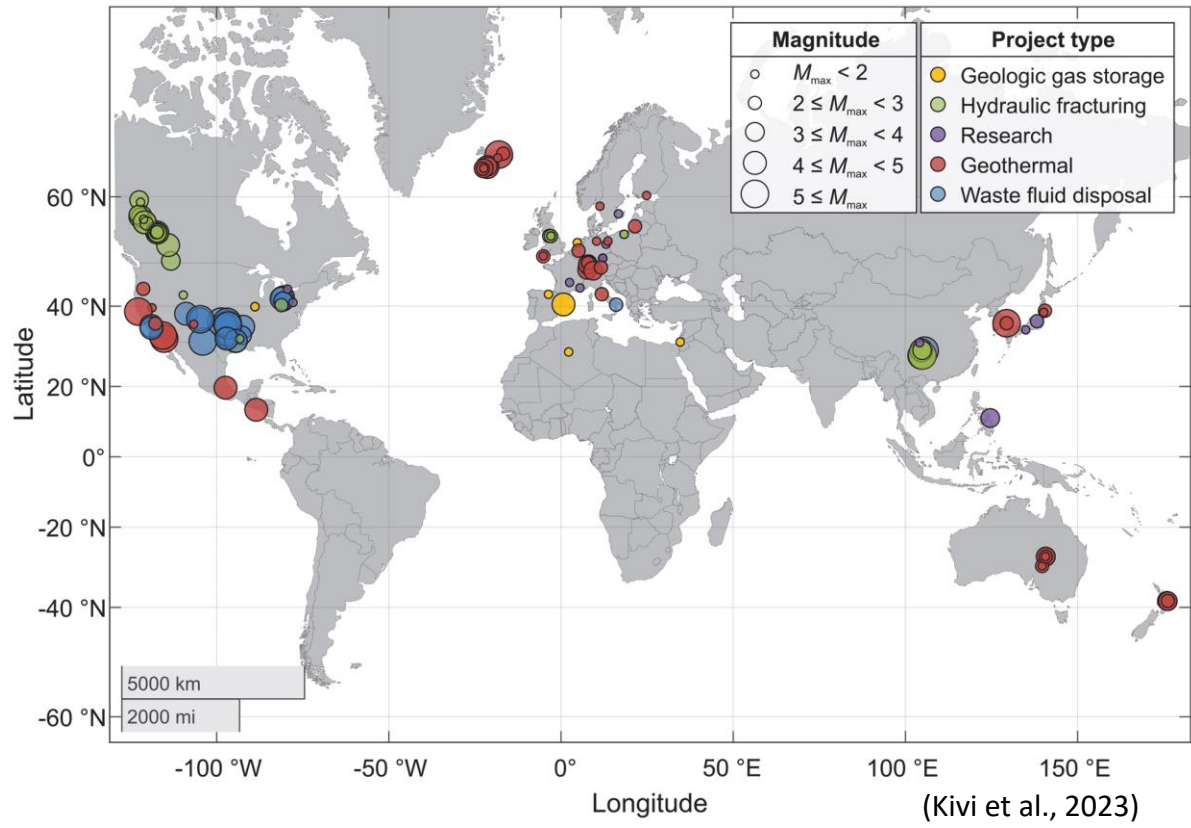
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# Geo-energy applications are major solutions for the energetic transition, but fluid injection may induce seismicity in the different applications

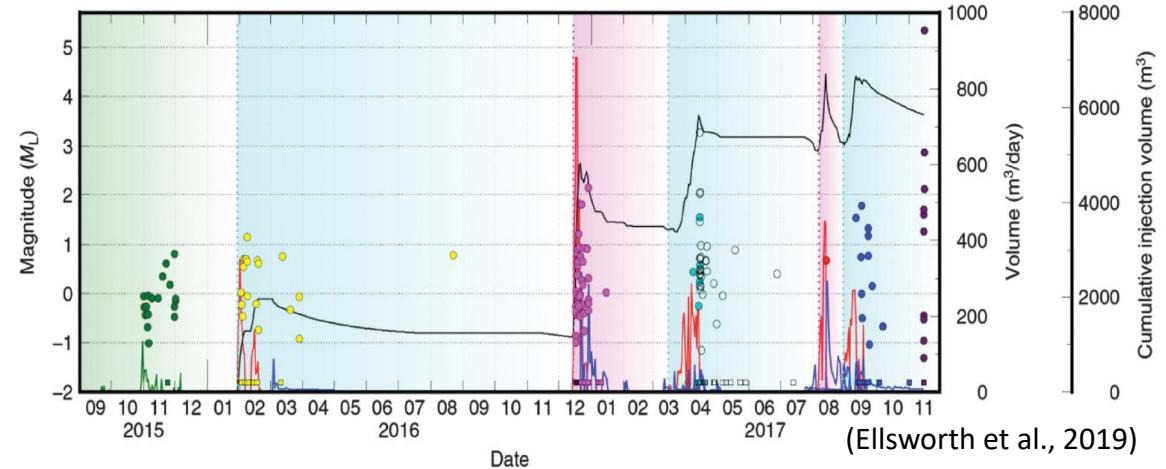


<https://www.georest.eu/>

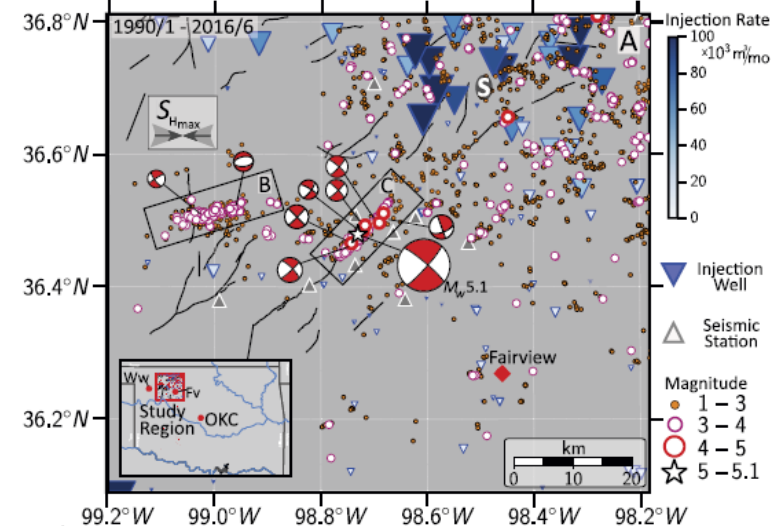
# Induced seismicity is an inherent hurdle to geo-energy applications and European energetic transition decisions increase the risks of induced seismicity



## Pohang EGS, Korean Republic – 2 months of delay



## Oklahoma WWD, USA



# Enhanced Geothermal Systems (EGS) aim to produce electricity using the thermal energy of the subsurface

Fluid circulation is limited due to the low permeability of the deep crystalline rock

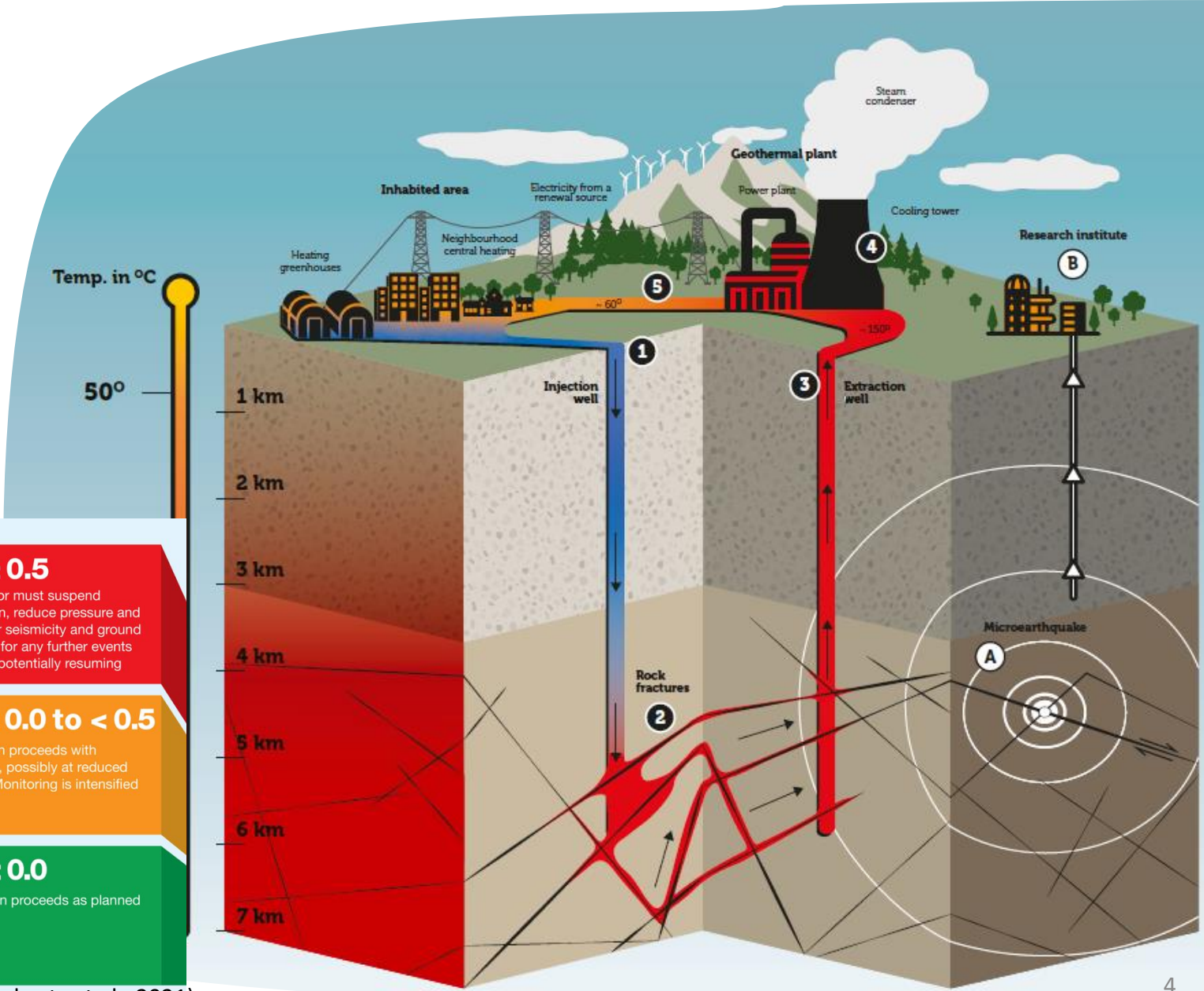
↳ Hydraulic stimulation enhances the permeability of the faults and initiates the propagation of a new fracture network

Felt earthquakes question the viability of these projects

Traffic light systems should prevent induced seismicity

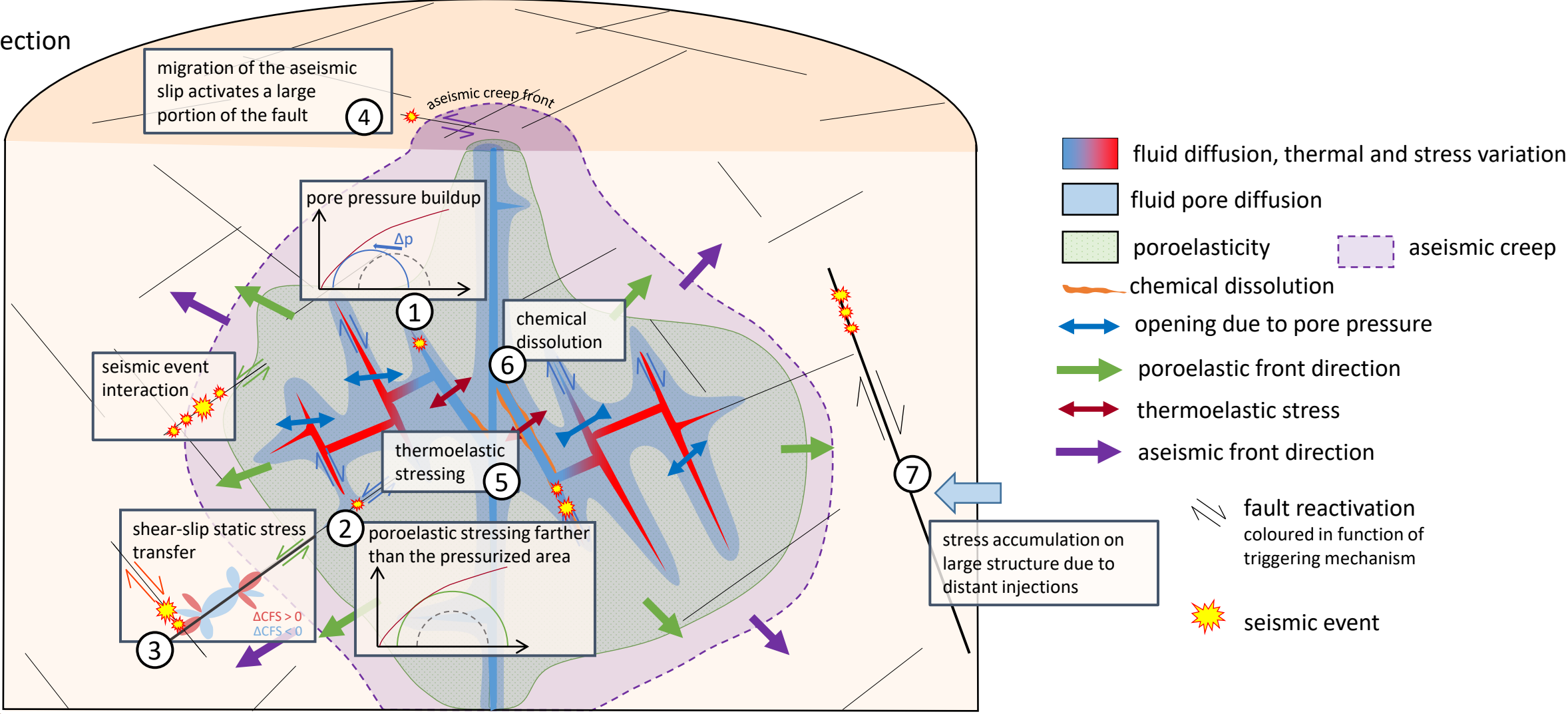
	<p><b>M ≥ 0.5</b> Operator must suspend injection, reduce pressure and monitor seismicity and ground motion for any further events before potentially resuming</p>
	<p><b>M ≥ 0.0 to &lt; 0.5</b> Injection proceeds with caution, possibly at reduced rates. Monitoring is intensified</p>
	<p><b>M &lt; 0.0</b> Injection proceeds as planned</p>

(Roberts et al., 2021)



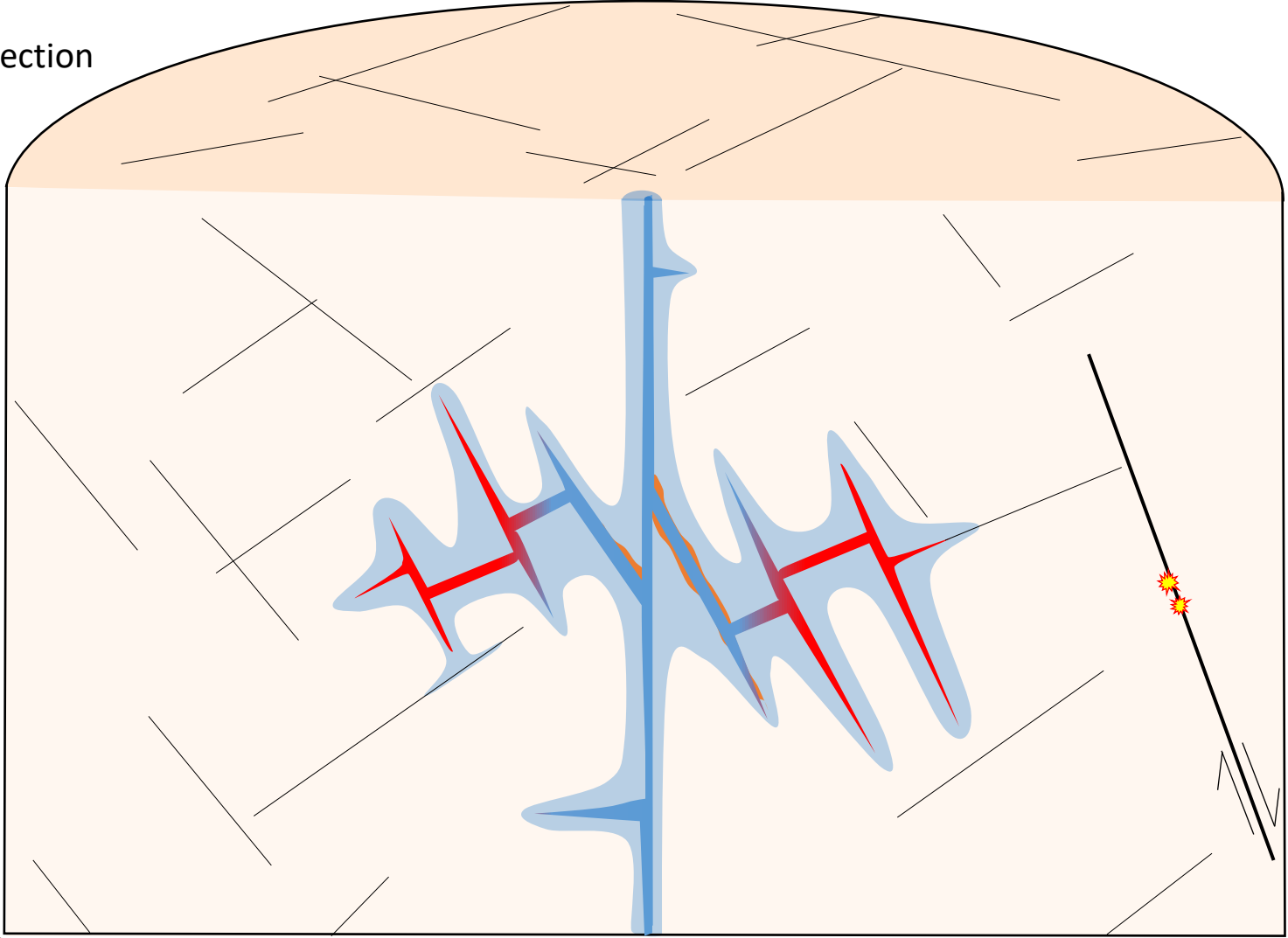
# Fluid injection redistributes pressure and stress along the fractured reservoir












during injection



# Fluid injection redistributes pressure and stress along the fractured reservoir

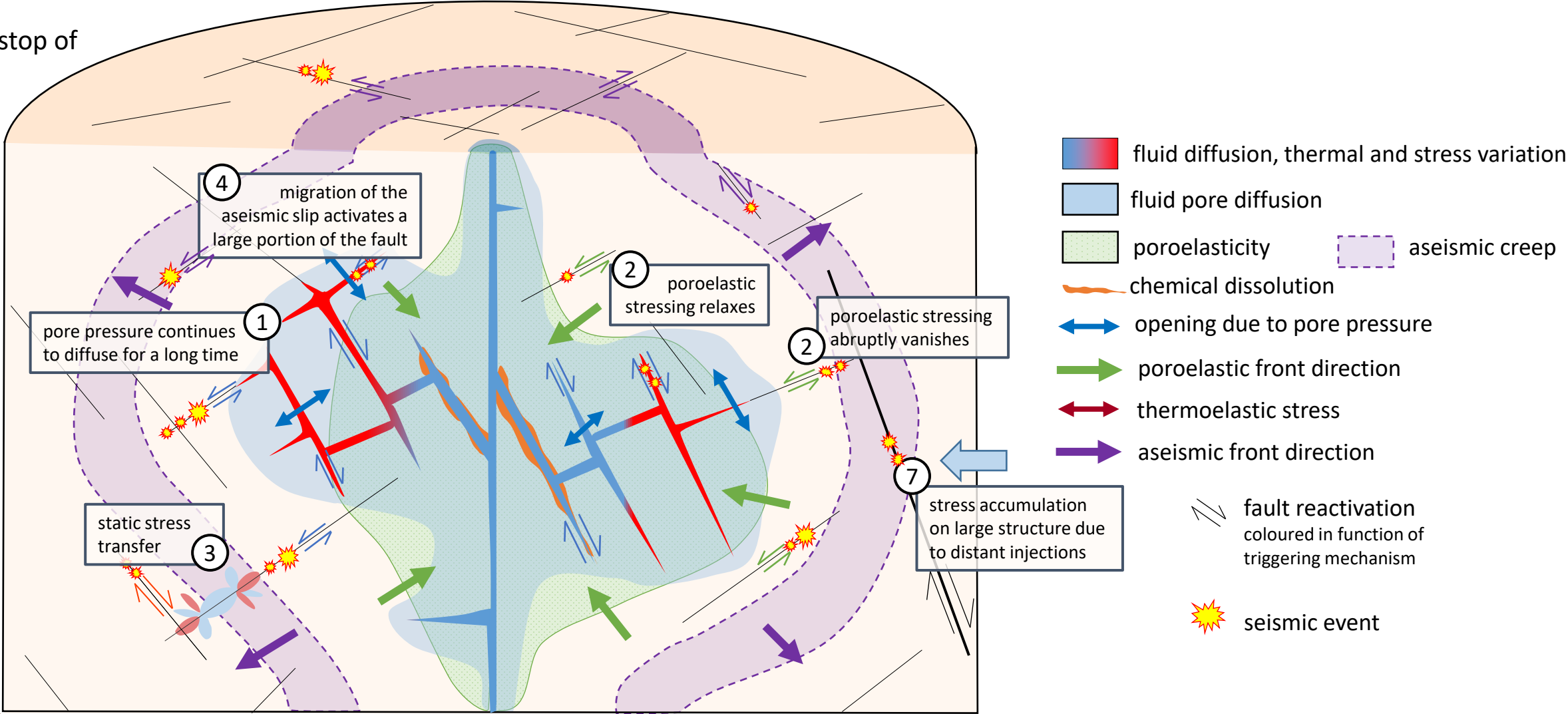
during injection



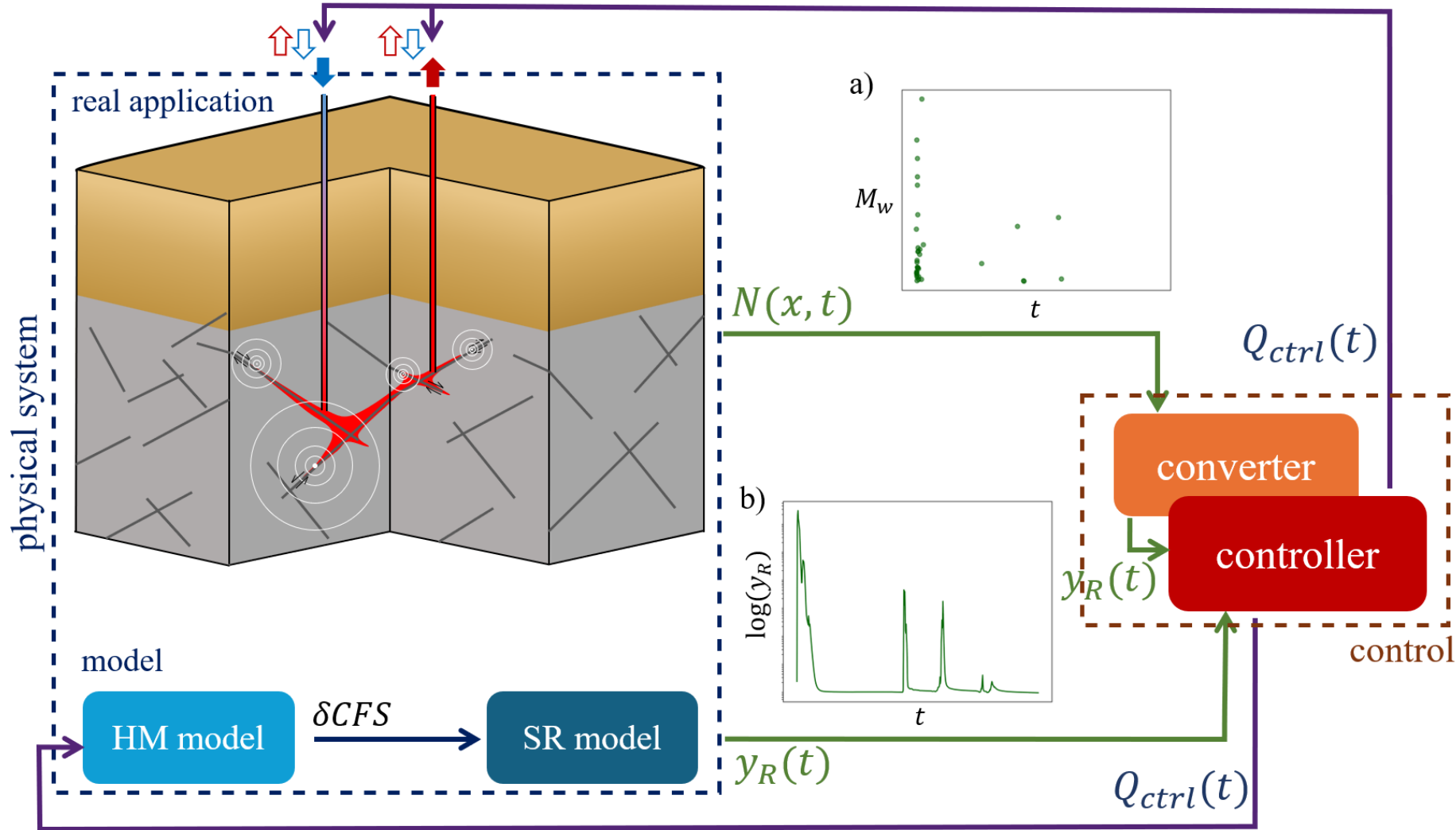
-  fluid diffusion, thermal and stress variation
-  fluid pore diffusion
-  poroelasticity
-  aseismic creep
-  chemical dissolution
-  opening due to pore pressure
-  poroelastic front direction
-  thermoelastic stress
-  aseismic front direction
-  fault reactivation  
coloured in function of  
triggering mechanism
-  seismic event

# After the stop of injection, the mechanisms continues to affect the stability of the pre-existing faulting network

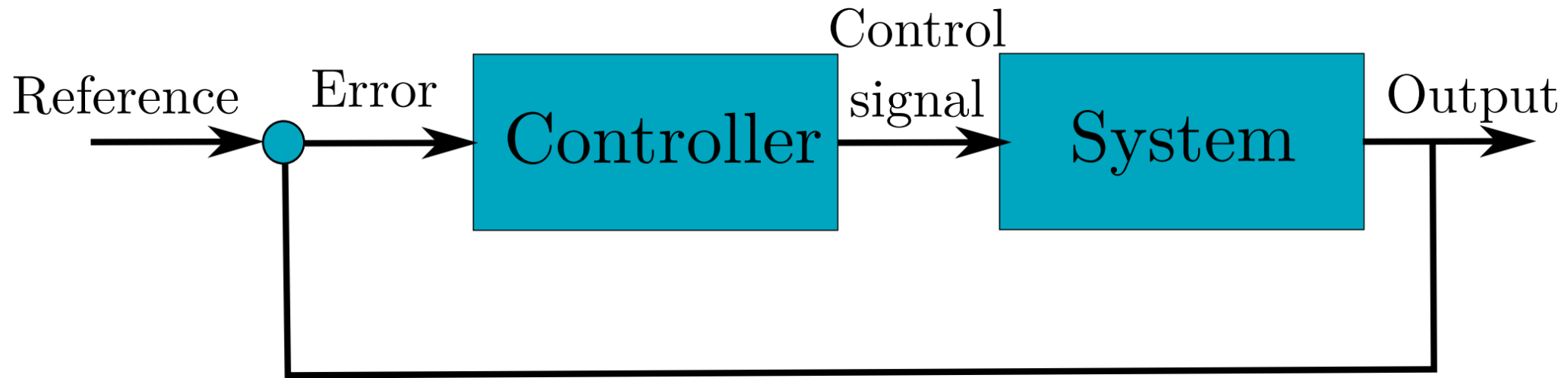
after the stop of injection



# Control theory brings a new paradigm for the prevention and mitigation of induced seismicity in geo-energy applications



Control theory is an automated closed-loop dynamic system set to force the system to achieve a desired reference or behaviour



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Nonlinear proportional–integral controller:

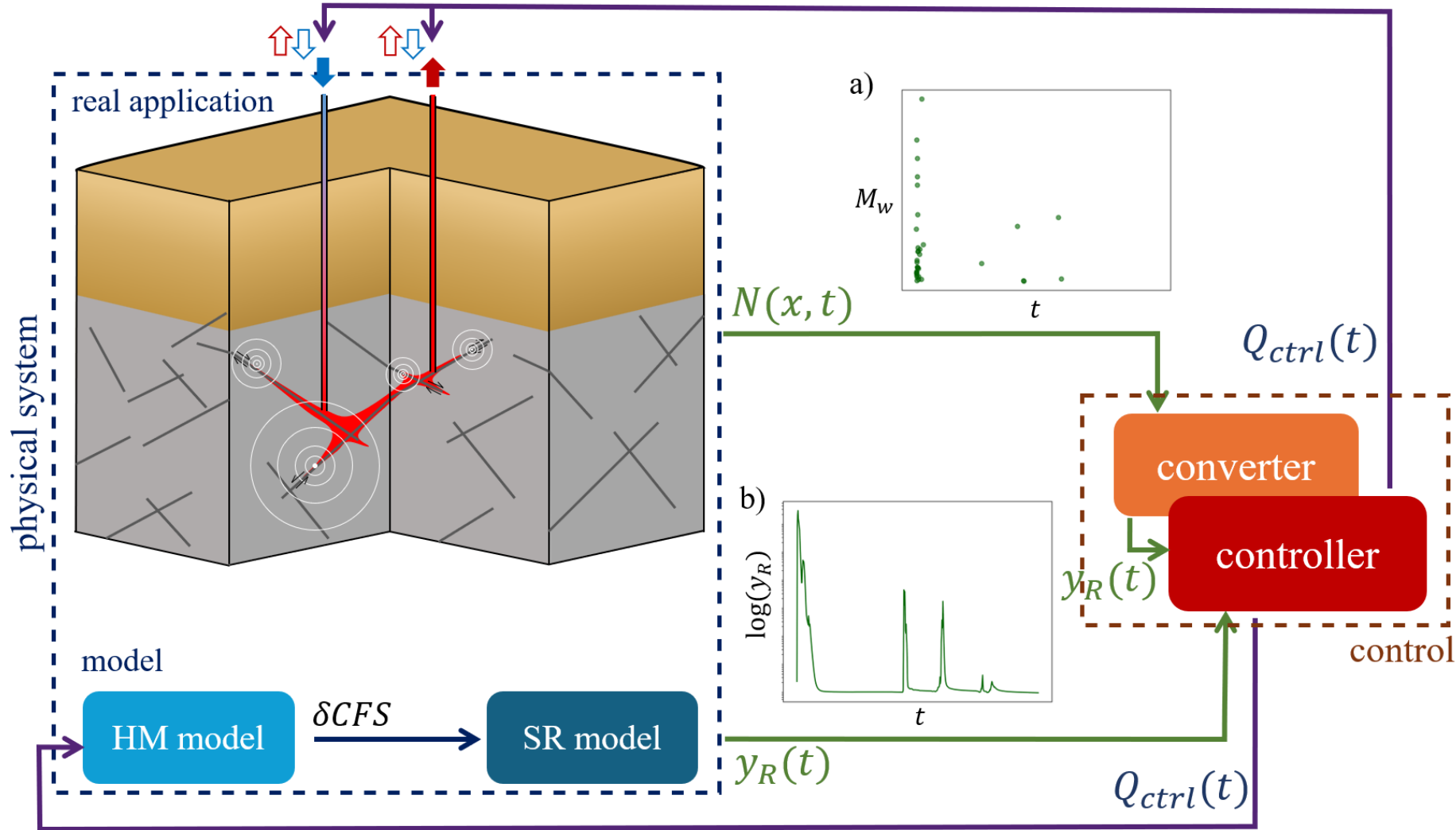
- continuously adjusts a system's input to reach and maintain a desired target.

It combines three actions:

- (a) the **Proportional** term reacts to the current error
- (b) the **Integral** term corrects accumulated past errors

Each one of them has gains, that need tuning to make the controller efficient and feasible in terms of technological limitations

# Control theory brings a new paradigm for the prevention and mitigation of induced seismicity in geo-energy applications



The governing equation couples the fluid diffusion and the volumetric deformation of the rocks following the Biot's theory (Biot, 1941):

$$\beta \dot{p}(x, t) + \alpha \dot{u}_{i,i} = -q_{i,i}(x, t) + \sum_{i=1} B_i(x) Q_i(t) + \sum_{i=1}^m B_i^s(x) Q_i^s(t),$$

$$0 = (\lambda(x) + G(x))_{,i} u_{j,j}(x, t) + (G(x) u_{j,j}(x, t))_{,j} + \alpha p_{,i}(x, t),$$

$$q_i(x, t) = -\frac{k(x)}{\eta(x)} p_{,i}(x, t),$$

$$p(x, t) = u(x, t) = 0 \quad \forall x \in \partial V,$$

$p(x, t)$  - change of the fluid pressure in the reservoir due to fluid injections

$u_i(x, t)$  - displacement

$k(x)$  - permeability of the host rock

$\eta(x)$  - dynamic viscosity of the fluid

$\beta$  - mixture compressibility, i.e.,

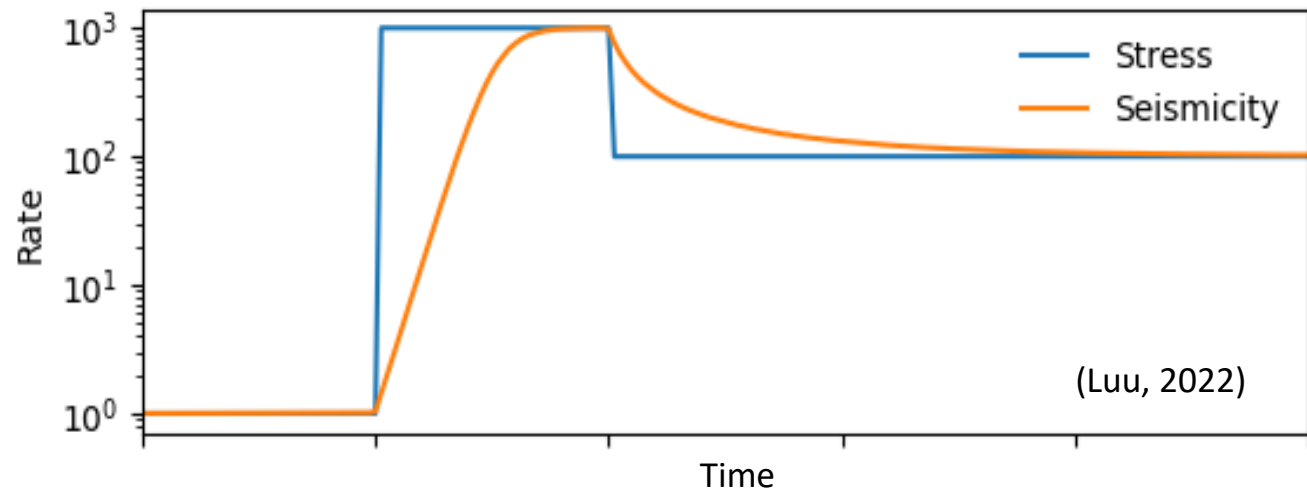
$\lambda(x)$  and  $G(x)$  - Lamé elastic parameters

$\alpha$  - Biot-Willis coefficient

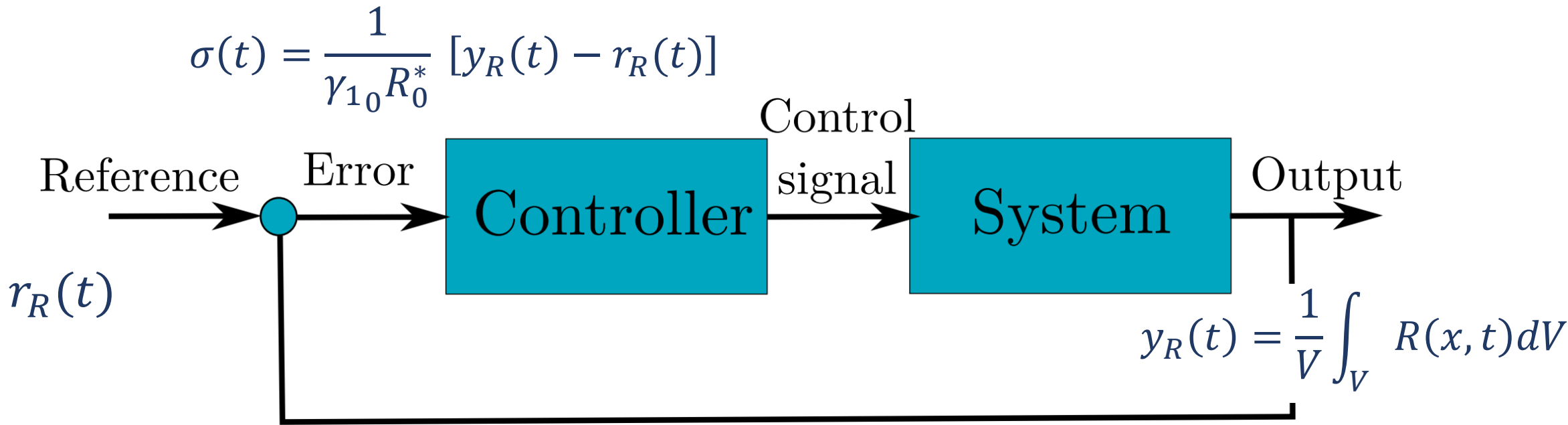
The stress changes are converted into seismicity rate following the Rate-and-State friction model (Dieterich, 1994; Segall& Lu, 2015), defined by:

$$\dot{R}(x, t) = \frac{R(x, t)}{t_a} \left( \frac{C\dot{F}S(x, t)}{\dot{\tau}_0} - R(x, t) \right),$$

$C\dot{F}S(x, t)$  - Coulomb Failure Stressing rate  
 $\dot{\tau}_0$  - background stressing rate  
 $t_a$  - characteristic decay time



The control-theoretical approach considers the seismicity rate of a region as the measurable output of the system and the background seismicity rate as the reference



$$Q_{ctrl}(t) = B_0^+ [-k_1 \phi_1(\sigma(t)) + v(t)]$$

$$\dot{v}(t) = -k_2 \phi_2(\sigma(t))$$

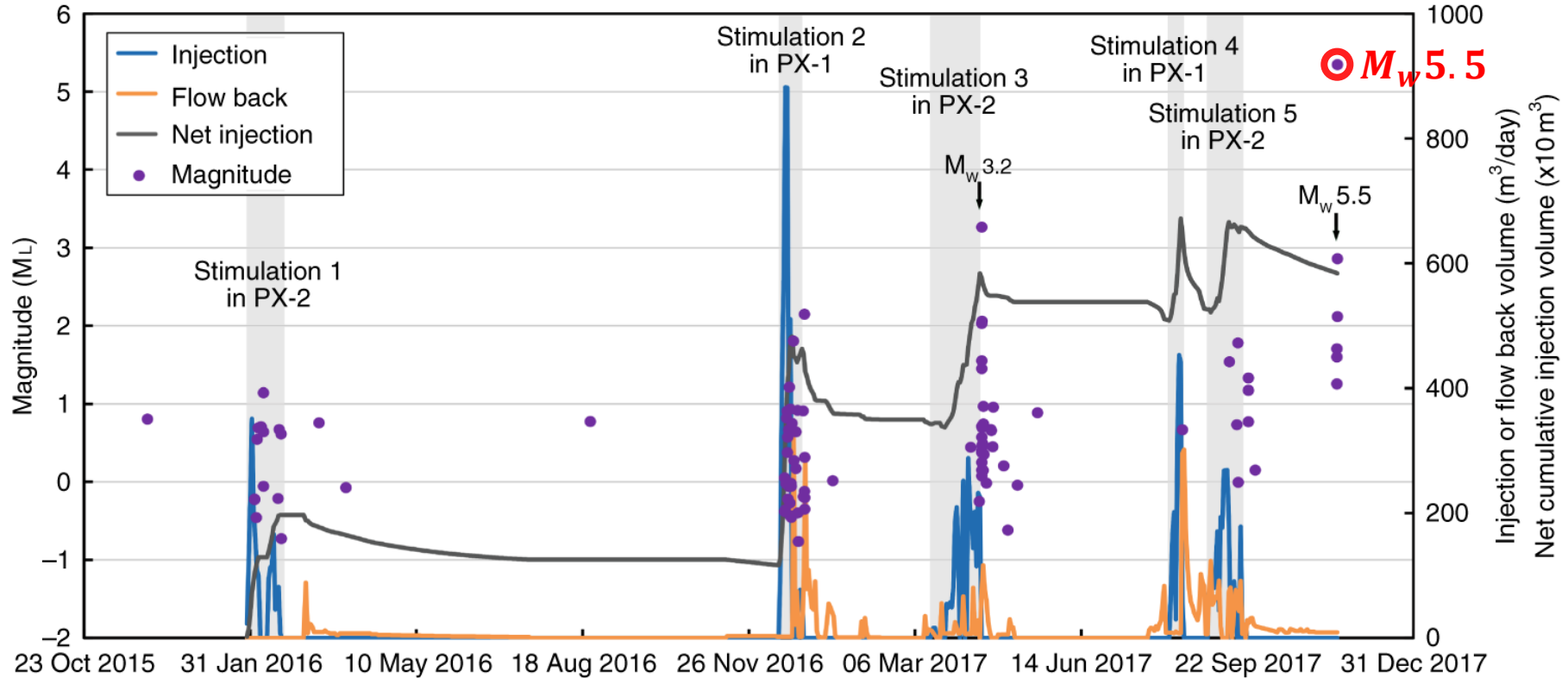
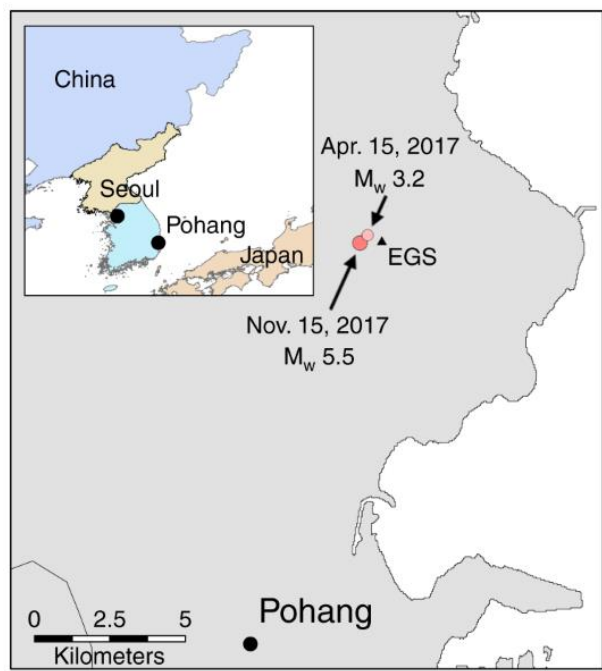
$\phi_1(\sigma) \phi_2(\sigma)$  - nonlinear functions of the error  
 $k_1, k_2$  - tuning parameters  
 $B_0$  - matrix with nominal values of the system

Gutiérrez-Oribio and Stefanou (2026), arXiv:2412.06327



The Pohang EGS was initiated in 2016 and five hydraulic stimulations were operated over two years. A post-injection earthquake of magnitude  $M_w$  5.5, occurred two months after the stop of the fifth stimulation.

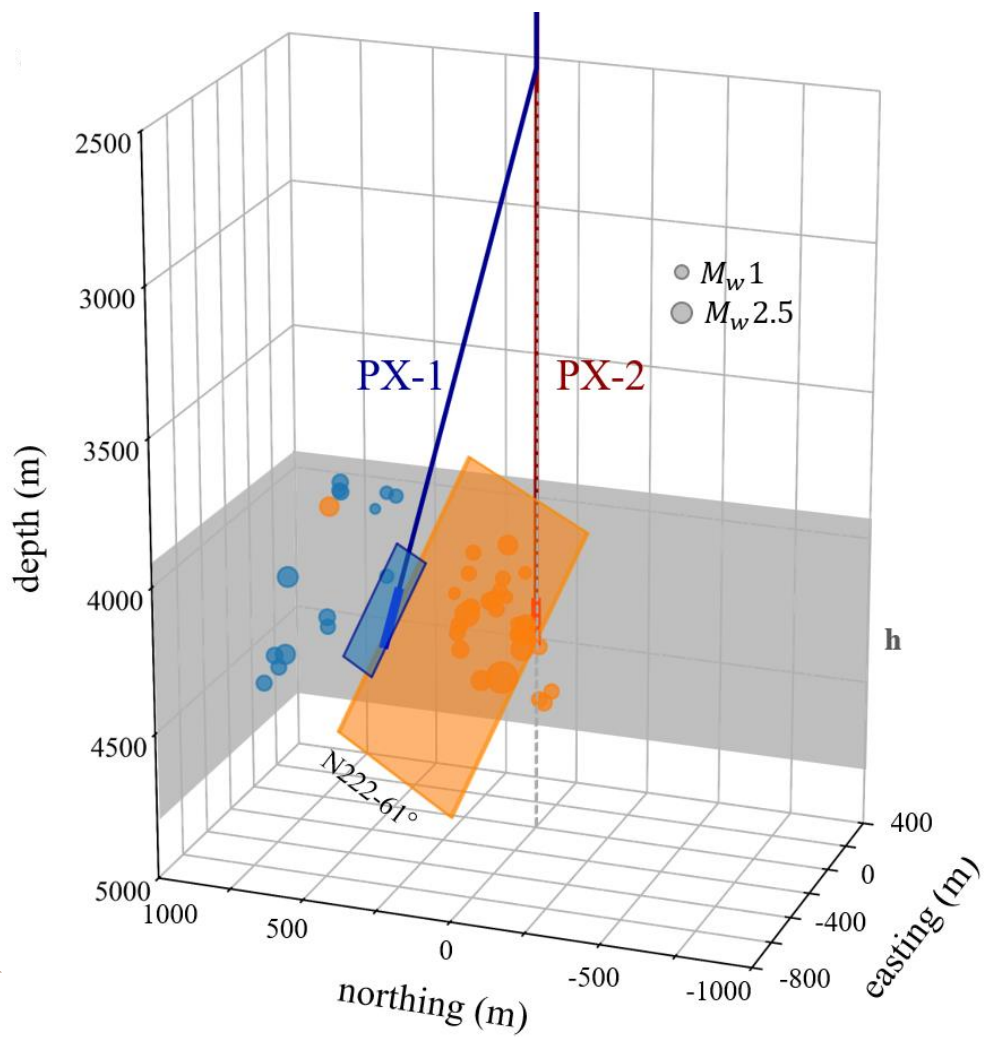
### Injection and induced earthquakes during the two-year stimulations



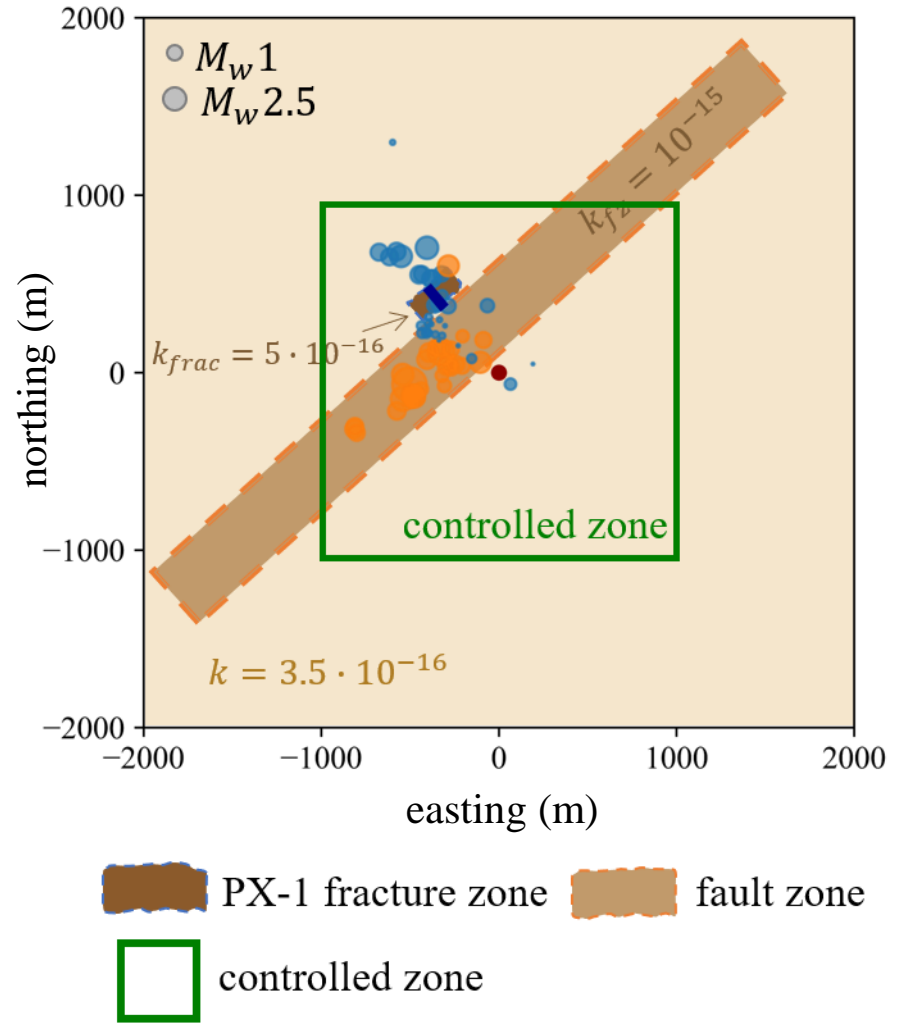
(Yeo et al., 2020)

# We model the Pohang EGS in a 2D depth-average coupled hydromechanical model simulating poroelasticity

Seismic data monitored during the PX-1 and the PX-2 stimulations

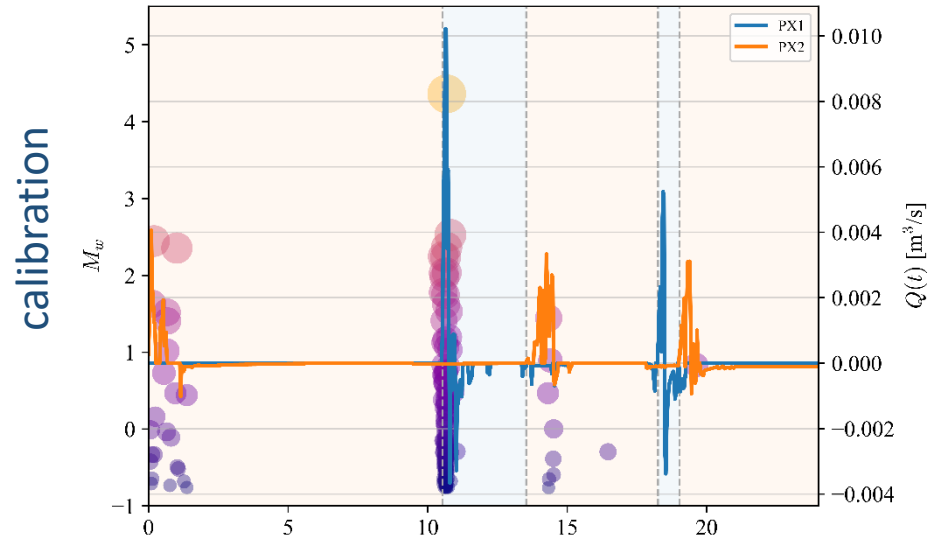


Model settings of the 2D modeling considering depth-average

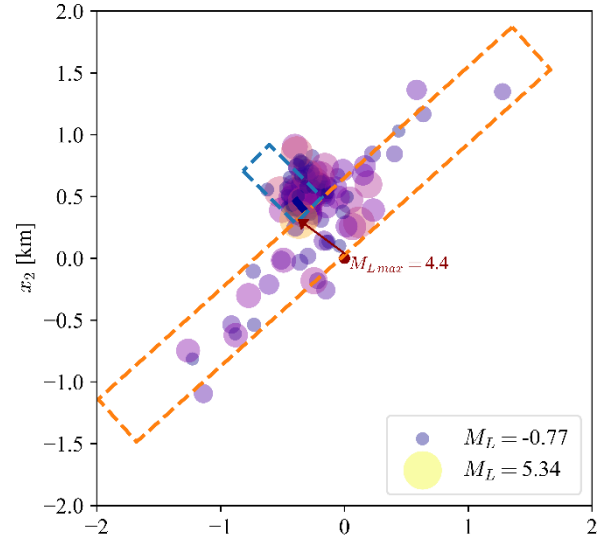


# The controller is efficient for the case of induced discrete events (converted in seismicity rate) to prevent seismicity

### Injection fluxes and magnitude of discrete seismic events



### Discrete seismic events

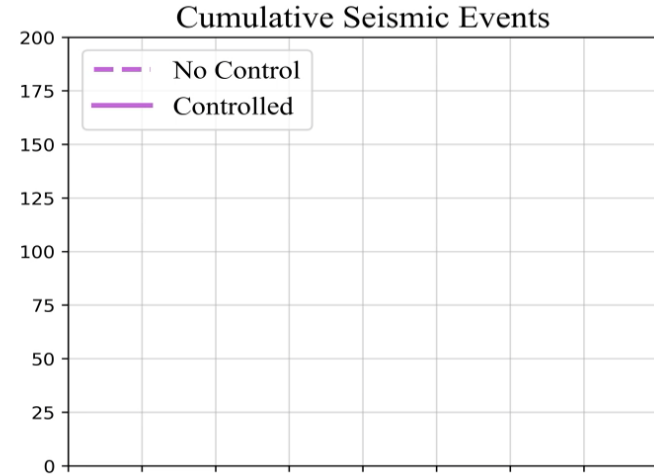
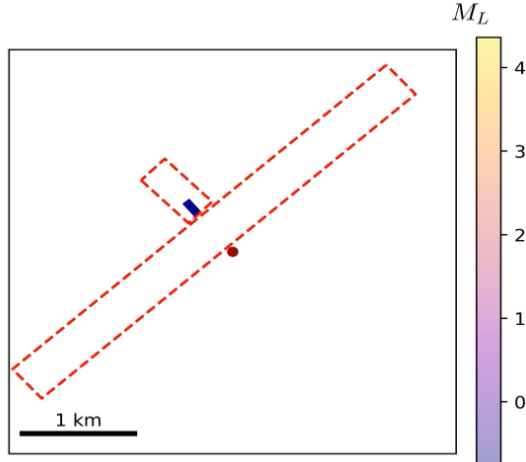
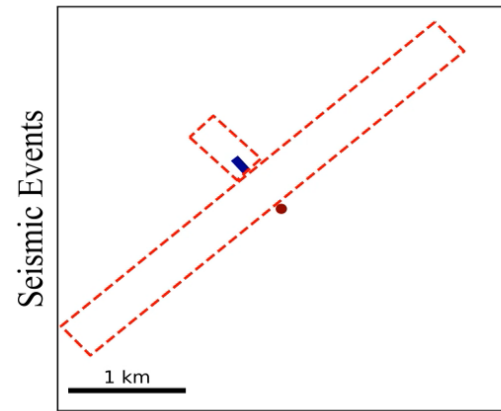
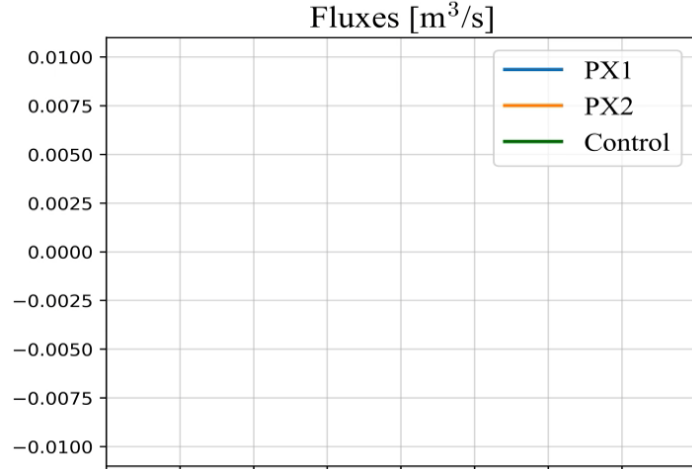
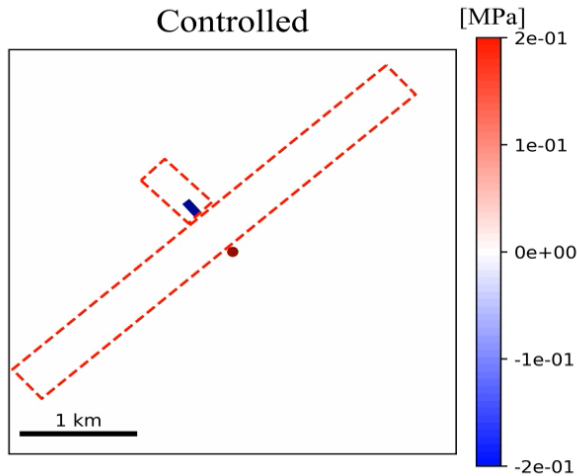
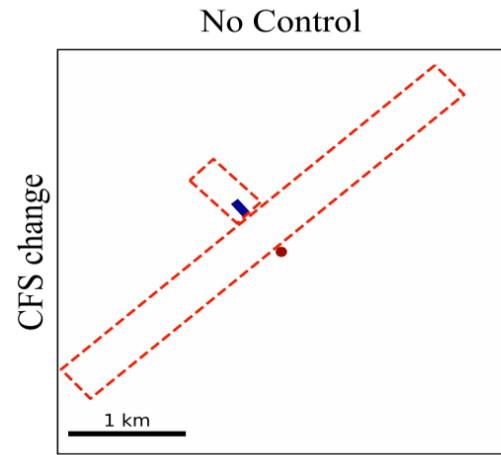


# The controller, considering discrete events, is also efficient to prevent seismicity during the two-year stimulations

## Discrete seismic events

## Injection fluxes and cumulative number of earthquakes

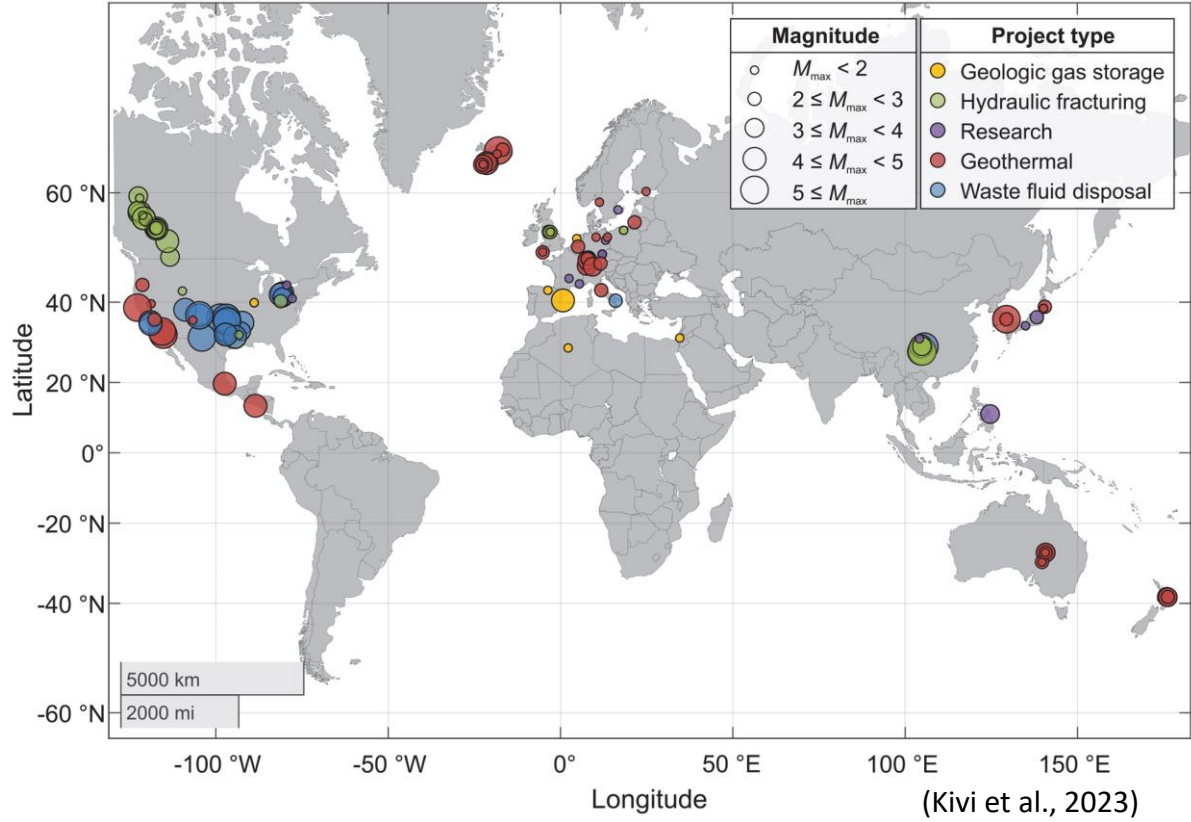
Pohang, 0.0 months



The control-theoretic approach has long path to be achievable in real application and development of models and controllers are necessary

### Limitations and future works:

- The models are simplifications of the real triggering mechanisms and seismic phenomena,
- Fractures and faults need to be considered as discrete, with plastic behavior
- The actuators are not physically limited and can change sign





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*This work is supported by the ERC grant INJECT, no. 101087771, doi: 10.3030/101087771, by the European Union.*

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# Control theory : a (small) introduction

Consider the simple system

$$\dot{x}_1 = x_2,$$

$$\dot{x}_2 = u.$$

$x_1, x_2$  - State variables (position and velocity)

$u$  - Control input (force)

**Objective:** Design the input  $u$  to follow a **constant** reference  $r$  on the state  $x_1$  (**regulation**).

# Control theory : a (small) introduction

Introducing the error:

$$e_1 = x_1 - r \quad e_2 = x_2 - \dot{r} = x_2$$

Error system:

$$\begin{aligned}\dot{e}_1 &= e_2, \\ \dot{e}_2 &= u.\end{aligned}$$

Question: Are they the same system?

**Difference:** If  $t \rightarrow \infty$ ,  $e_1, e_2 \rightarrow 0$  solved the regulation problem!

# Control theory : a (small) introduction

PID control:  $u = -k_P e_1 - k_D e_2 - k_I \zeta,$

$$\dot{\zeta} = e_1,$$

Closed-loop system:  $\dot{e}_1 = e_2,$

$$\dot{e}_2 = -k_P e_1 - k_D e_2 - k_I \zeta,$$

$$\dot{\zeta} = e_1.$$

**How to chose the gains  $k_P, k_D, k_I$  ?**

# Control theory : a (small) introduction

System matrix:

$$A = \begin{bmatrix} 0 & 1 & 0 \\ -k_P & -k_D & -k_I \\ 1 & 0 & 0 \end{bmatrix}$$

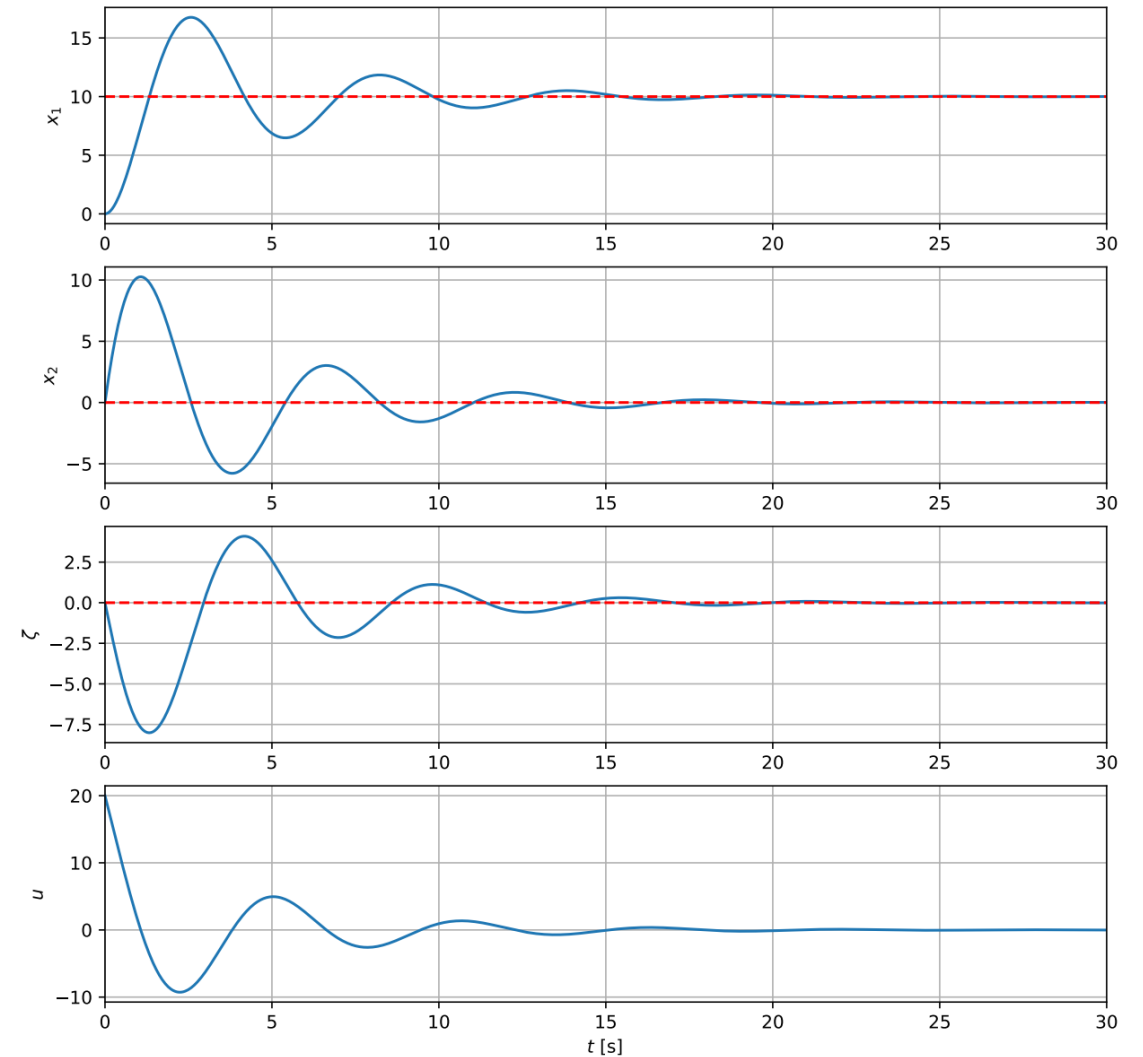
Characteristic equation:

$$s^3 + k_D s^2 + k_P s + k_I = 0$$

Exponentially stable if:

$$k_P > 0, \quad k_D > 0, \quad k_I < k_P k_D$$

Solution with  $k_P=2$ ,  $k_D=2$ ,  $k_I=2$



# Control theory : a robust control design

Output of the system:

$$y_R(t) = \frac{1}{V} \int_V R(x, t) dV$$

Reference for SR

$$r_R(t)$$

Error variable:

$$\sigma(t) = \frac{1}{\gamma_{10} R_0^*} [y_R(t) - r_R(t)]$$

# Control theory : a robust control design

$$Q_{ctrl}(t) = B_0^+ \left[ -k_1 \phi_1(\sigma(t)) + \nu(t) \right],$$
$$\dot{\nu}(t) = -k_2 \phi_2(\sigma(t)),$$

$\phi_1(\sigma)$   $\phi_2(\sigma)$  - nonlinear functions of the error

$k_1, k_2$  - tuning parameters

$B_0$  - matrix with nominal values of the system

## Analytic results:

- Exact tracking of the reference.
- Requires minimum information of the system.
- Agnostic against uncertainties and external perturbations.
- Finite-time or exponential convergence.

# Control theory : Sketch of the proof

Closed-loop error dynamics :

$$\dot{\sigma} = [\mathbb{I}_m + \Delta B(t)] [-k_1 \phi_1(\sigma) + \sigma_I],$$

$$\dot{\sigma}_I = -k_2 \phi_2(\sigma) + \dot{\Psi}(t).$$

The control  $Q(t)$  will work if:

$$\|\Delta B(t)\| \leq \delta_B < 1,$$

$$\|\dot{\Psi}(t)\| \leq \delta,$$

# Control theory : Sketch of the proof

Using Lyapunov theory, we can conclude :

$$\|u(x, t)\|_{L^2(V)} \leq \Gamma_u,$$

$$\|u_t(x, t)\|_{L^2(V)} \leq \Gamma_{u_t},$$

$$\|R(x, t)\|_{L^2(V)} \leq \Gamma_R,$$

$$\|R_t(x, t)\|_{L^2(V)} \leq \Gamma_{R_t},$$

Which ensures the existence of  $\delta_B, \delta$