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# Etude expérimentale de la localisation des déformations dans les roches en utilisant des méthodes de mesure de champs

an experimental insight into the mechanisms of localized deformation in rocks

Cino Viggiani



+ Steve Hall, Nicolas Lenoir, Pierre Bésuelle, Jacques Desrues, Michel Bornert, Elma Charalampidou, Sergei Stanchits, Erika Tudisco, Philippe Roux, ...

- how can we model localized deformation ?
- • how can we investigate it in the lab ?

two examples: (1) clay rock and (2) sandstone

first, time for a coffee...

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Neutron Radiography to look  
inside an italian coffee maker

(there is plenty of fun things that  
one can do with full-field methods)





to fully understand the mechanisms at play  
it is important to

- see inside test specimens (when possible)
- characterize the “full-field” behavior
- employ techniques sensitive to the phenomena of interest

→ full-field methods

## full-field measurements: what and how

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the fields that can be measured concern **a range of physical variables**, which may be scalars (*e.g.*, temperature), vectors (*e.g.*, displacement) or even tensors (*e.g.*, strain)

for each of such variables, **many different techniques** exist (each of them having its advantages and its limitations)

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- Optical Methods for Kinematics (speckle, speckle interferometry, geometric moiré, moiré interferometry, holographic interferometry, image correlation, grid method, ...)
- Ultrasonic Tomography
- Magnetic Resonance Imaging (MRI)
- Electrical Resistivity Tomography
- Neutron Tomography
- X-ray Tomography
- ... → see review paper by Viggiani & Hall (2008)

## full-field measurements - why?

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qualitative and quantitative characterization of **heterogeneities** in both **material properties** and **processes**



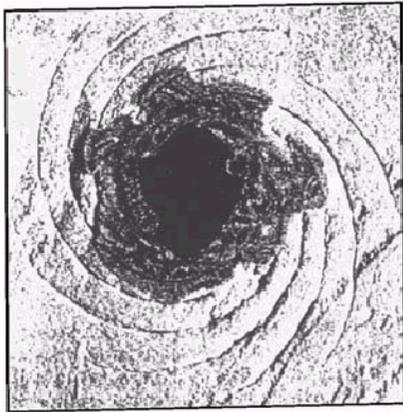
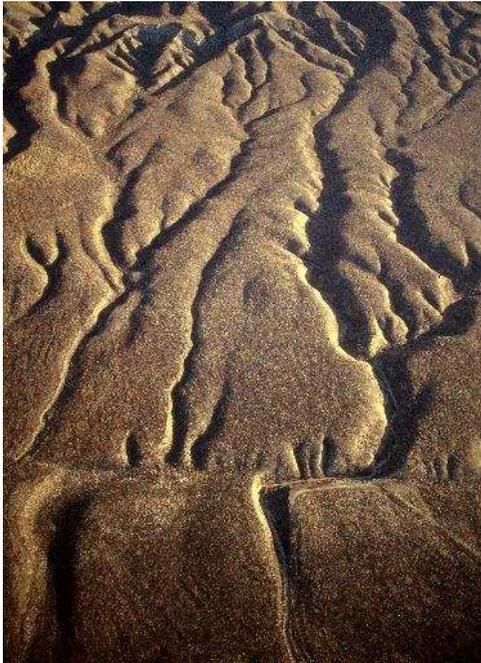
particularly attractive for geomechanics, because heterogeneity (at different scales) is the rule rather than the exception

useful in a number of ways:

- material characterization and specimen inspection
- assessment of actual test boundary conditions
- • tracking of heterogeneous response during a test
- validation and identification of models

this is ideal for studying mechanisms of **localized deformation** in rocks ( shear/compaction bands, tensile/shear cracks or fractures)

# strain localization



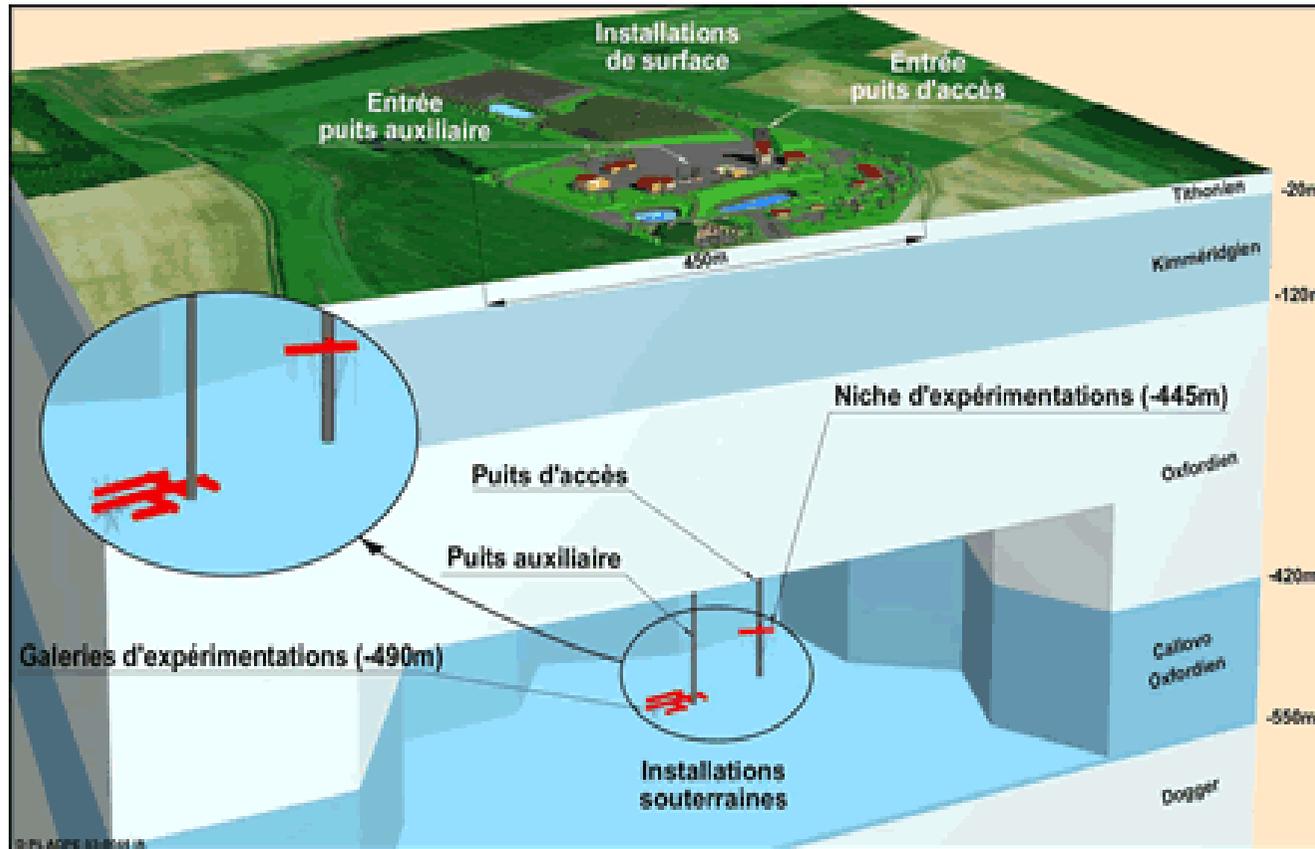
**example 1**

**localization in clay rock**

**(the invisible localization)**

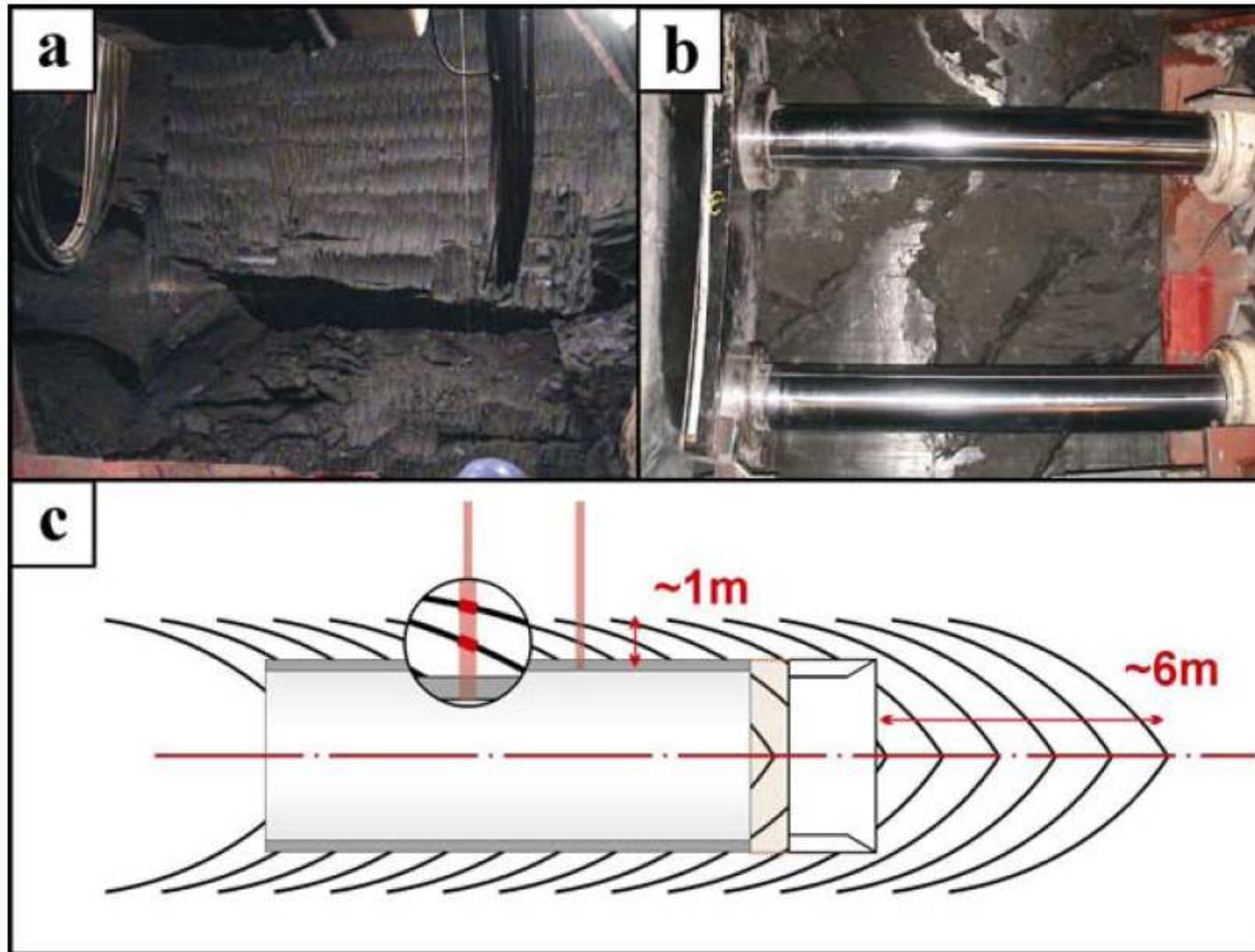
in-situ x-ray micro tomography + 3D DIC

radioactive waste disposal in deep underground galleries



URL in Bure (France) , depth: – 490m

EDZ around radioactive waste underground storage galleries



**DAMAGE/DEFORMATION** around deep excavations in clays **IS LOCALIZED !**

# patterns of localization observed in lab tests

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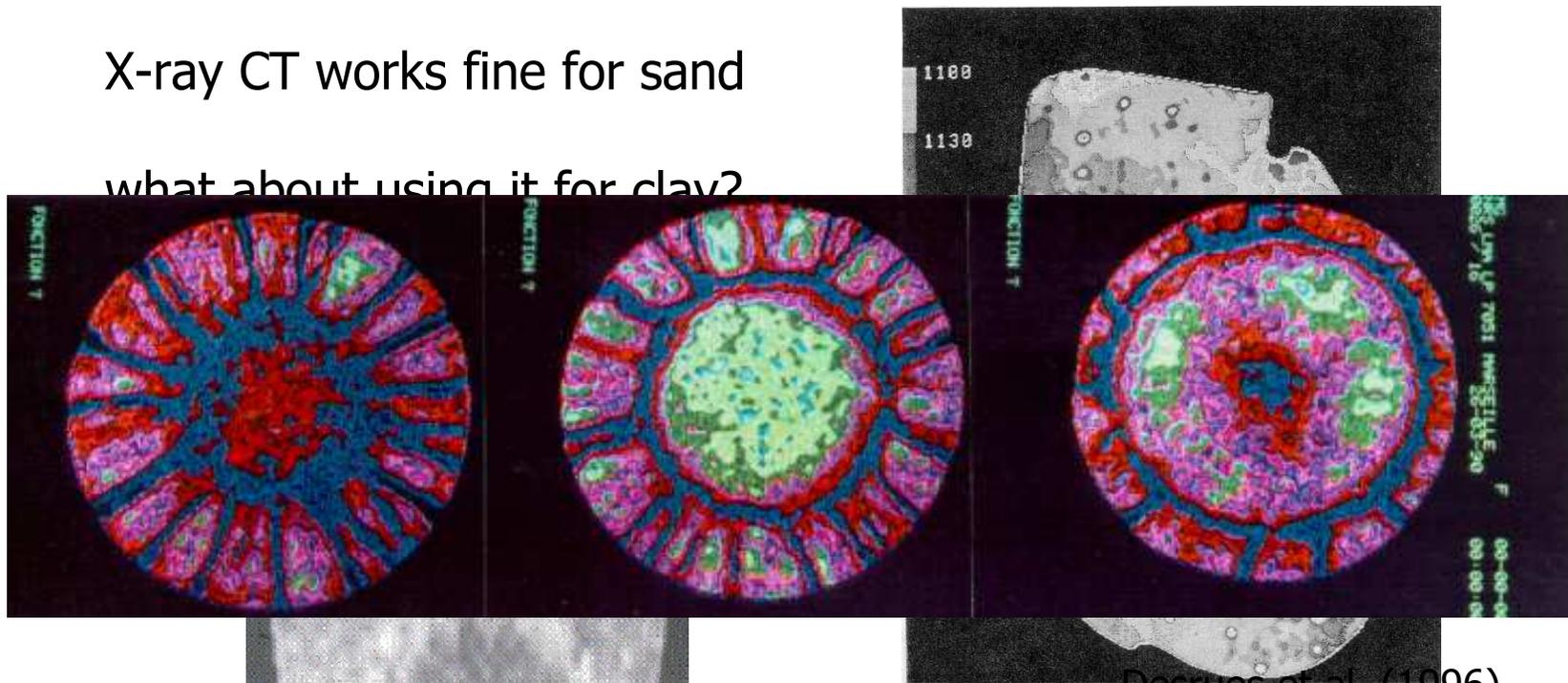
Opalinus Clay and Boom Clay tested in triaxial compression (Coll 2005 - SELFRAC)

## x-rays to study strain localization

non destructive 3D imaging techniques → X-ray tomography

X-ray CT works fine for sand

what about using it for clay?



Tillard (1992)

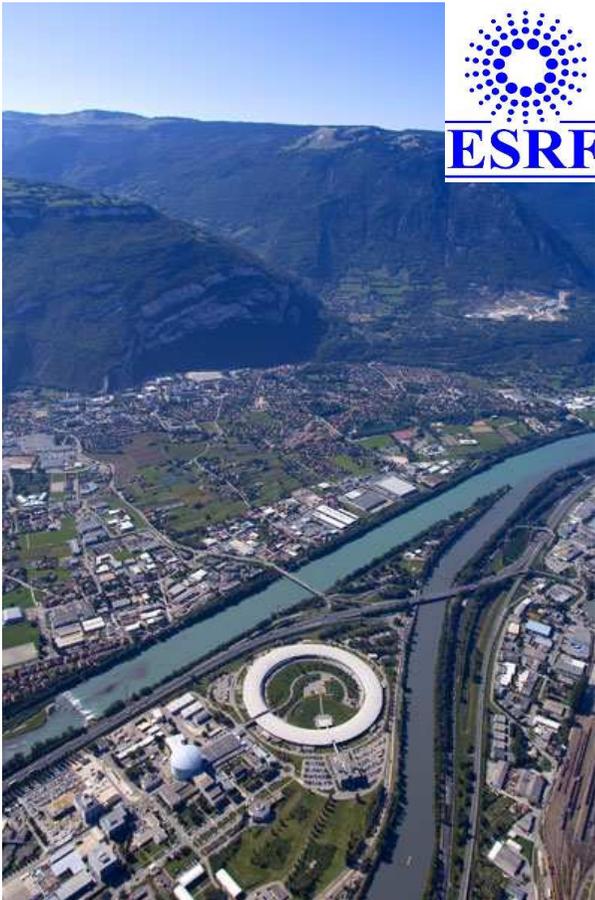
Desrues et al. (1996)  
Hicher et al. (1994)

→ spatial resolution was not enough

# micro x-ray CT at ESRF: a significant step forward

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... let's go high tech: synchrotron radiation micro tomography!



high-energy beamline **ID15A** at the **ESRF in Grenoble** (European Synchrotron Radiation Facility – collaboration w/ M. di Michiel)

## **key advantages:**

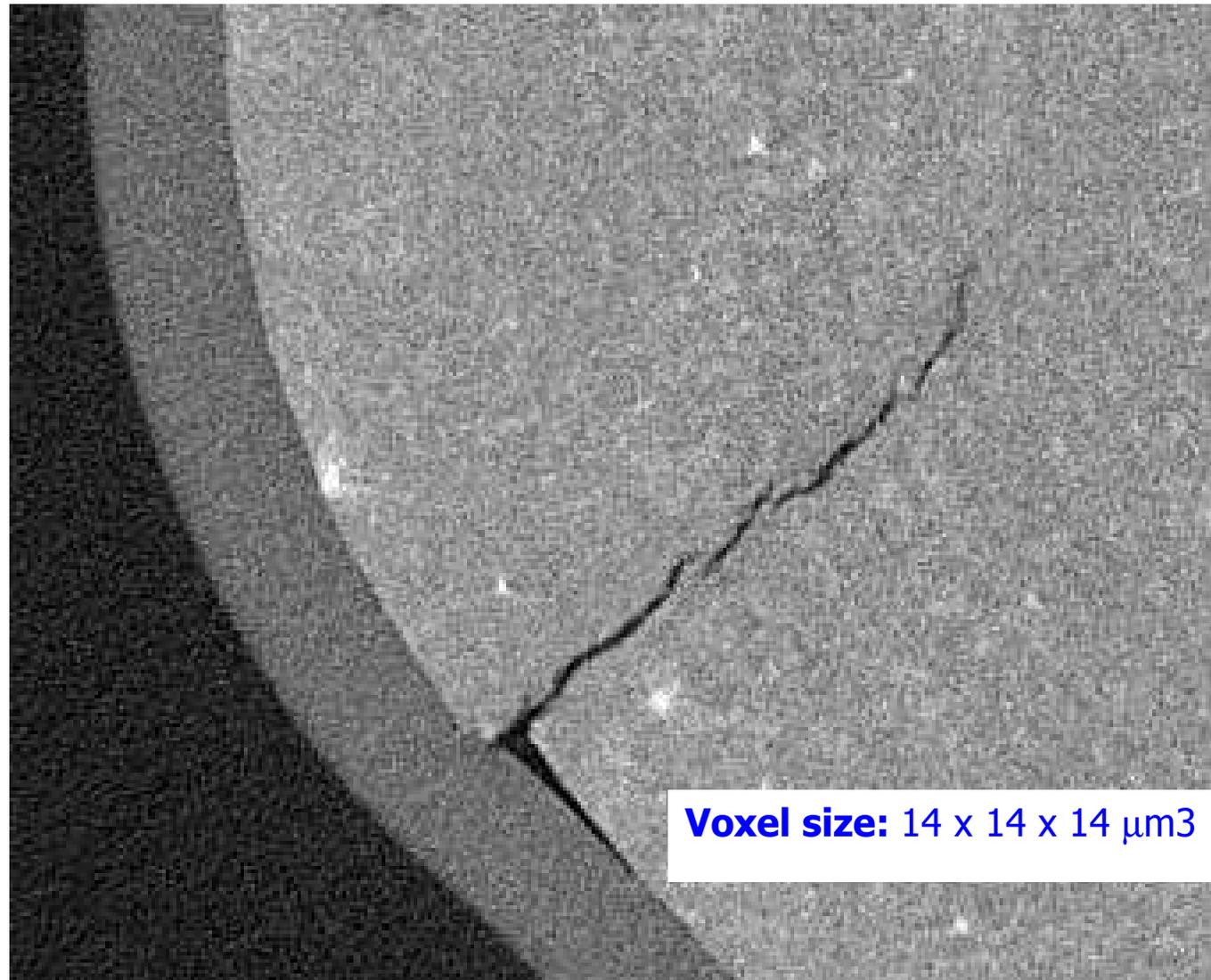
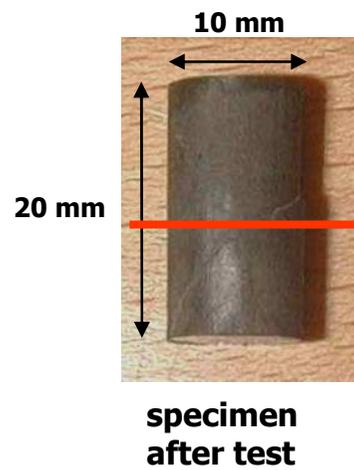
- ⇒ short scanning time
- ⇒ high resolution

acquisition of the entire specimen takes about **12 mins** (4 scans of overlapping vertical sections)

voxel size in the reconstructed volume is **14 x 14 x 14  $\mu\text{m}^3$**

# micro x-ray CT at ESRF: a significant step forward

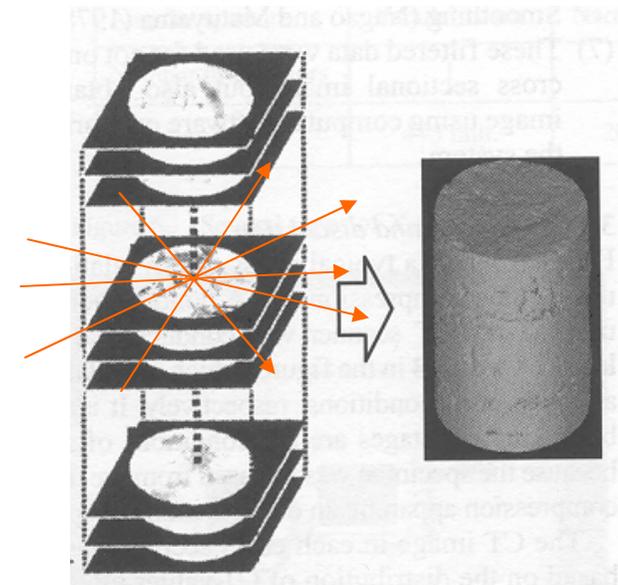
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# micro x-ray CT at ESRF

## basic principle

- recording attenuation profiles through a specimen slice, under different angular positions
- reconstructing a radiograph of the slice
- repeating to get a complete set of slices over the specimen
- reconstructing a 3D image of the internal structure of the specimen from the spatial distribution of the linear attenuation coefficient



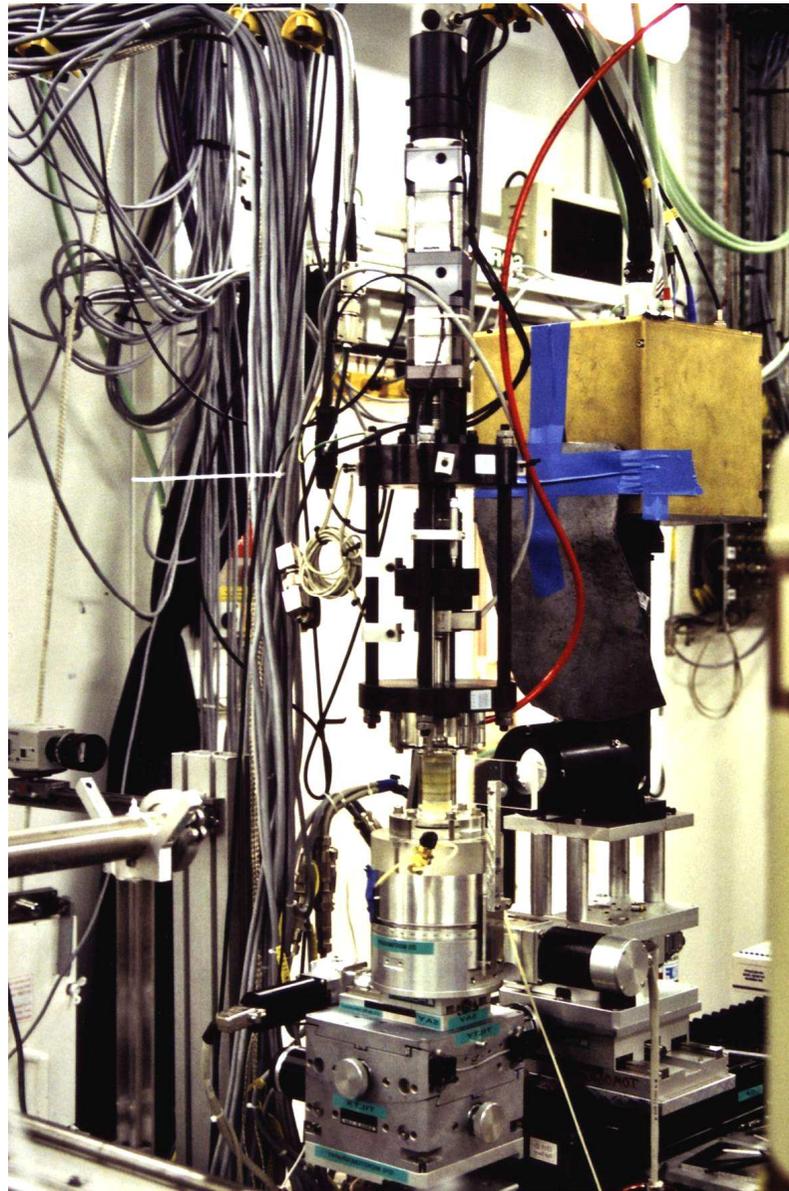
*ESRF, Grenoble (France)*

## x-ray characteristics

- x-ray white beam to have a **high photon flux**
- x-ray energy: 50 to 70 keV
- spatial resolution: **14  $\mu\text{m}$**  (voxel size)
- time for scanning: **12 to 15 minutes**

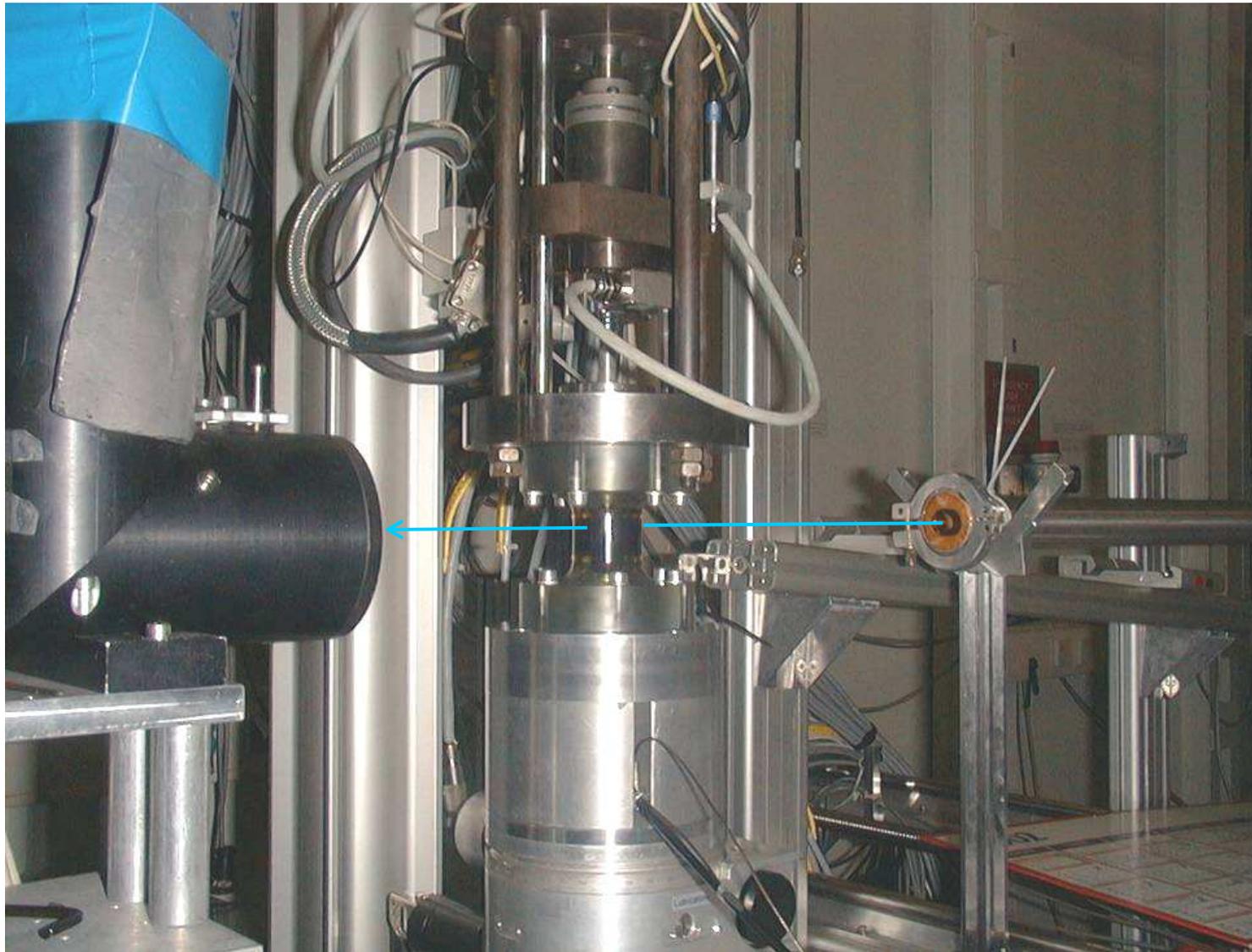
# experimental setup

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# experimental setup

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## Callovo-Oxfordian argillite

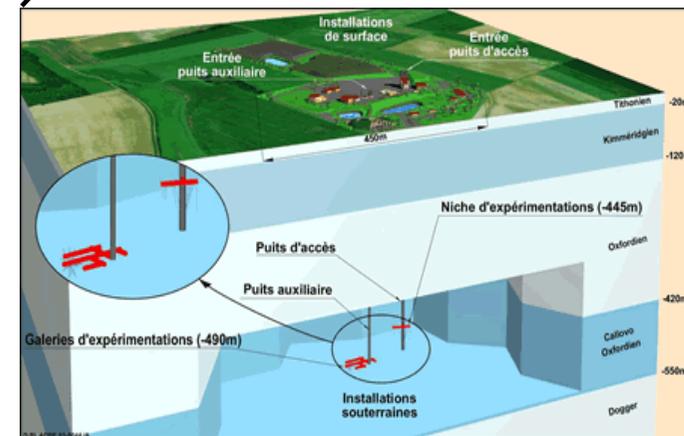
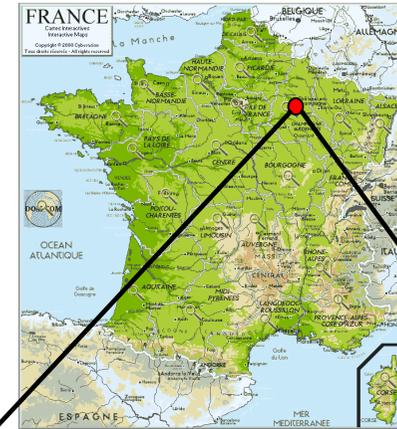
from the Borehole EST261 (depth 476m) of  
the Underground Research Laboratory of  
Bure (ANDRA)

## a few characteristics

clay content : 40 %

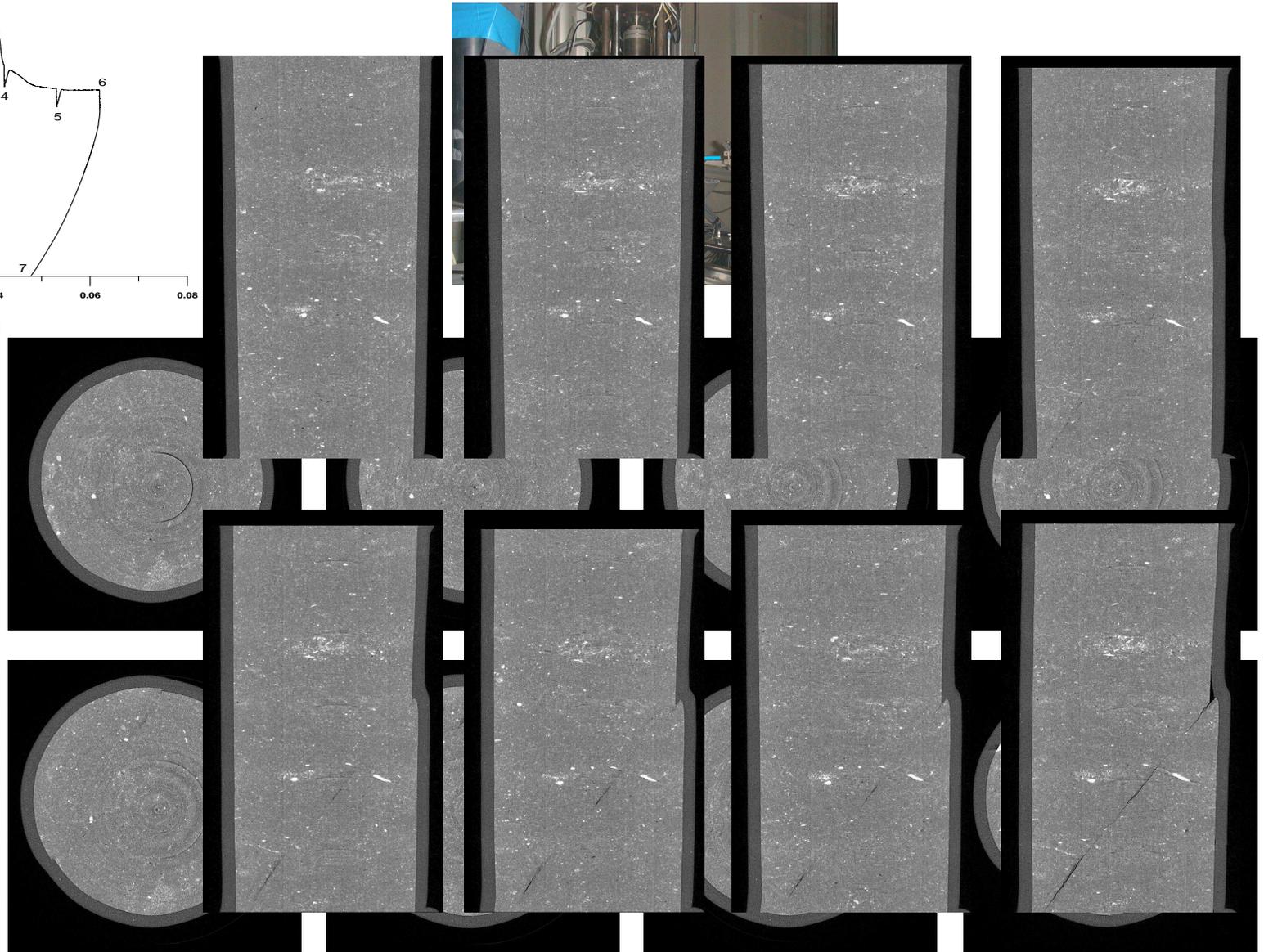
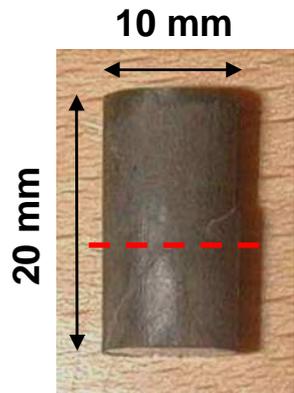
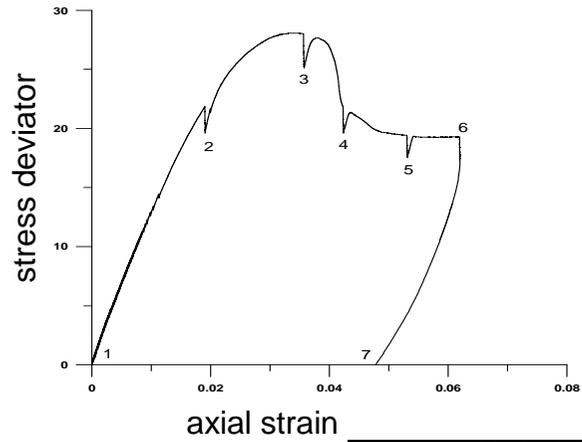
water content : 6 %

permeability :  $10^{-20}$  to  $10^{-22}$  m<sup>2</sup>



URL in Bure (France), depth: - 490m

# X-ray images from a test ( $\sigma_c = 10$ MPa)

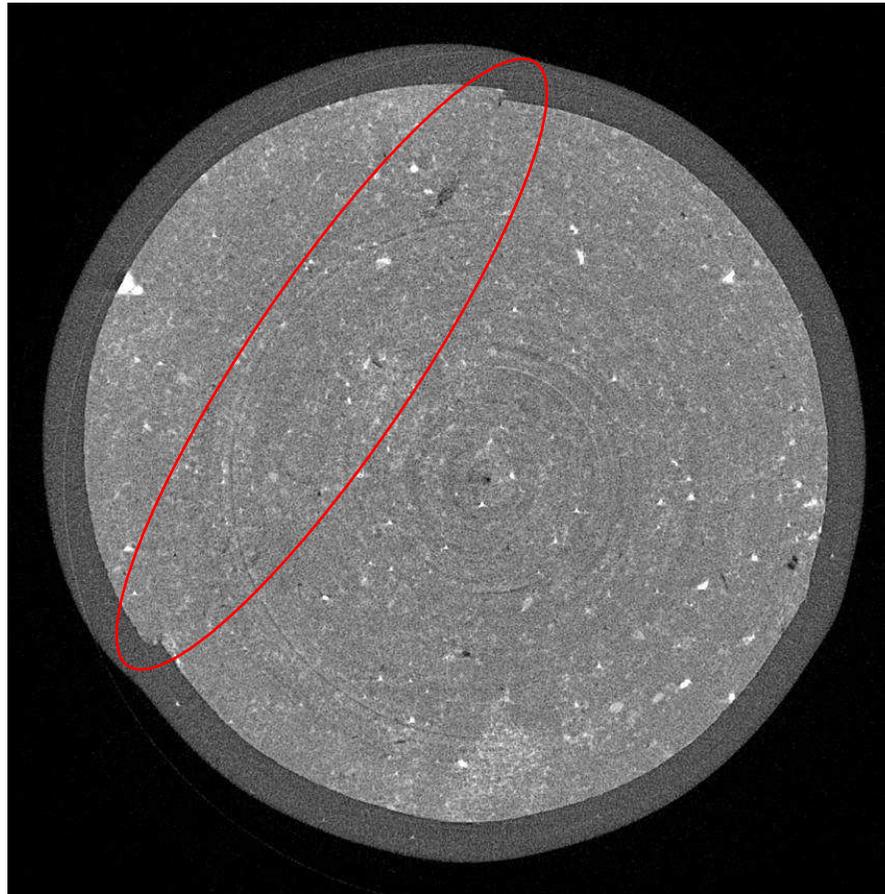




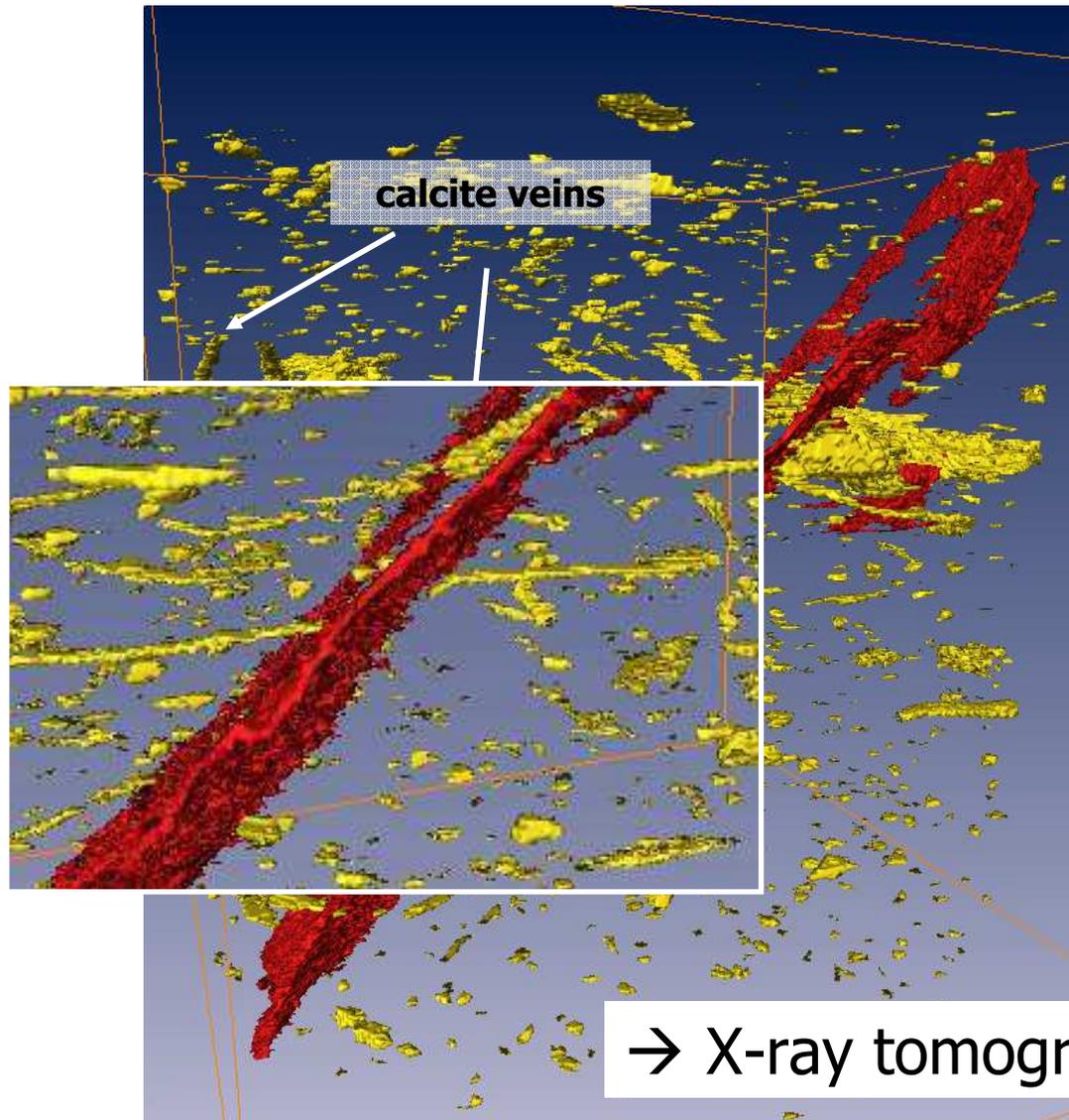
## what information can we get from these images?

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... and if density does not change ?  
*(mode II cracks, shear bands with no volume changes)*



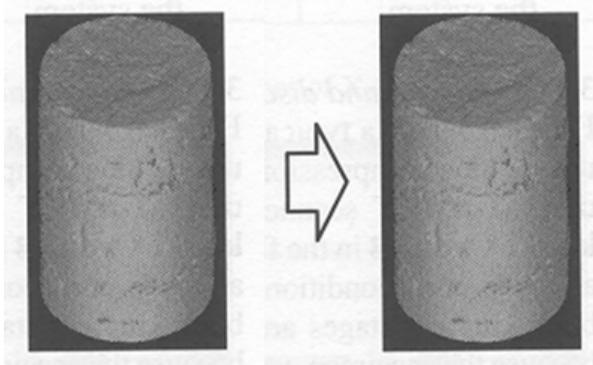
# X-ray images do not show everything



natural inclusions in yellow  
open cracks in red

→ X-ray tomography + 3D DIC

# basic principles of 3D DIC: mapping one digital image onto another



two 3D images of specimen at different loading/deformation levels

**definition of nodes** distributed in the first image

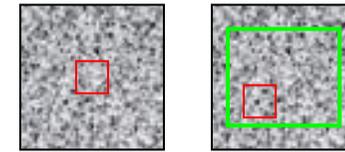
**definition of the "motif", or correlation window** (region about each node)

**calculation of a correlation coefficient** for each displacement of this motif, within a region ("search" window) about the target node in the second image

**definition of the discrete displacement** (integer number of pixels) i.e. that with the best correlation

**sub-pixel refinement** (because the displacements are rarely integers of pixels), which may also involve more complex transformations than simply rigidbody translation

**calculation of strain** from the displacements



search in 3D for best correlation  
displacement vector (integer - pixel)

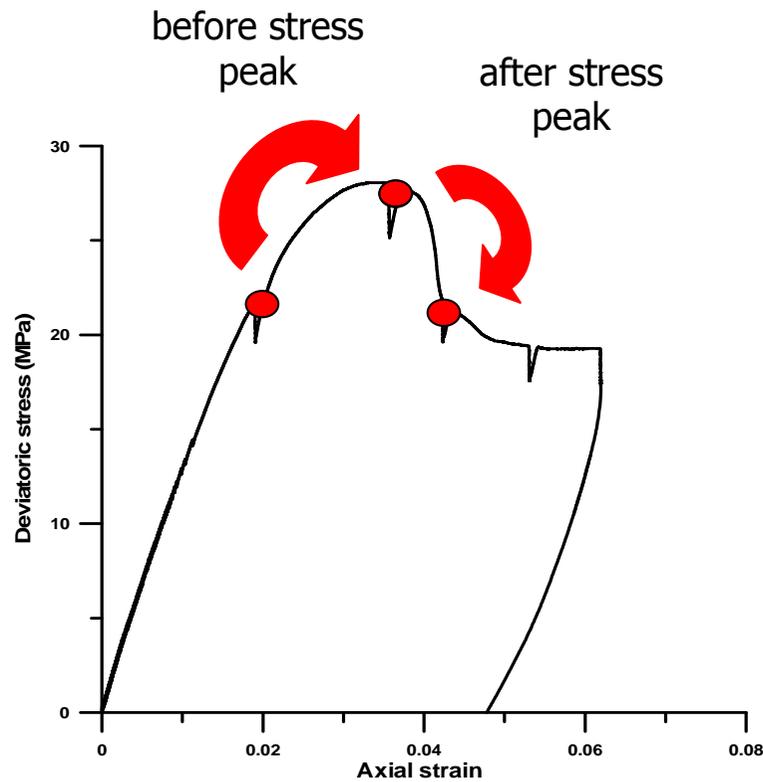
**sub-pixel  
refinement**

**interpolating correlation coefficient**  
fast, but can only assess rigid body motion  
**interpolating gray-level**  
slow, but more general transformations

**displacement field with sub-pixel accuracy [dx, dy, dz]**

# 3D DIC results from COX argillite

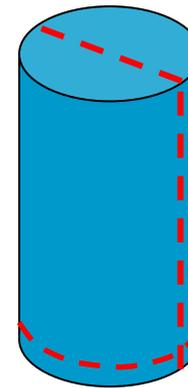
undrained compression,  $p_0 = 10$  MPa



3D DIC using CorrelManu3D

86247 nodes

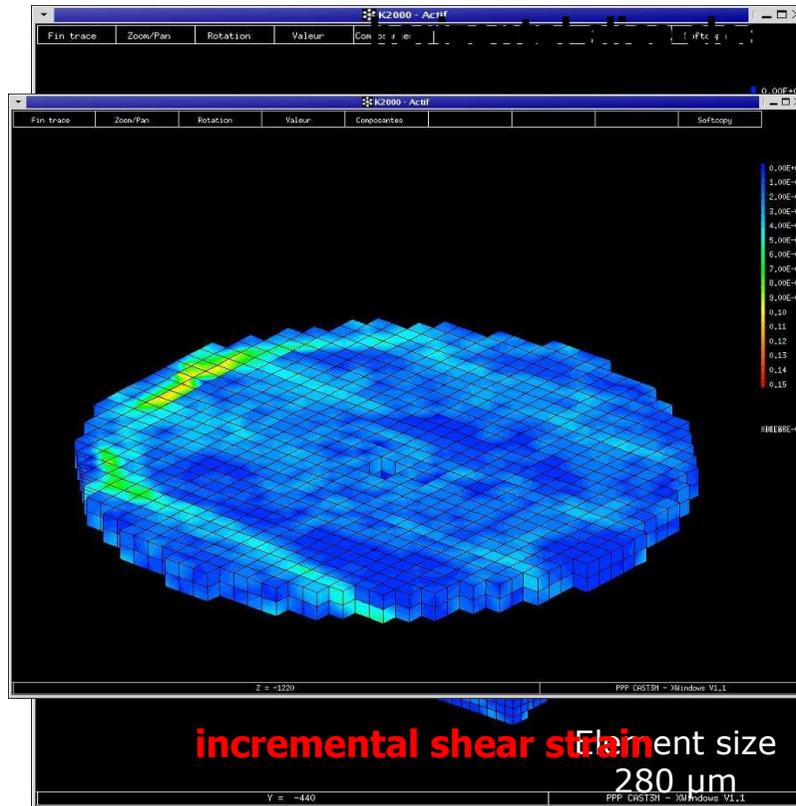
correlation window size = 20 voxels



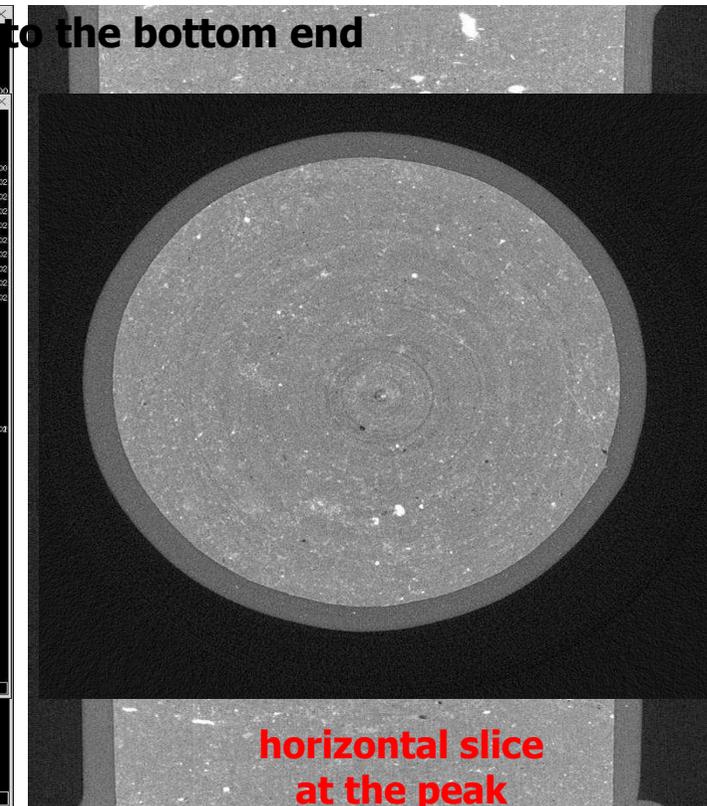
Lenoir et al. (2007) – Strain, International Journal for Experimental Mechanics, Vol. 43, No. 3, 193–205

# increment **before** stress peak

vertical slice along the axis



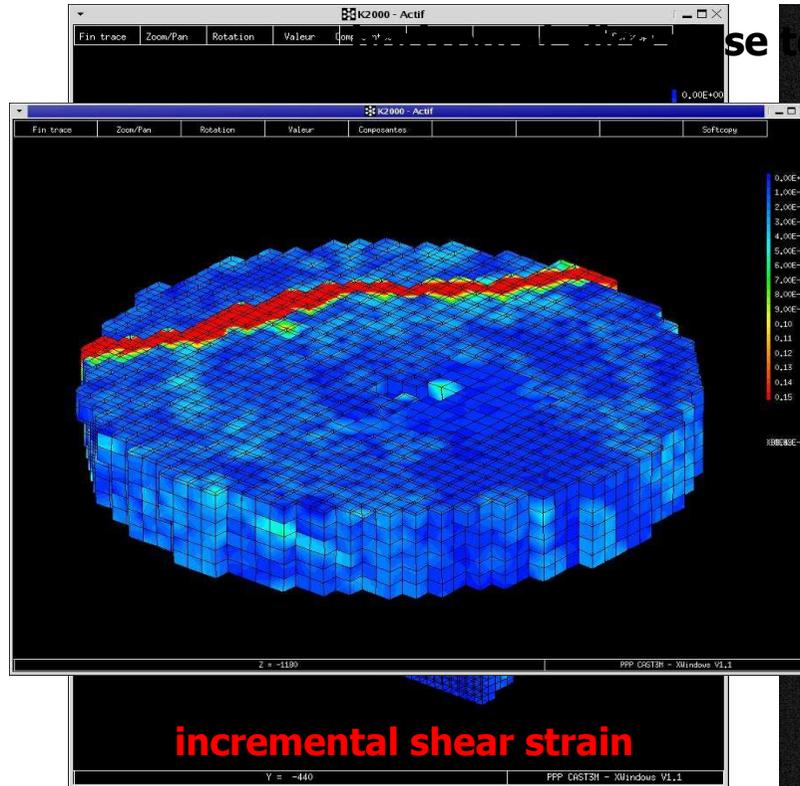
incremental shear strain



Lenoir et al. (2007) – Strain, International Journal for Experimental Mechanics, Vol. 43, No. 3, 193–205

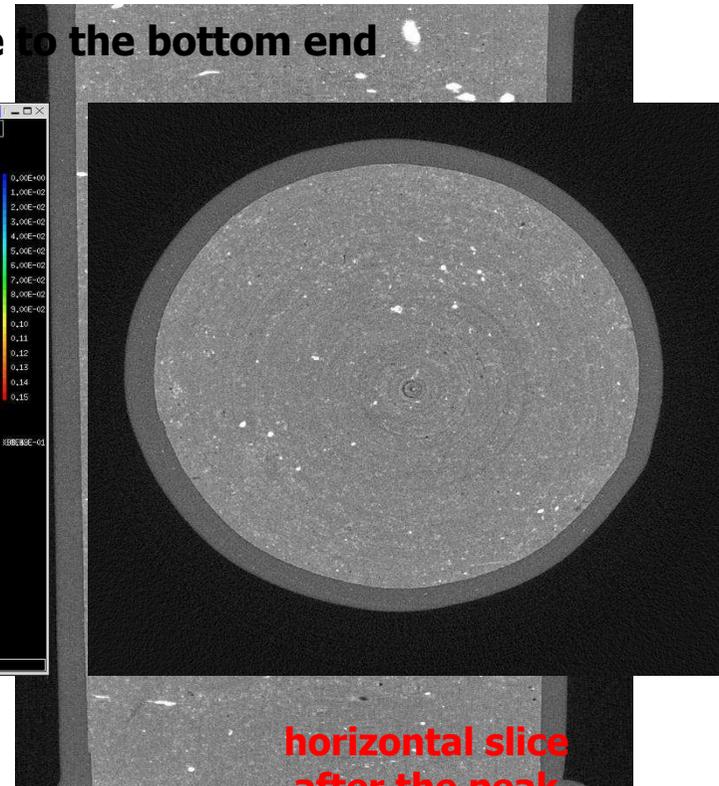
# increment **after** stress peak

vertical slice along the axis



**incremental shear strain**  
**incremental shear strain**

se to the bottom end



**horizontal slice**  
**after the peak**  
**vertical slice**  
**after the peak**

Lenoir et al. (2007) – Strain, International Journal for Experimental Mechanics, Vol. 43, No. 3, 193–205

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## example 2

### localization in sandstone

### (shear bands and compaction bands)

investigating **a range of full-field methods** with different **sensitivities** to different physical properties, to characterize different aspects of the **mechanical processes**

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investigating **a range of full-field methods** with different **sensitivities** to different physical properties, to characterize different aspects of the **mechanical processes**:

- pre- and post-mortem x-ray tomography
- 3D Digital image analysis
- 3D Digital Image Correlation (DIC)
- ultrasonic tomography
- neutron tomography
- acoustic emissions
- thin section analysis (microscopy and SEM)

# specimens of Vosges sandstone – loaded in triaxial compression

## Vosges sandstone (see Bésuelle, 1999)

- ▣ Ve2 (50 MPa confining pressure):
  - shear bands
  
- ▣ Ve4/6 (130 MPa confining pressure):
  - compaction bands

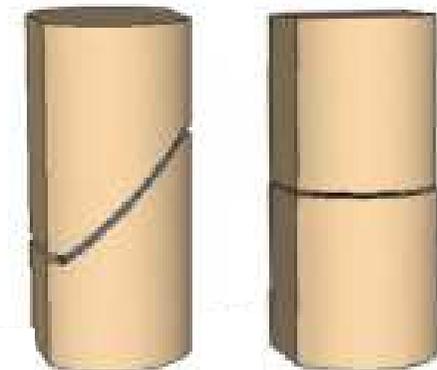
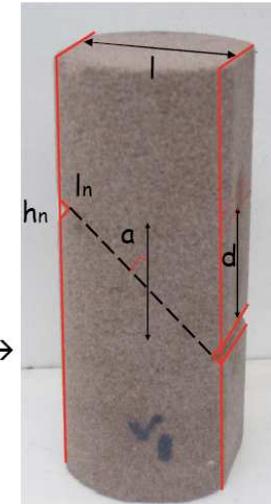
→ “flattened cylinders”

→ x-ray and ultrasonic scanning before and after tests

**Vosges sandstone**  
mean grain size = 0.3 mm

**Notches** → to enforce **distinct shear band** in the middle of the sample (expected)

**Flattened faces** → contact surfaces for the barrettes



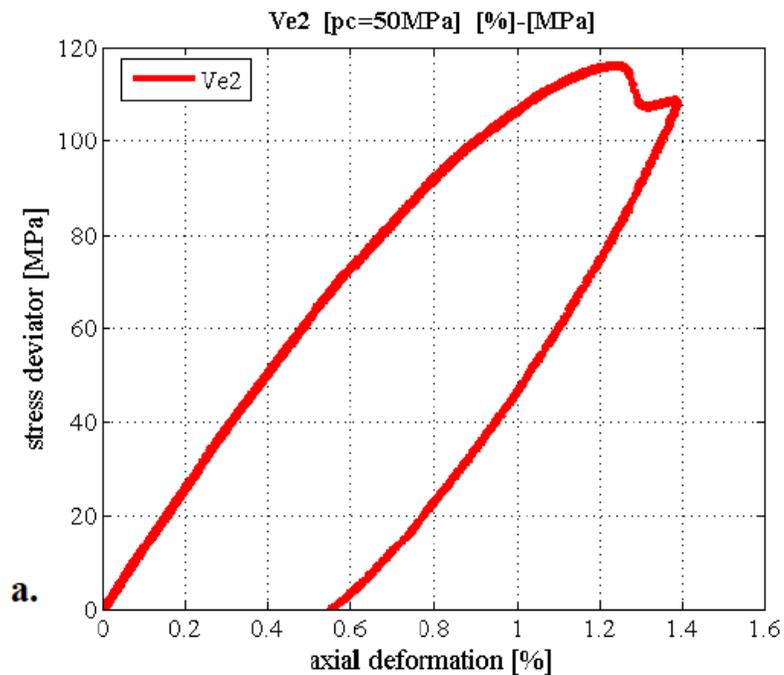
# specimens of Vosges sandstone – loaded in triaxial compression

## Vosges sandstone (see Bésuelle, 1999)

at GFZ, Potsdam

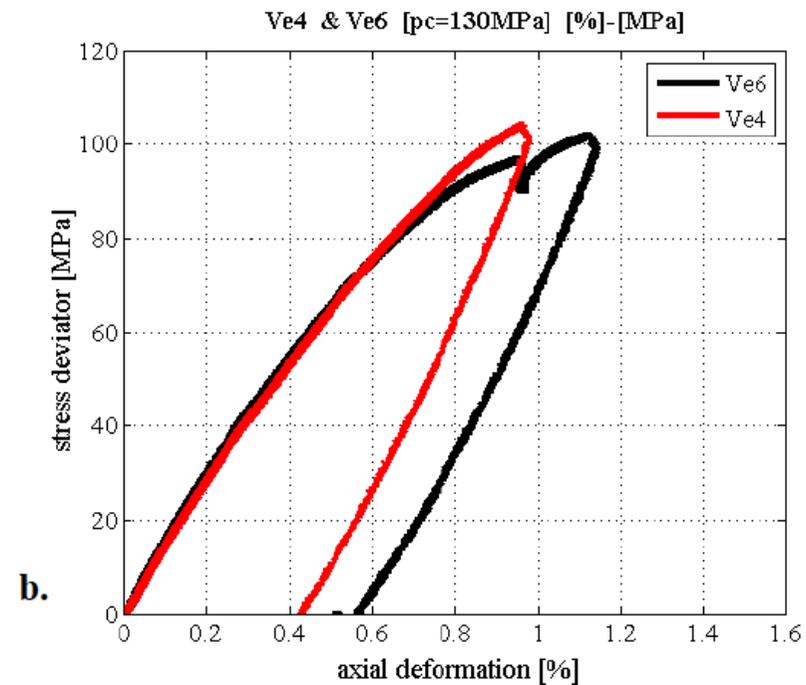
### ▣ Ve2 (50 MPa confining pressure)

- shear bands



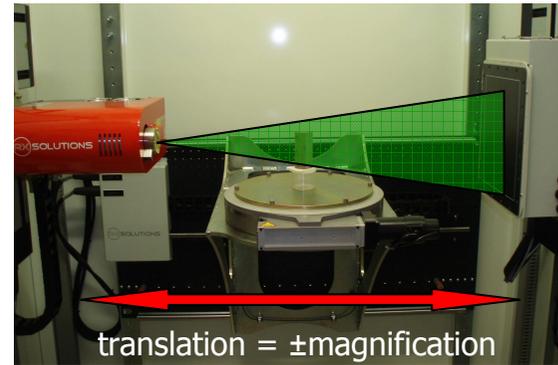
### ▣ Ve4/6 (130 MPa confining pressure)

- compaction bands



→ tests stopped shortly after peak stress not to break the specimen in two pieces

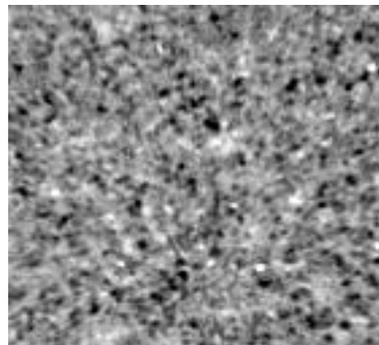
# x-ray scanning performed at 3S-R (not at ESRF)



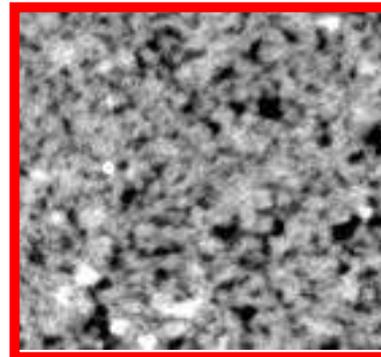
Cone Beam  
Variable magnification:  
ø4 mm  $\Rightarrow$   $\approx$  5  $\mu$ m voxel width  
ø210 mm  $\Rightarrow$   $\approx$  220  $\mu$ m voxel width  
Adaptability to access the physics of materials at the pertinent scale(s)

## Grès de Vosges (grain diameter $\approx$ 300 $\mu$ m)

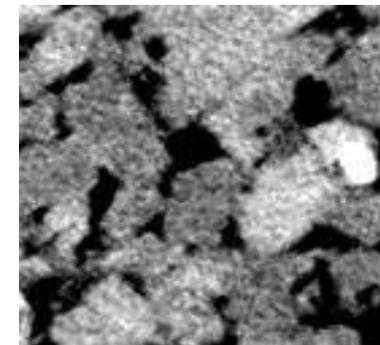
- Voxel width: 90  $\mu$ m



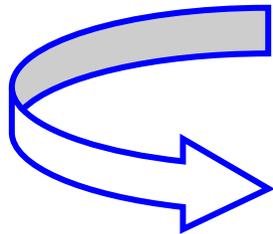
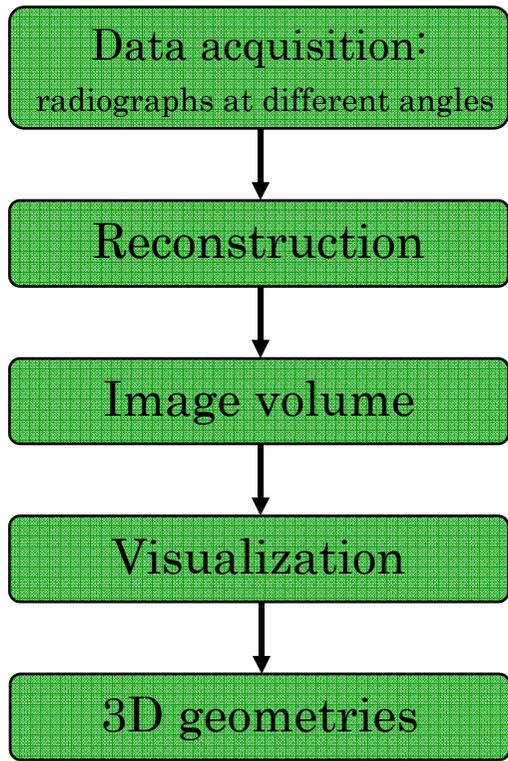
30  $\mu$ m



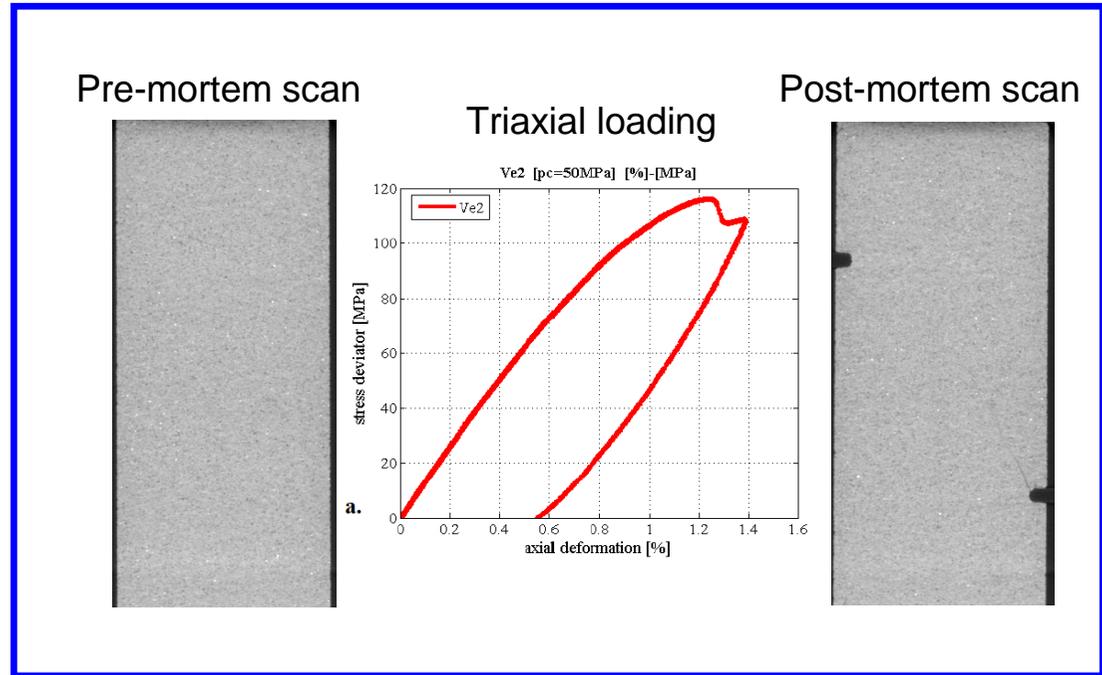
7  $\mu$ m



# X-ray tomography at 3S-R



(Image voxel size  $\approx 30\mu\text{m}$ )



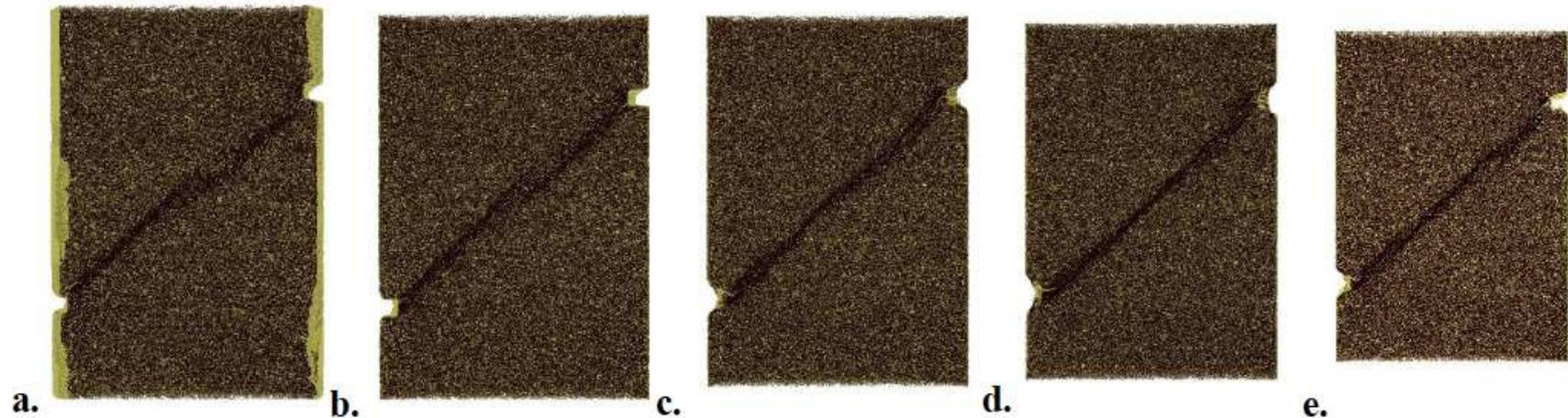
raw data (CT number)  
- density information



standard deviation  
- heterogeneity

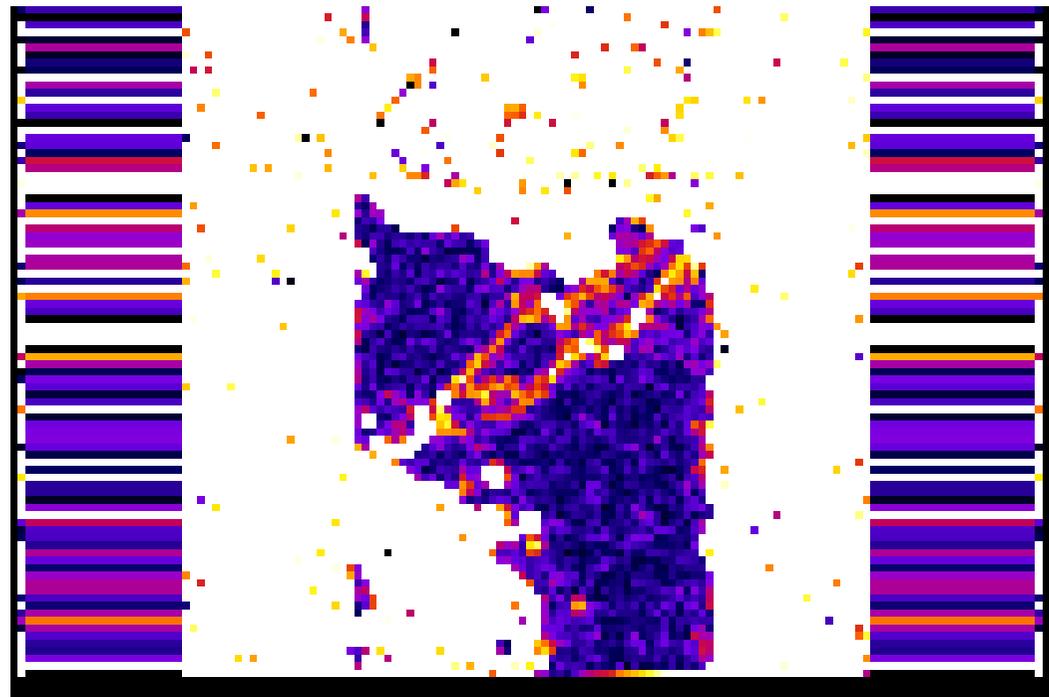
**specimen VE2** (50 MPa confining stress)

high resolution scans  $\sim 30 \mu\text{m}$  voxel size



- Localised deformation appears as higher density zones (dark = higher density)
- Two bands meeting in middle of sample

**specimen VE2 (50 MPa confining stress)**



Maximum shear strain



zero

high

DIC grid spacing = 10 voxels

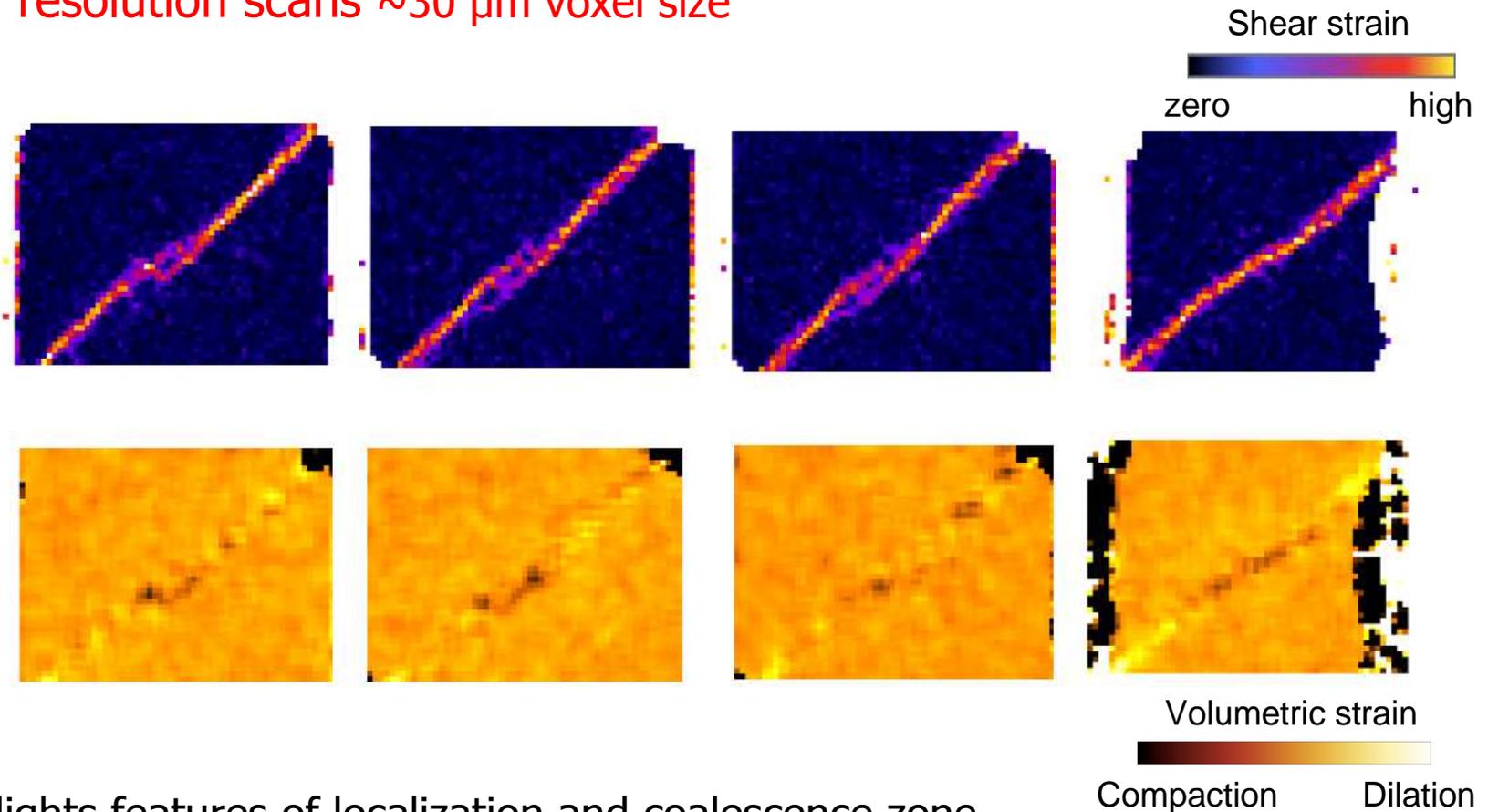
Correlation window = 5 voxels

(voxel side = 30  $\mu\text{m}$ )

## 3D DIC results (using in-house 3SR code *Tomowarp*)

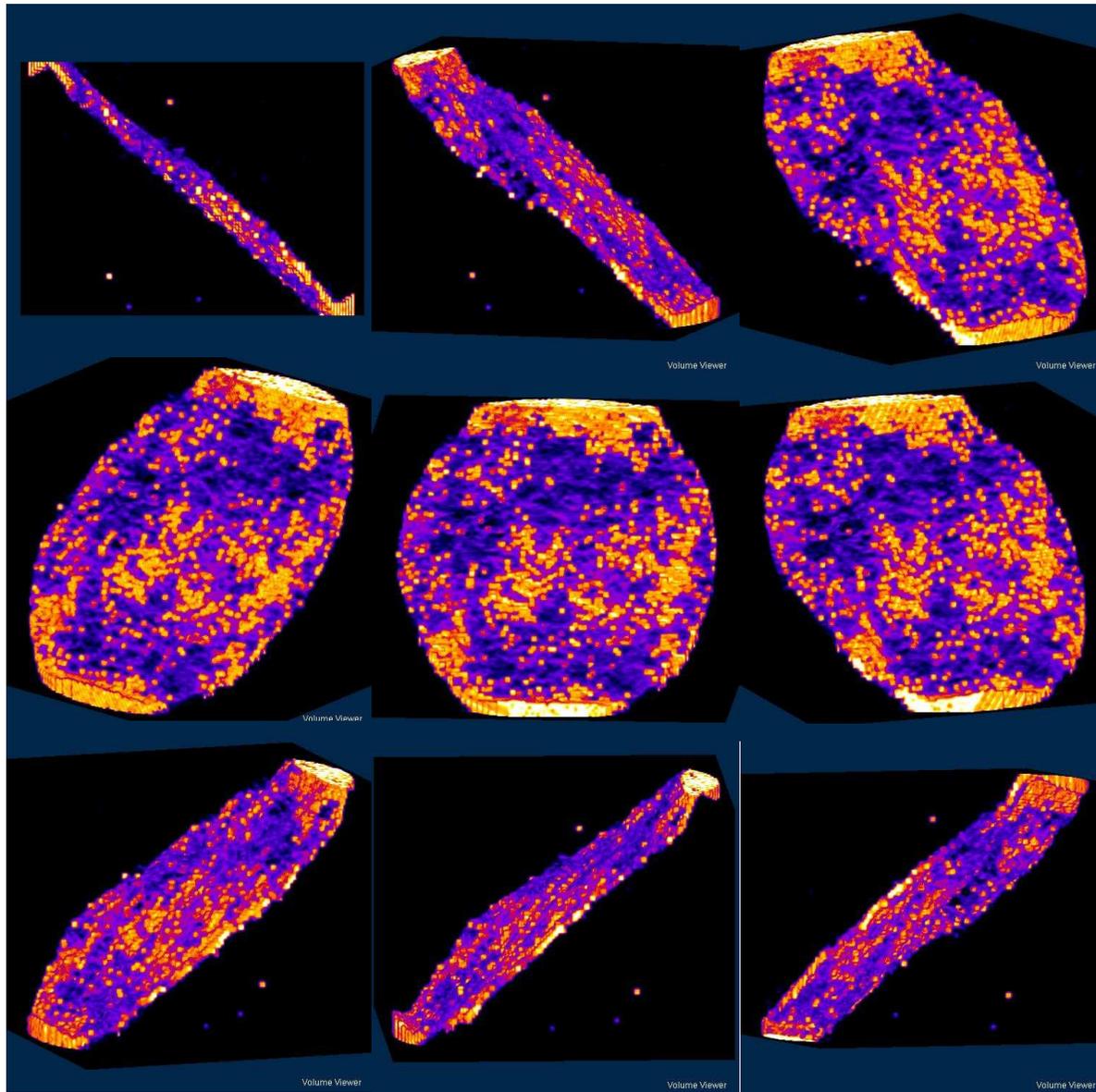
**specimen VE2** (50 MPa confining stress)

high resolution scans  $\sim 30 \mu\text{m}$  voxel size



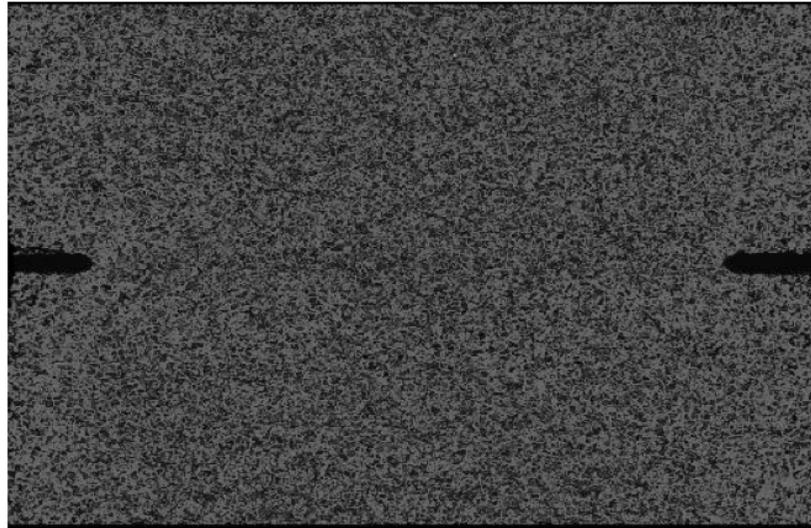
- highlights features of localization and coalescence zone
  - greater shear strain than volumetric
  - volumetric strain varies between compression and dilation

# 3D DIC results (same test, 3D views of the shear band)

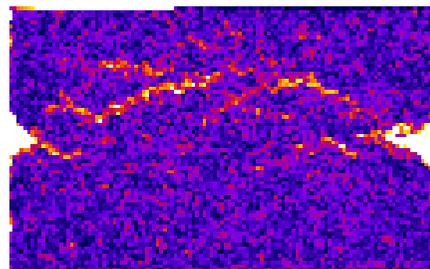


# x-ray tomography images + results of 3D DIC

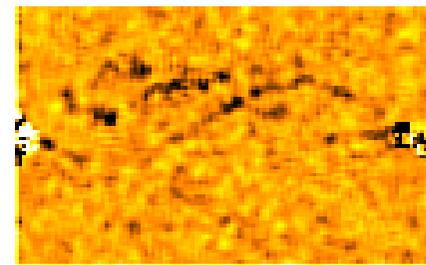
## specimen VE6 (130 MPa confining stress)



- no evidence (to the naked eye) of localized deformation



Maximum shear strain



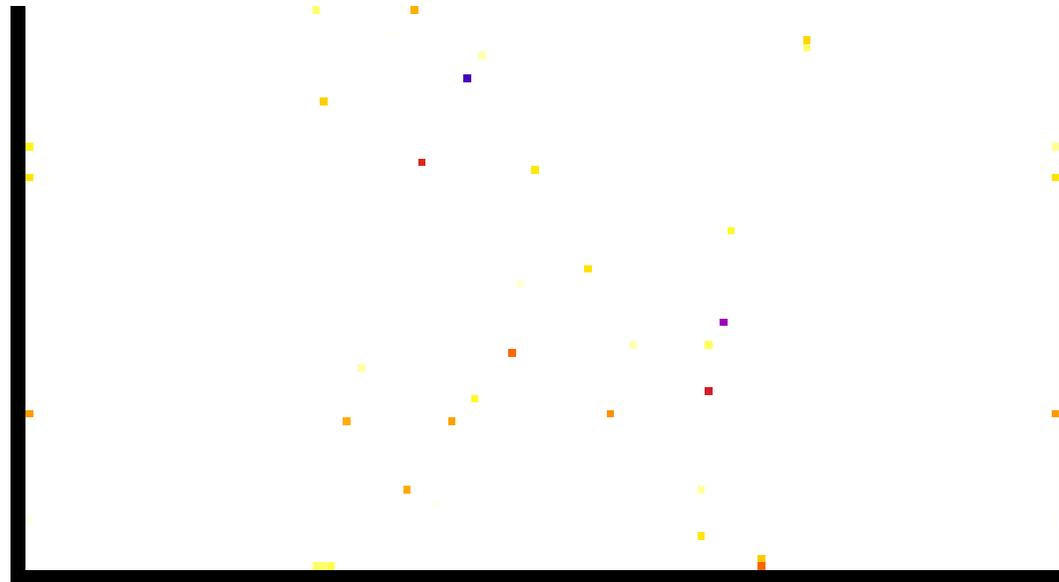
Volumetric strain



DIC grid spacing = 10 voxels, correlation window = 5 voxels

**specimen VE6 (130 MPa confining stress)**

- DIC results clearly show localized deformation



Maximum shear strain



zero

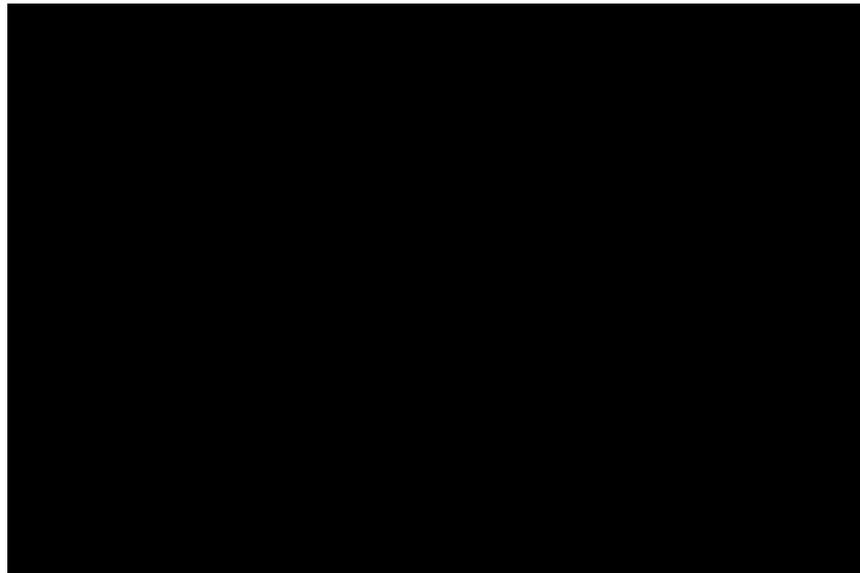
high

DIC grid spacing = 10 voxels, correlation window = 5 voxels

# StdDev maps

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**VE2 (50 MPa) / ~30  $\mu\text{m}$  voxel size**

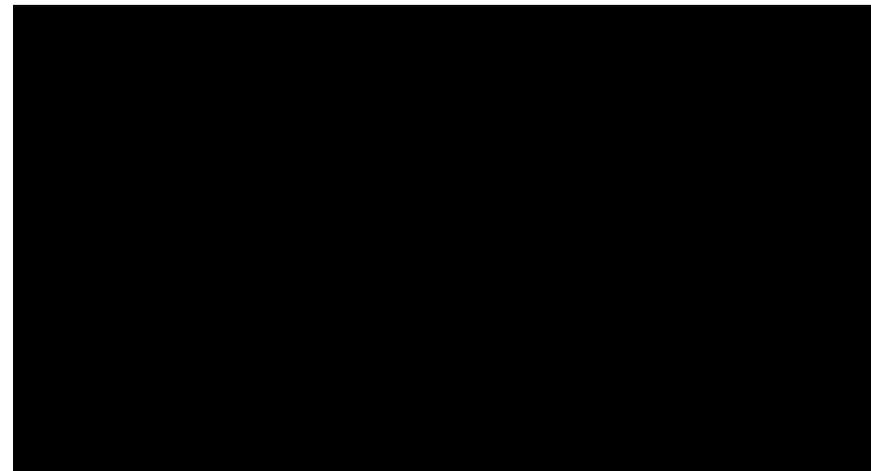


when direct observation of x-ray tomography images does not allow compaction band features to be resolved, local statistical measures of the gray-level values such as skewness and standard deviation may help (Louis et al. 2006)



calculation made throughout the image volume over sub-volumes of  $20 \times 20 \times 20$  voxels<sup>3</sup> at a spacing of 5 voxels in each direction

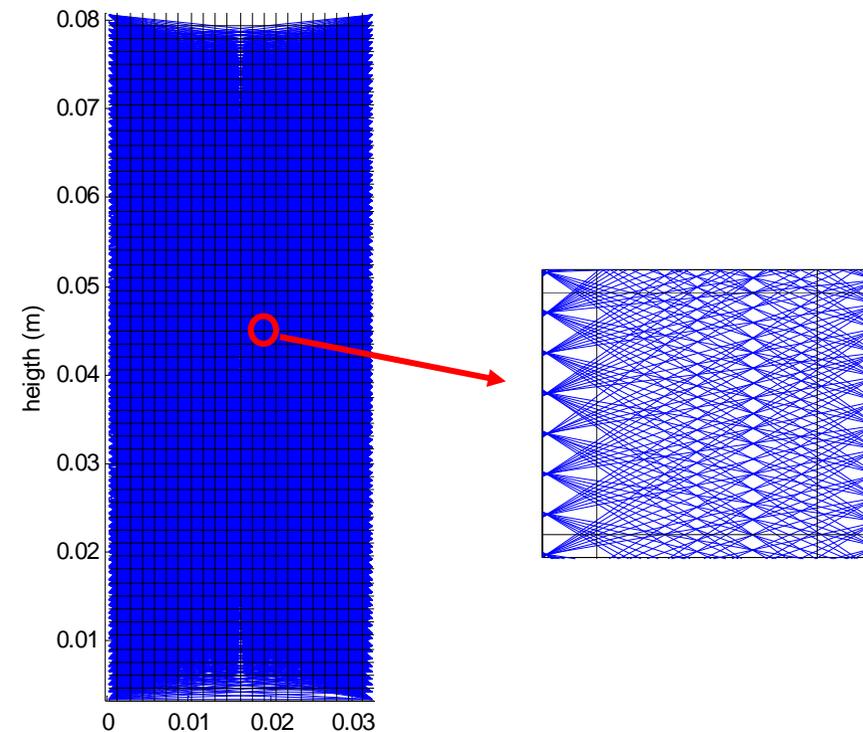
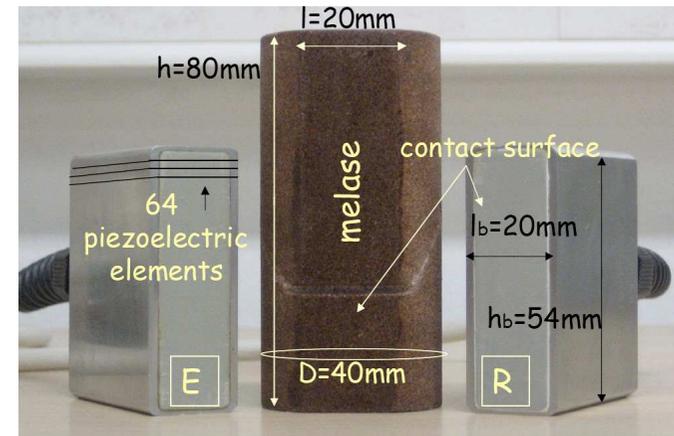
shear and compaction bands appear as zones of decreased standard deviation



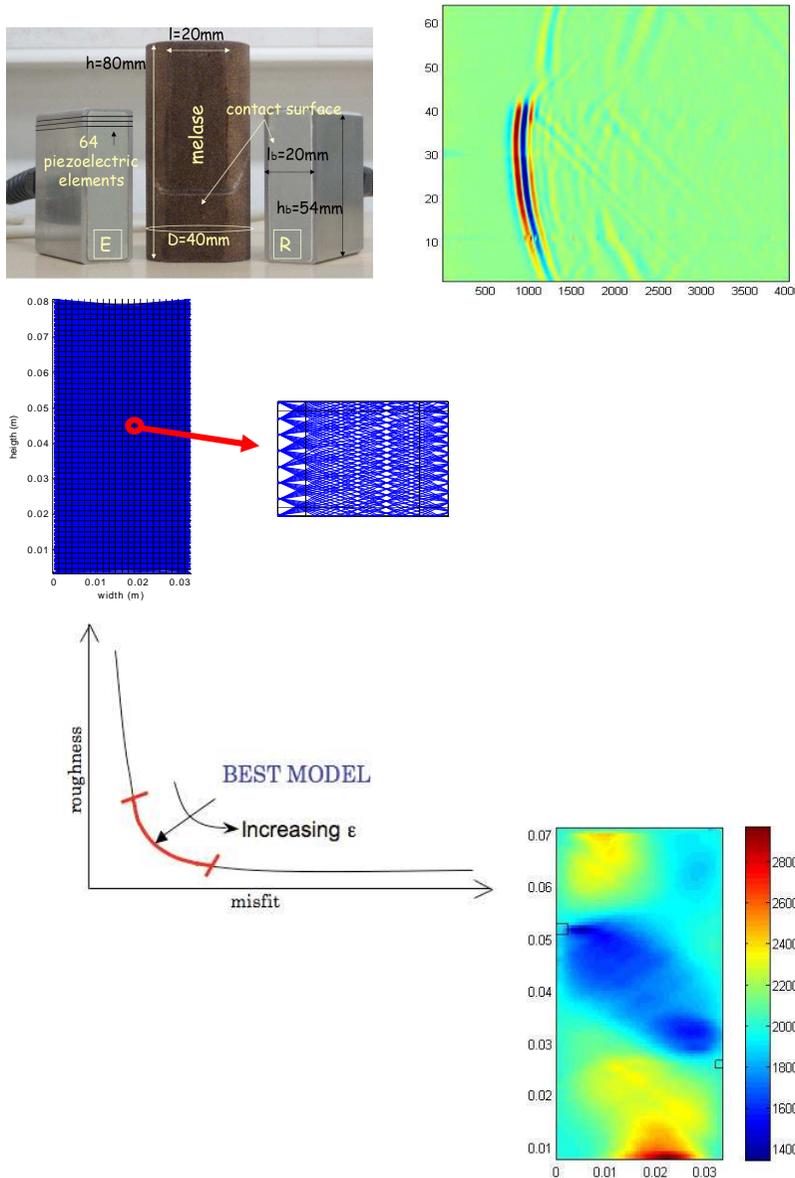
**VE6 (130 MPa) / ~30  $\mu\text{m}$  voxel size**

# ultrasonic tomography – data acquisition

- Ultrasonic data acquisition:
  - two arrays of **64 piezoelectric transducer elements** (Vermon)
    - elements size: about 20 x 0.75 mm
    - main frequency : 1 MHz
  - **64 source/receiver channel recording system** (Lecoeur Electroniques)
    - LGIT, Grenoble
- Data acquired over 64x64 intersecting raypaths in a few seconds
  - unprecedented (for geomaterials) spatial coverage



# ultrasonic tomography – method: discretization



Pick travel-times

↓

Discretise model space (grid)

↓

$$t_i = \sum_j l_j p_j$$

↓

$$d_i = (t_1, t_2, t_3, \dots, t_N)$$

**d = Am**     $A_{ij} = \{l_1, l_2, l_3, \dots, l_N\}_i$

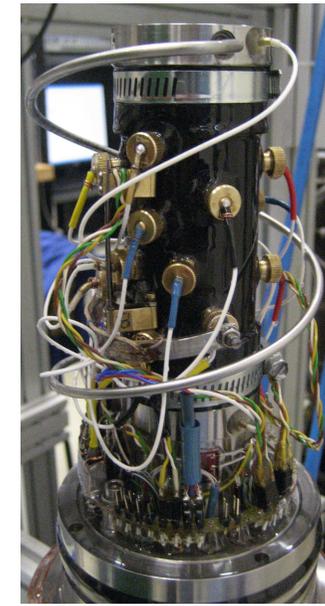
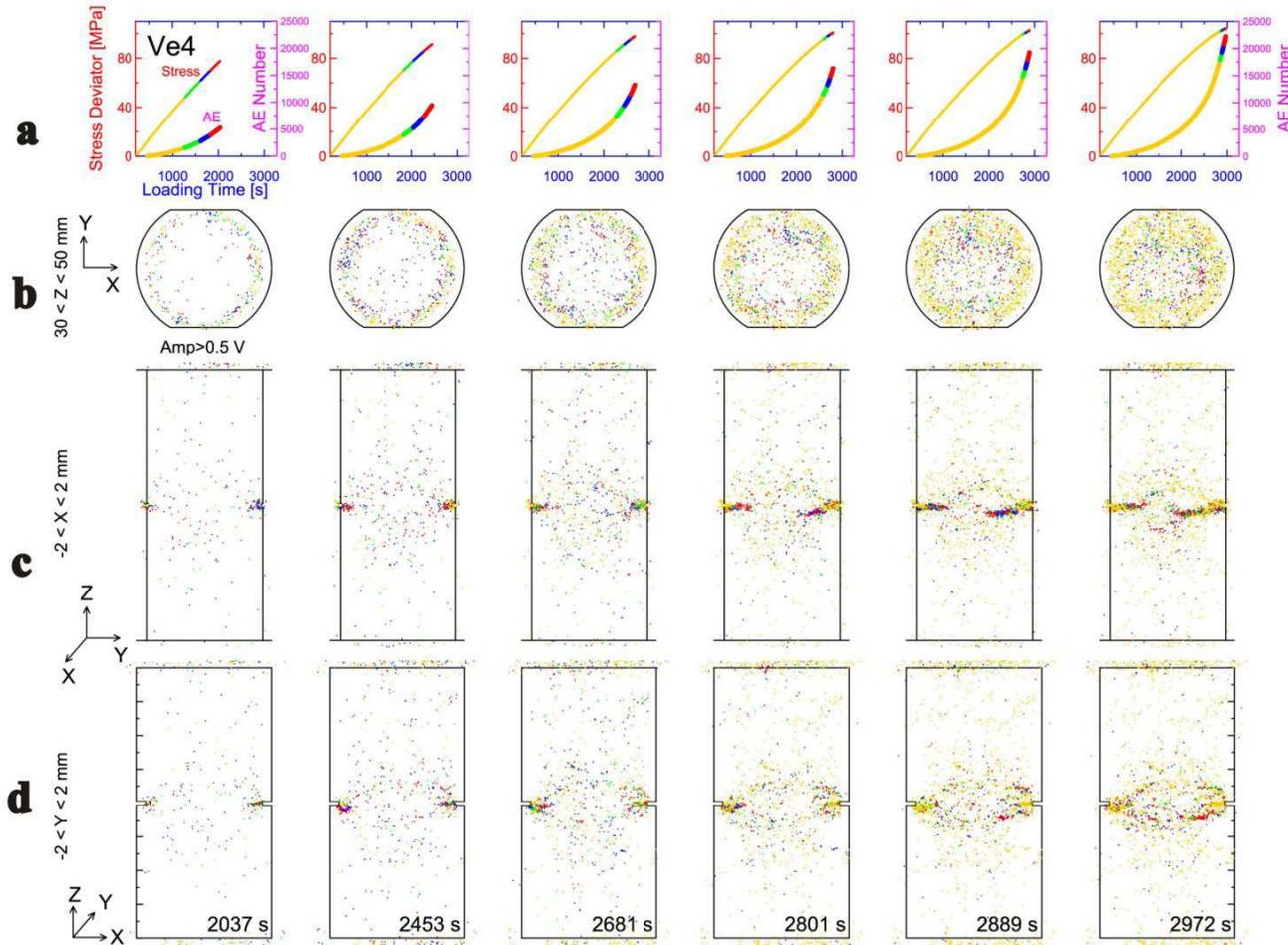
$$m_j = (p_1, p_2, p_3, \dots, p_M)^T$$

↓

**solve  $m = (A^T A)^{-1} A^T d$**   
(with constraints)

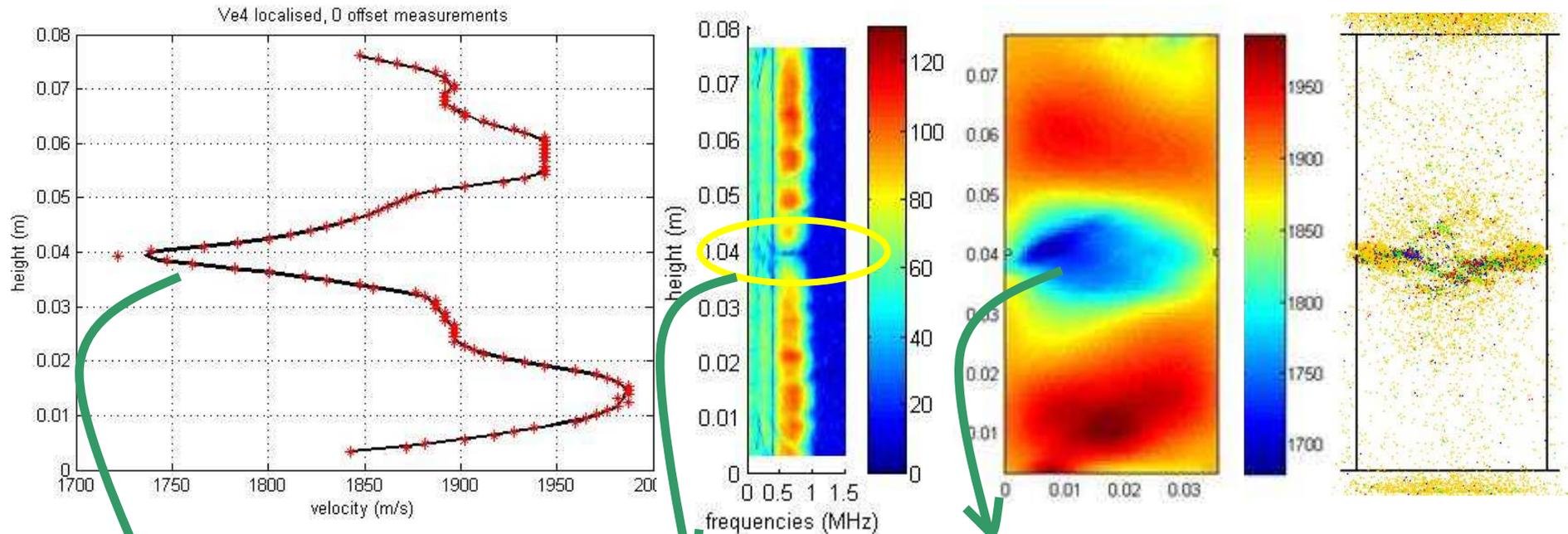
$t_i$  = travel time of *i*th ray  
 $l_j$  = path length of *i*th ray in *j*th cell  
 $p_i$  = slowness = velocity<sup>-1</sup> in *j*th cell

**specimen VE4 (130 MPa confining stress)**



# combining ultrasonic tomography and acoustic emissions

## specimen VE4 (130 MPa confining stress)



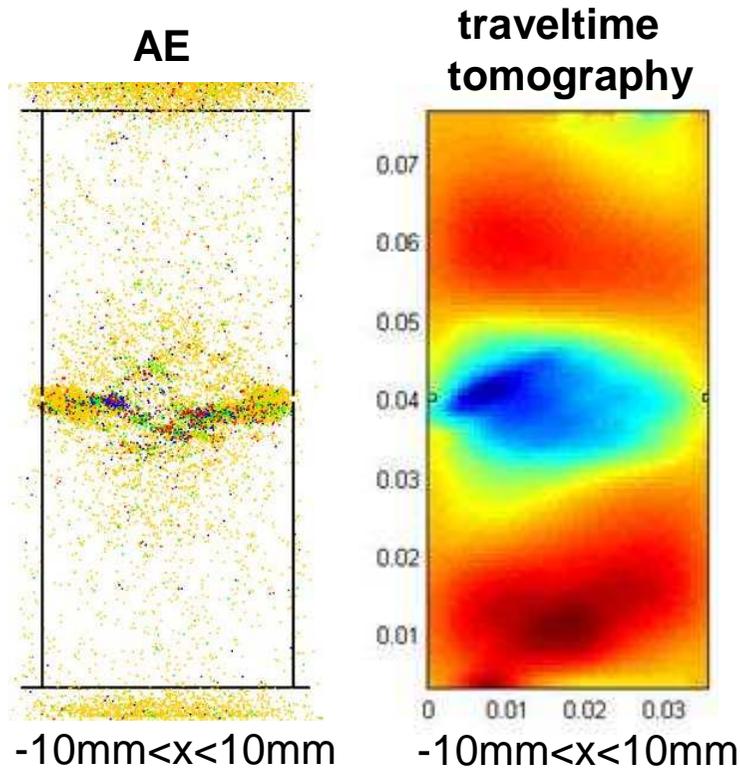
**drop in velocities  
→ cracking, damage**

**~ 70%  
amplitude  
reductions**

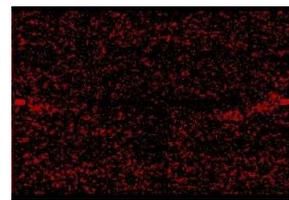
**CB  
low velocity zone  
but resolution?**

# consistency of results from different techniques

## specimen VE4 (130 MPa)

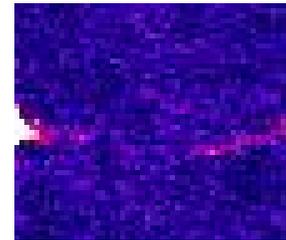


high resolution  
X-ray scans  
( $\sim 30 \mu\text{m}$ )

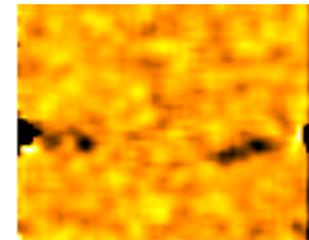


$y = 18.79 \text{ mm}$

Max shear  
strains



Volumetric  
strains



small density variations,  
homogeneous regions in the band  
compaction and localized shear in the band

acoustic emissions,  
reduced velocities,  
→ damage mechanisms

from specimen to grain scale



**thin sections**

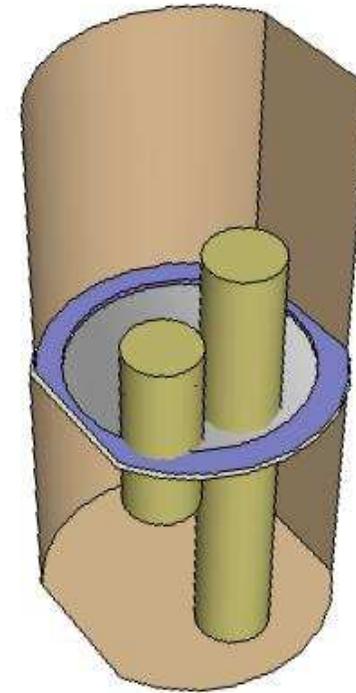
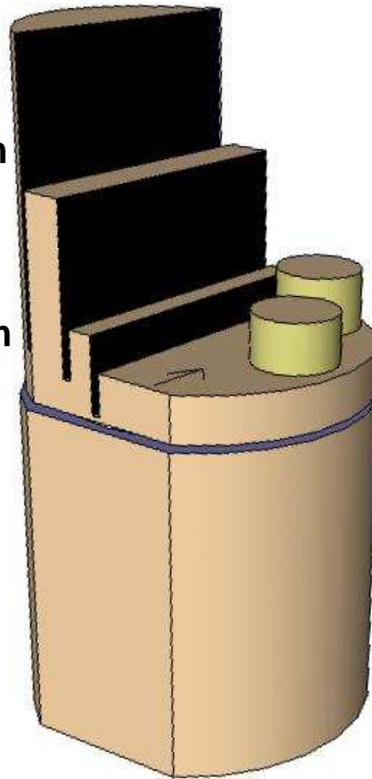


optical & electron  
microscope

**epoxy**

$y = 9.4 \text{ mm}$

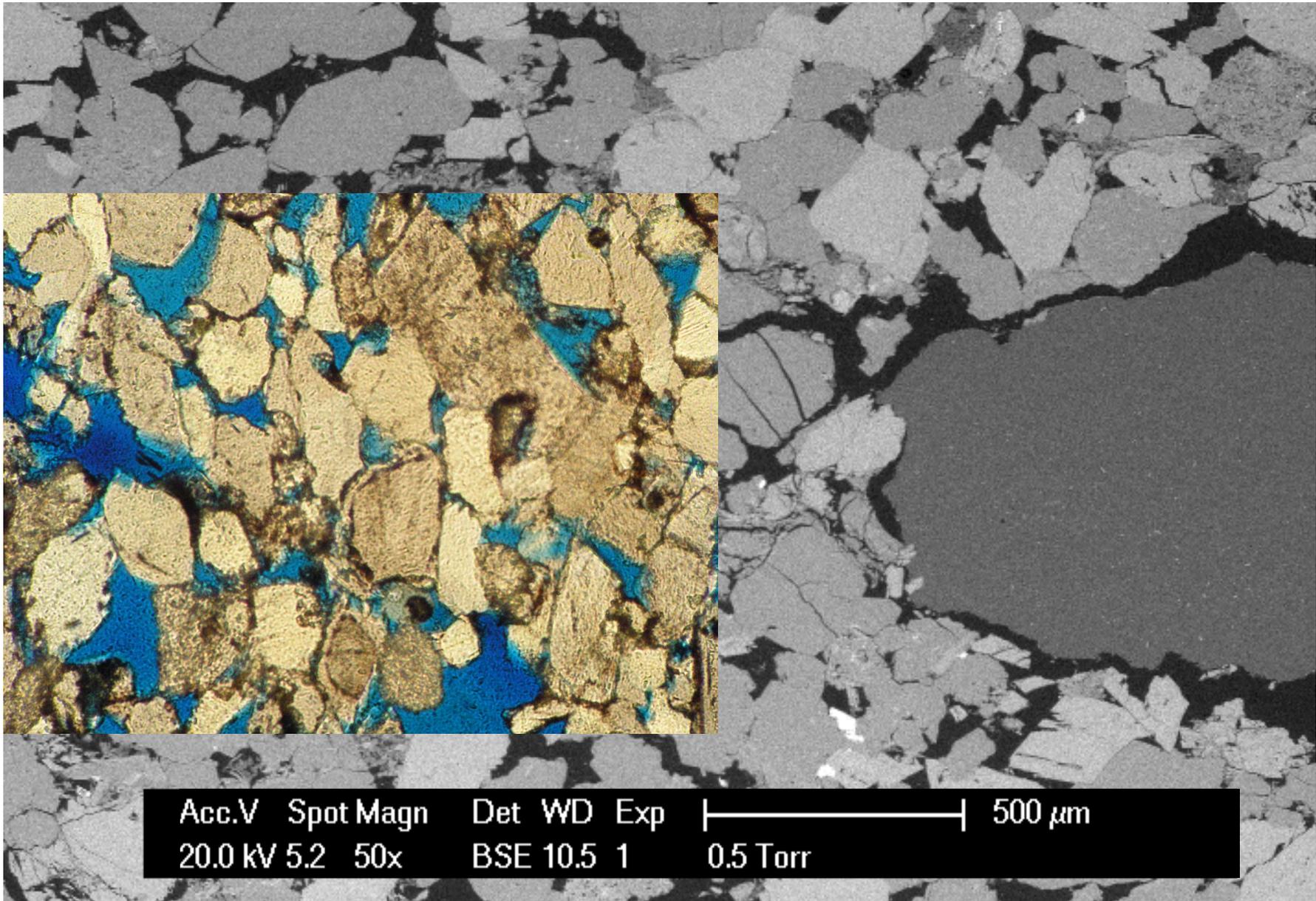
$y = 14.65 \text{ mm}$



**small cores (D=10mm)**



very high resolution  
x-ray images  $\sim 7 \mu\text{m}$



the key idea: combining different methods!

- **Full-field methods essential in the study of localization**
  - capture heterogeneity of the processes
  - allow measurement of dimensions e.g., localization widths
- **X-ray tomography provides insight into 3D density distributions**
  - high spatial resolution - Geometrical features and dimensions
  - low sensitivity to damage (only sees larger density changes)
- **3D-DIC**
  - clearer view of localization structures
  - quantification of strain and decomposition into shear and volumetric (compaction or dilation) components
- **Ultrasonic tomography**
  - damage mapping (full-field measurement of elastic properties)
- **Next steps - in-situ experiments**
  - during-loading x-ray tomography
  - plane strain apparatus for rocks
  - neutron tomography