

Geostatistical study of the linear Fracture Frequency (FF) in two Chilean copper deposits

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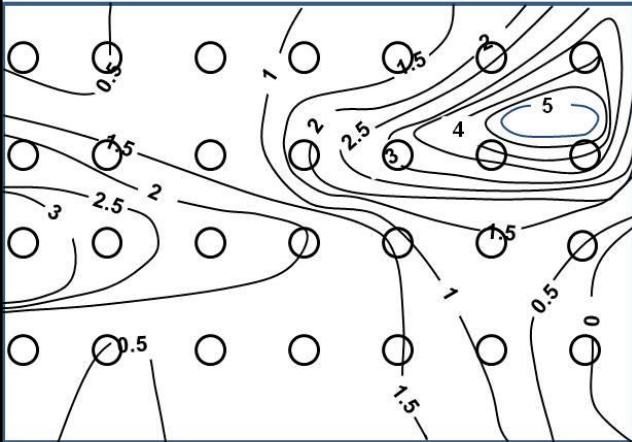
Cristian Guajardo, Codelco, Chuquicamata, Chile

Ramon Freire, Codelco, Casa Matriz, Chile

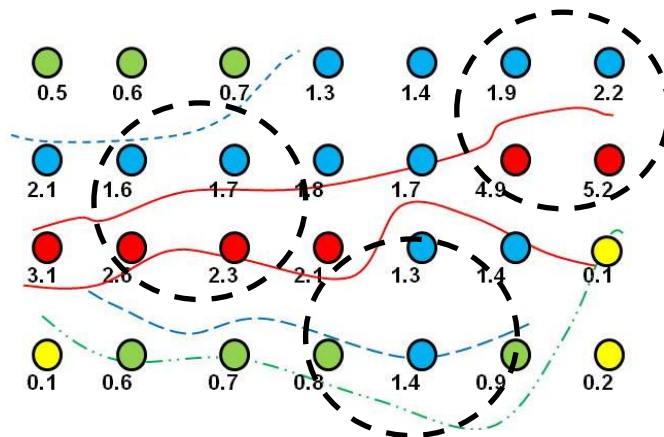
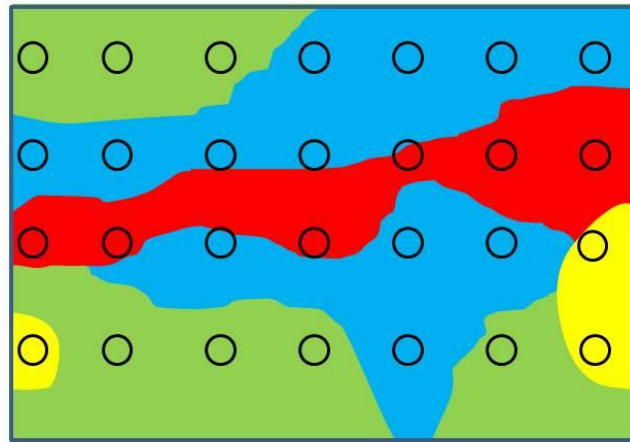


Geostatistics ?

Continuous
(grade)



Categorical
(geol. Unit)



Geostatistics



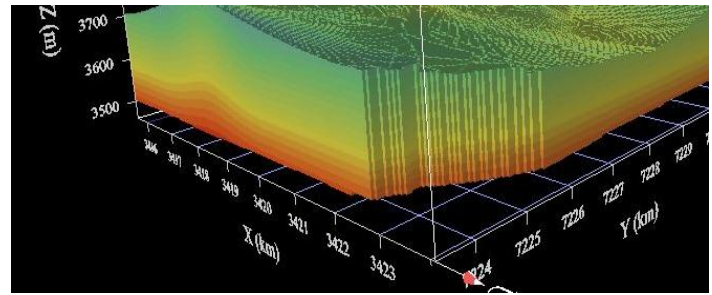
Spatial statistics



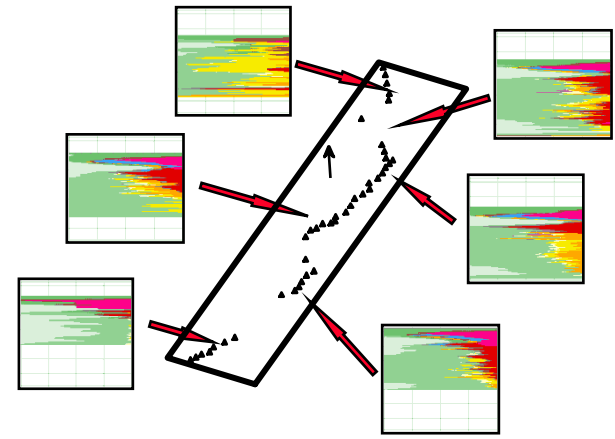
Modeling spatial
uncertainty

Geostat. ESTIMATION

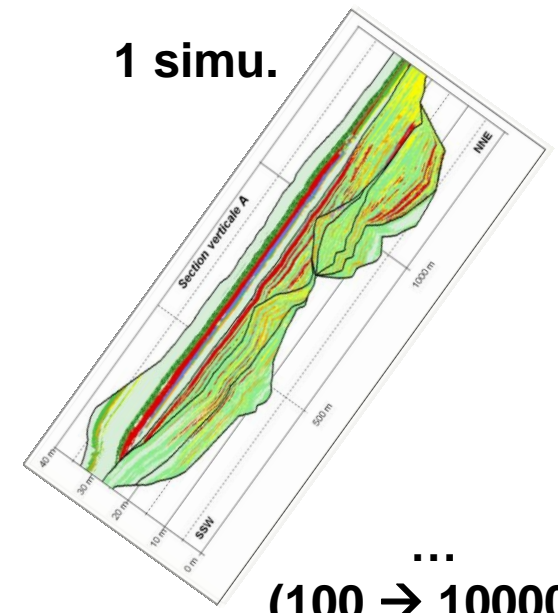
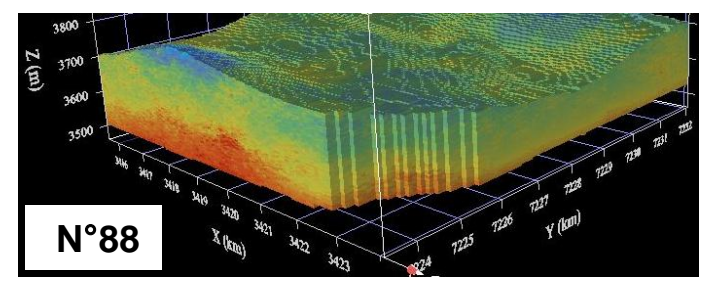
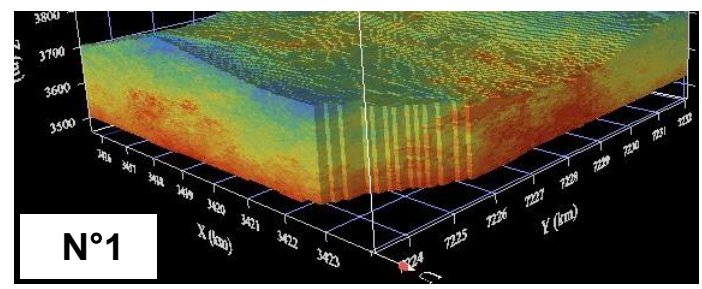
Continuous (grade)



Categorical (geol. Unit)



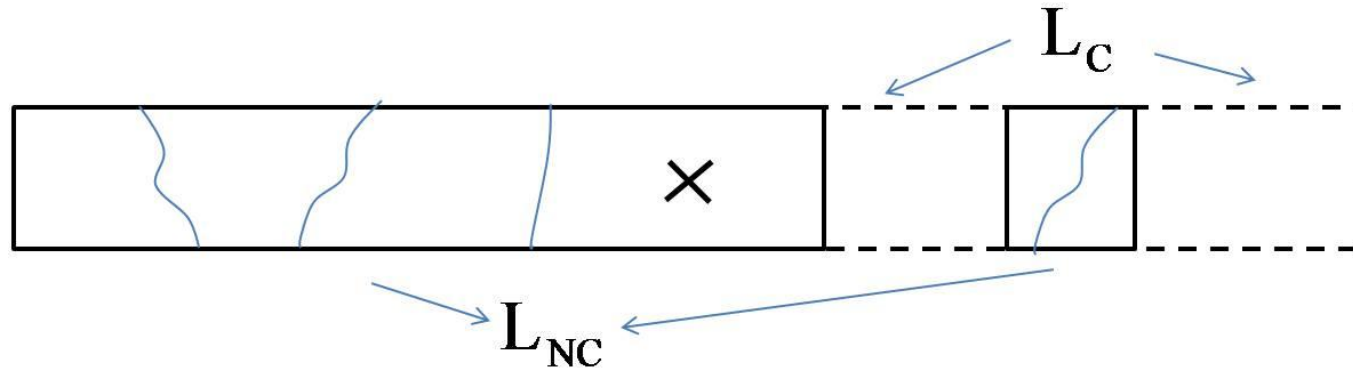
Geostat. SIMULATION



...
(100 → 10000)

| | Contin. V. | Categ. V. |
|--------|--------------|-----------|
| ESTIM. | X | |
| SIMU. | | |

Fracture Frequency



L_{NC} : total length of Non Crushed part of the sample

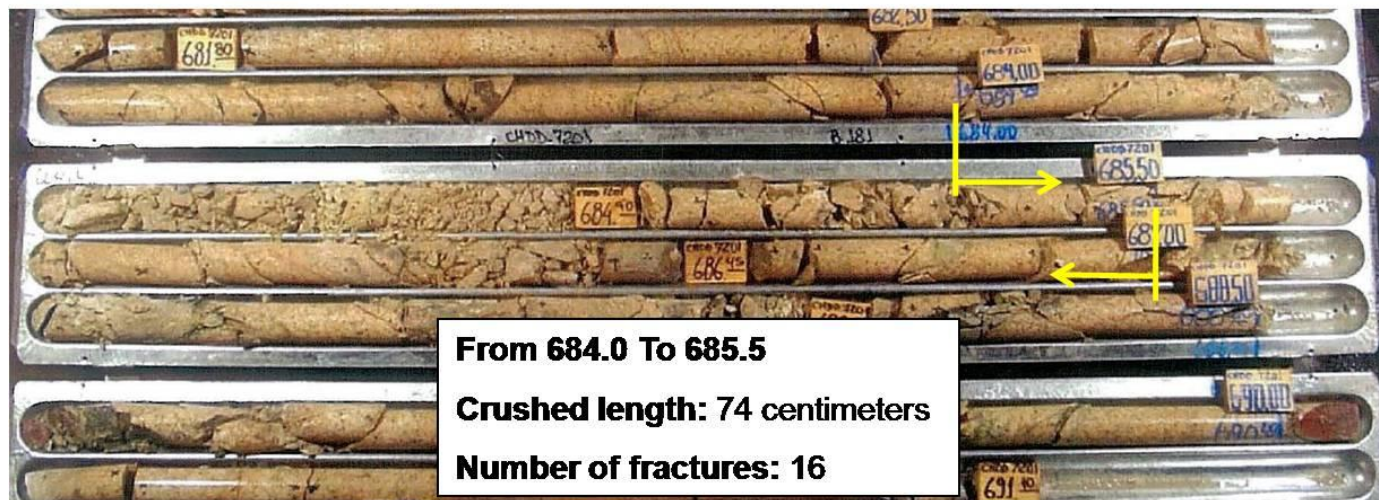
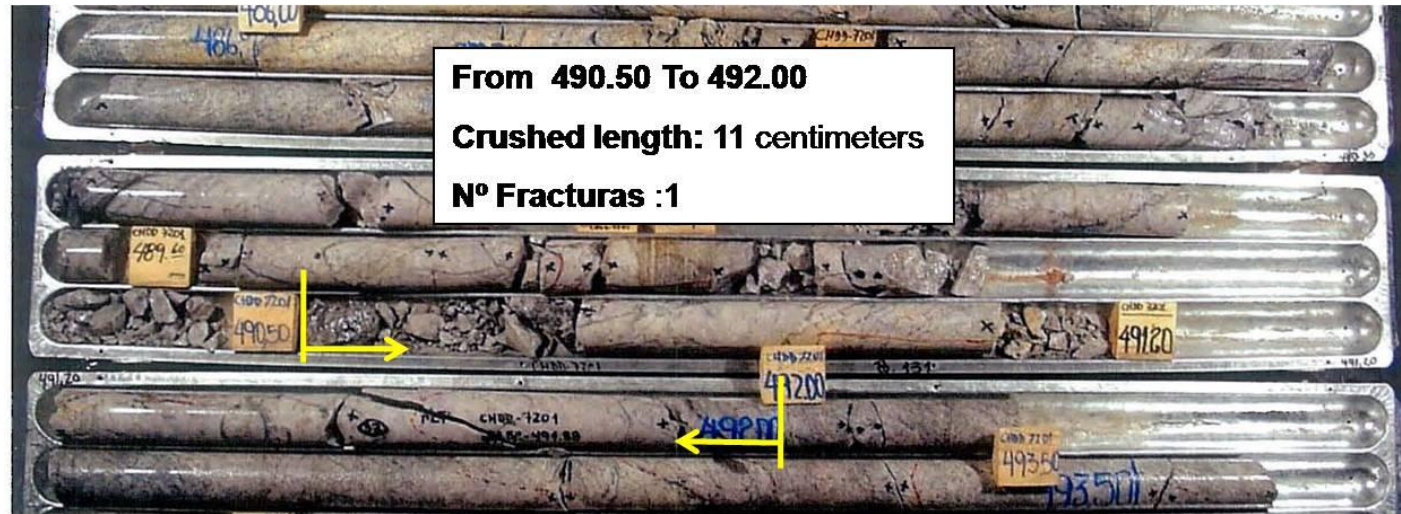
L_C : total length of Crushed part of the sample

$$L_{NC} + L_C = 1.5\text{m}$$

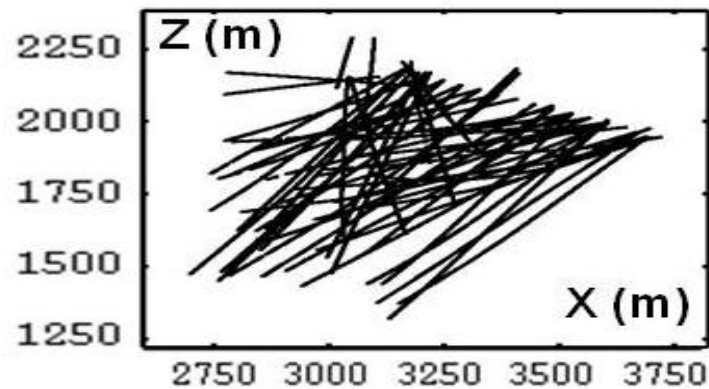
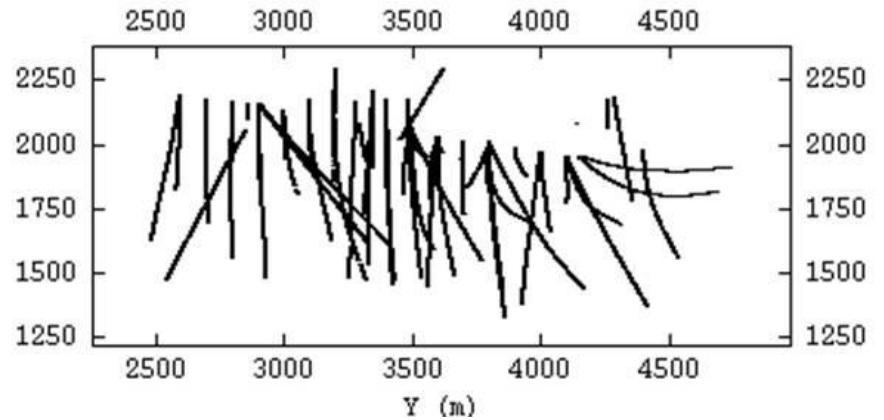
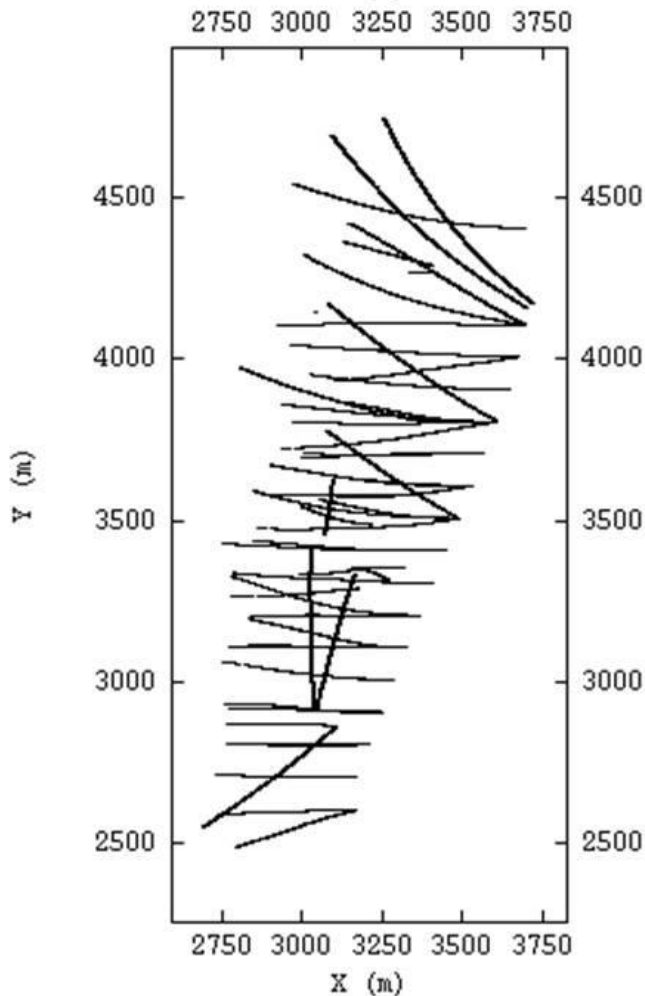
N_{fract} : number of fractures (corrected or not) along L_{NC}

$$FF(x) = \frac{N_{\text{fract}}(x)}{L_{NC}(x)}$$

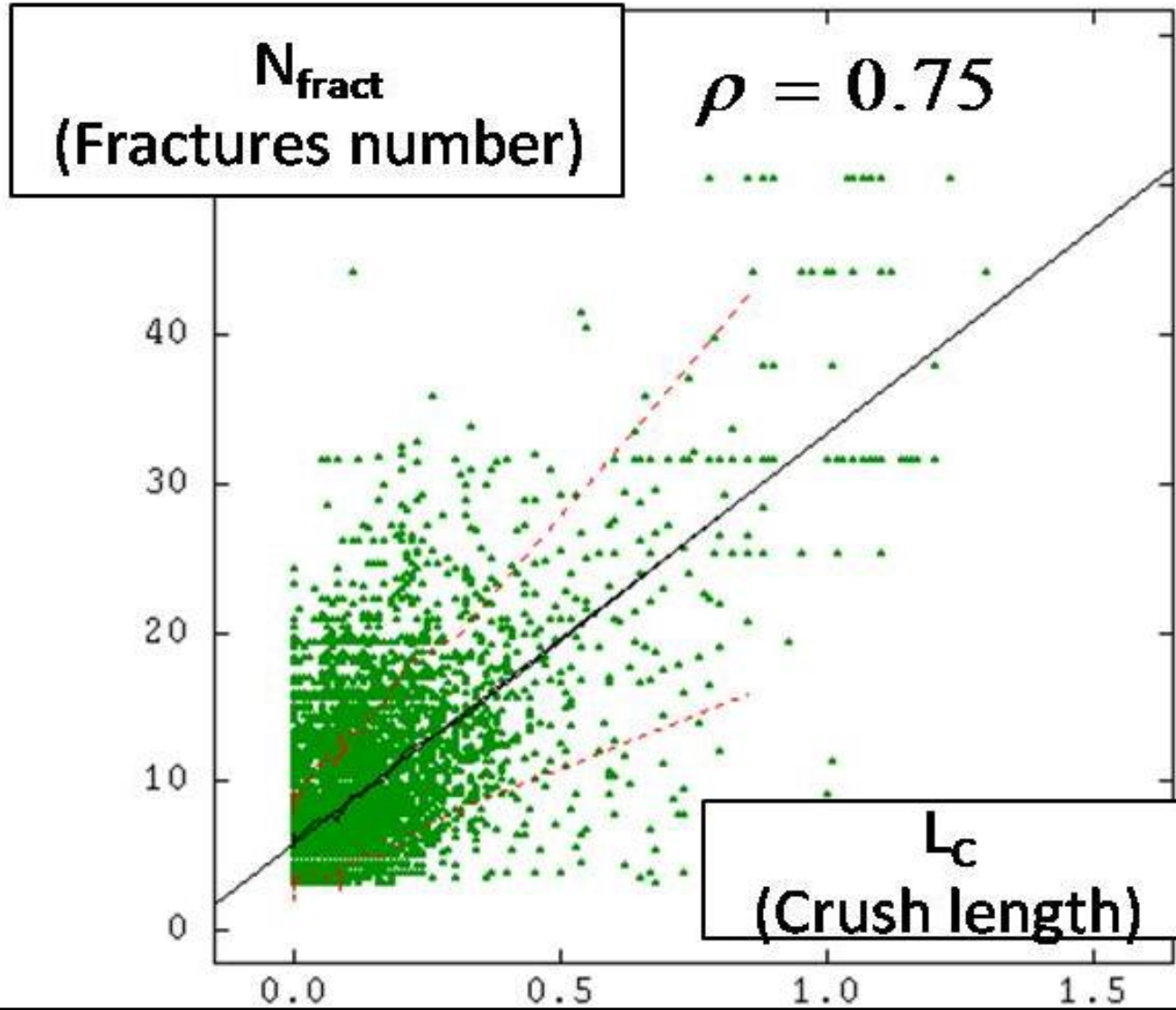
Observation of a natural phenomenon



- 13,000 samples
- 1,5 m length
- Underground mine, Codelco
- $1000 \times 2300 \times 1000 \text{ m}^3$

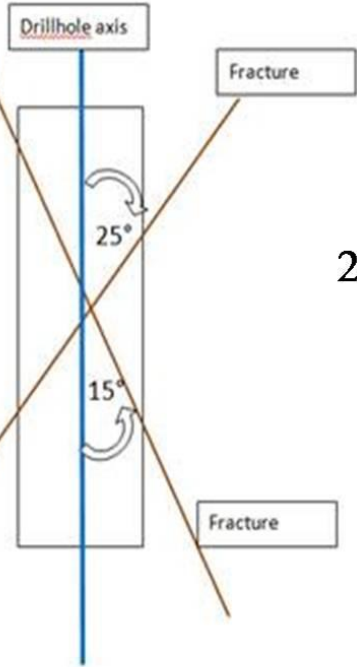


Understanding this link

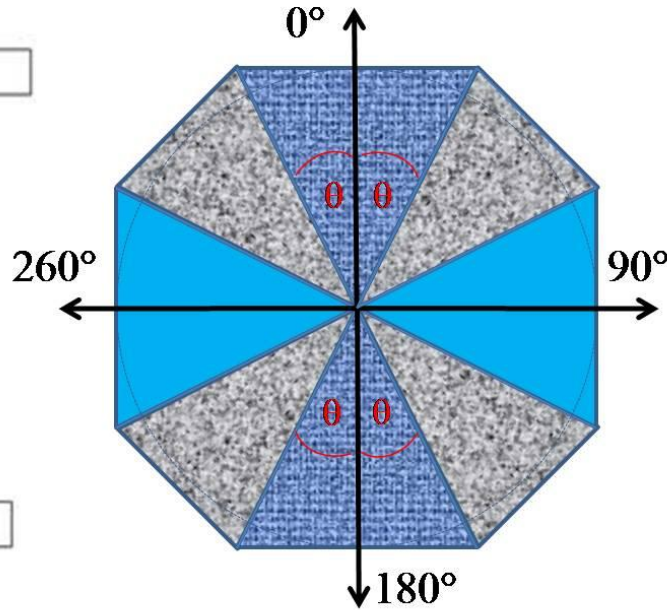


Directional Classes

(a)



(b)



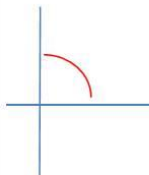
[0°, 30°] class



The angle
between two
fractures of
the class < 60°



[30°, 60°] class



The angle
between two
fractures of
the class < 90°



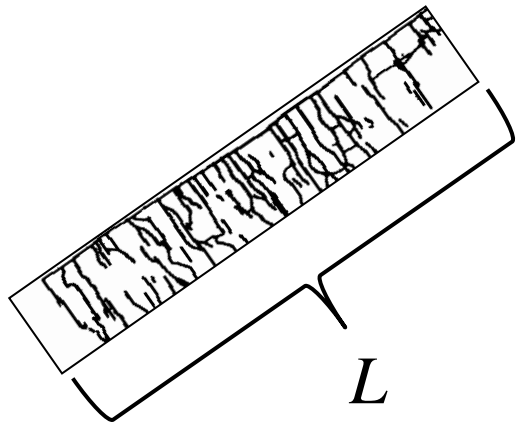
[60°, 90°] class



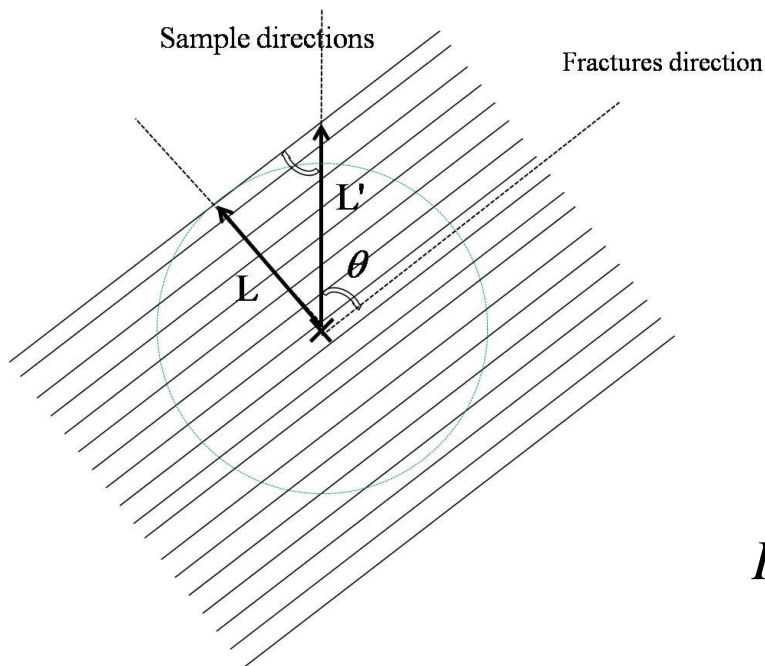
The angle
between two
fractures of
the class < 60°

$$N_{tot}(x) = \sum_{\theta=1}^{n_{\theta}} N(\theta, x)$$

Terzagui Correction



$$FF = \frac{\sum n(\theta)}{L}$$



$$FF_{corrected} = \frac{\sum \frac{n(\theta)}{\sin(\theta)}}{L}$$

(Terzaghi, 1965)

Directional Concentration

$$N_{tot}(x) = \sum_{\theta=1}^{n_{\theta}} N(\theta, x)$$

$$\sigma_{\theta}^2(x) = \text{Var}_{\theta}[N(\theta, x)] = E_{\theta}[(N(\theta, x) - N_{\theta,mean}(x))^2]$$

$$N_{\theta,mean}(x) \approx \frac{N_{tot}(x)}{n_{\theta}}$$

$$\sigma_{\theta}^2(x) \approx \frac{1}{n_{\theta}} \sum_{\theta=1}^{n_{\theta}} (N(\theta, x) - N_{\theta,mean}(x))^2$$

Directional Concentration

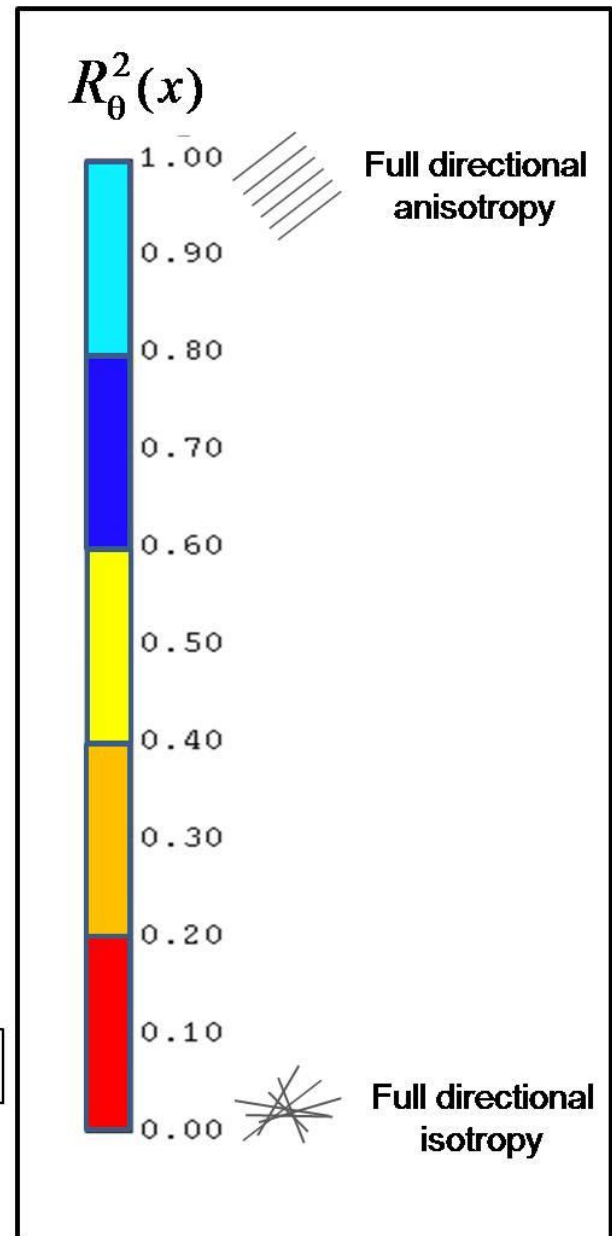
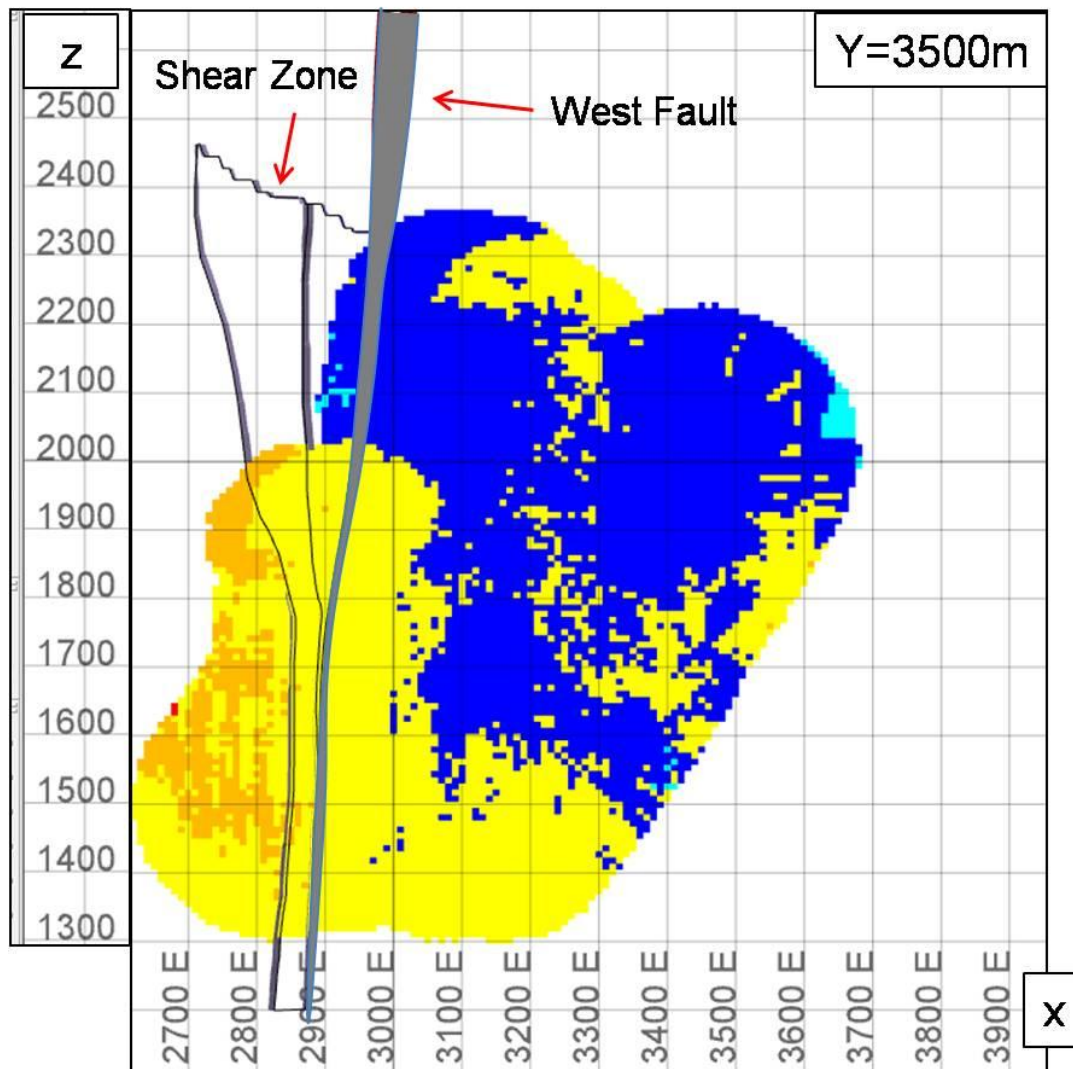
$$0 \leq \sigma_{\theta}^2(x) \leq \sigma_{\theta, \max}^2(x) = N_{\theta, \text{mean}}(x)^2 (n_{\theta} - 1)$$

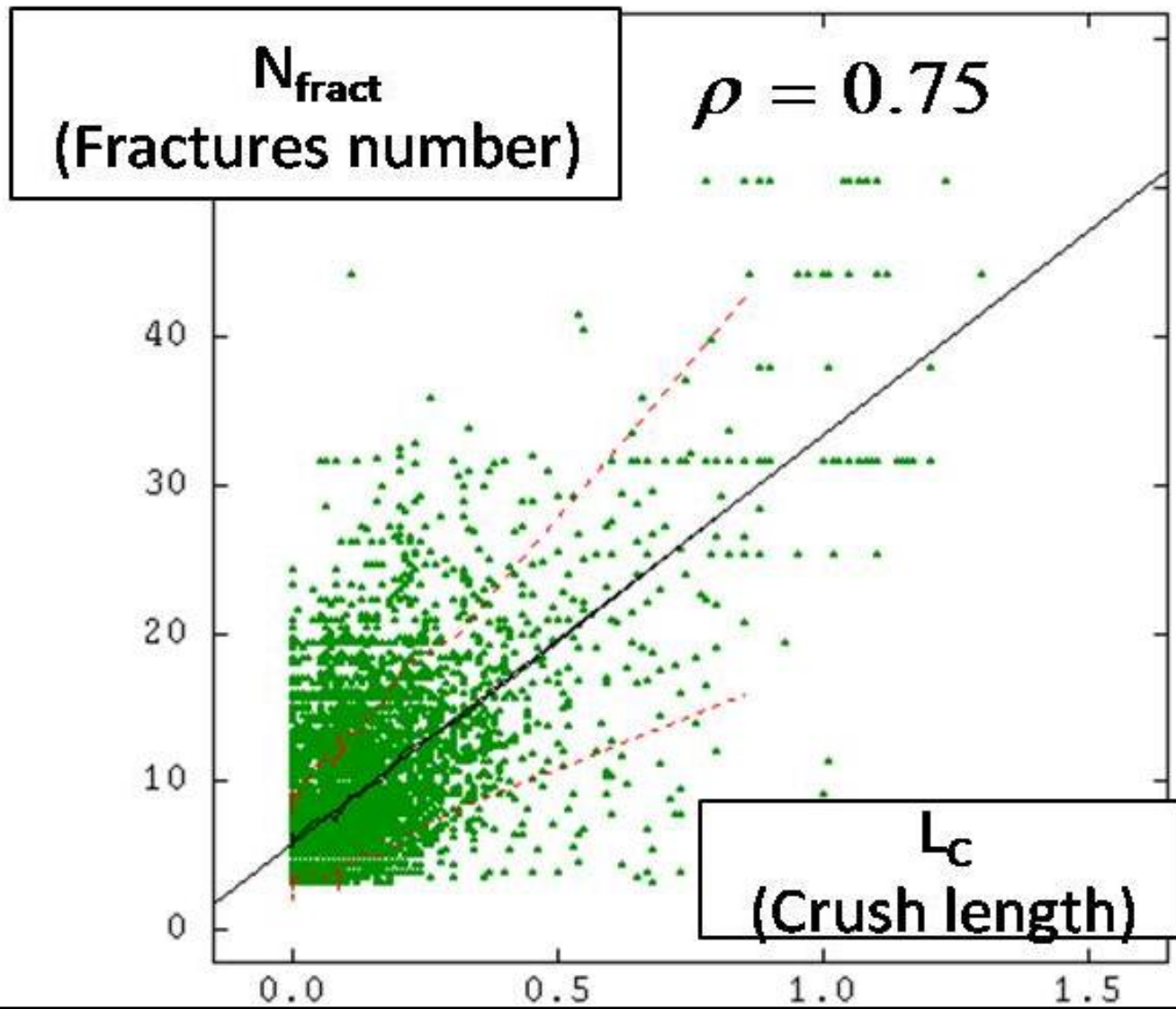
$\sigma_{\theta}^2(x) = 0$ full directional isotropy, all the fractures are equally distributed over the directions

$\sigma_{\theta}^2(x) = \sigma_{\theta, \max}^2$ full directional anisotropy, all the fractures lie along one direction

$$R_{\theta}^2(x) = \frac{\sigma_{\theta}^2(x)}{\sigma_{\theta, \max}^2(x)} = \frac{1}{n_{\theta}(n_{\theta} - 1)} \sum_{\theta=1}^{n_{\theta}} \left(\frac{N(\theta, x)}{N_{\theta, \text{mean}}(x)} - 1 \right)^2$$

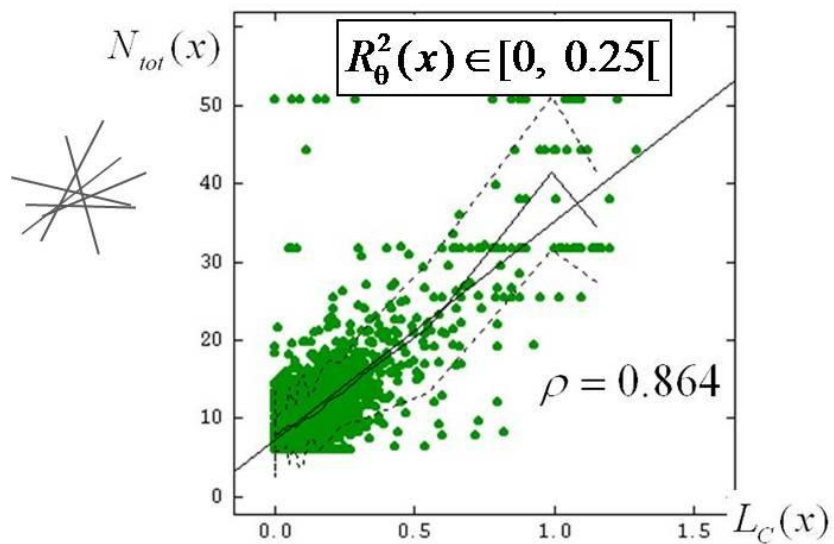
Directional Concentration



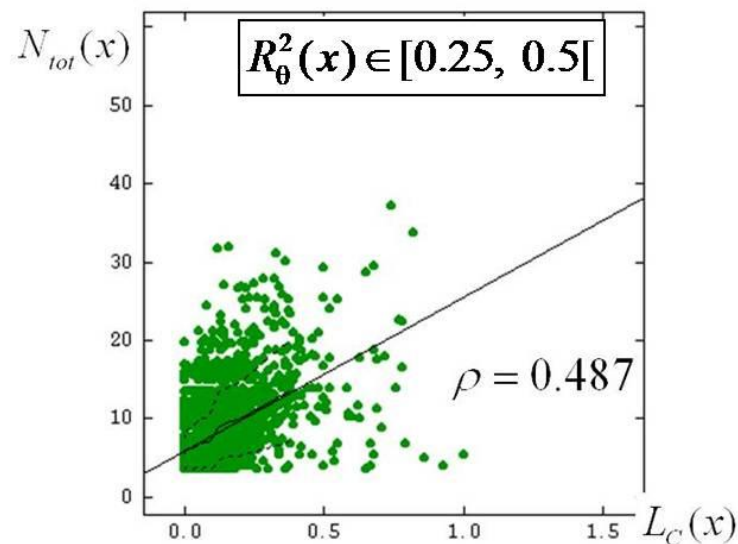


Directional Concentration Classes

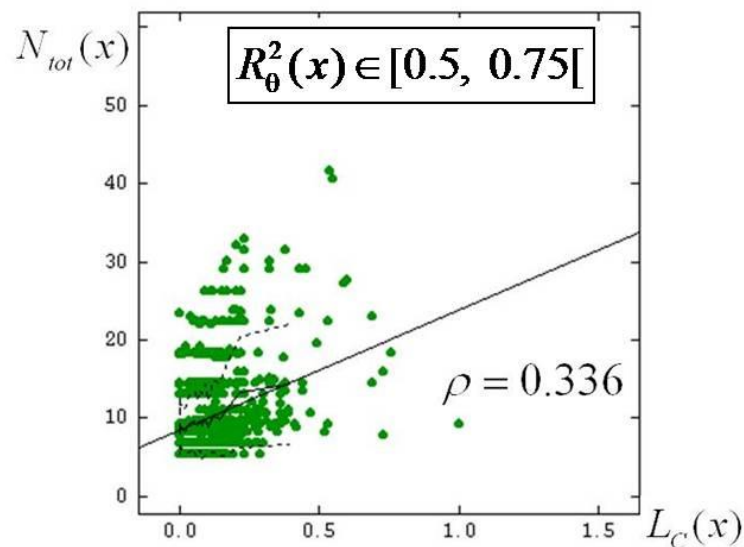
(a)



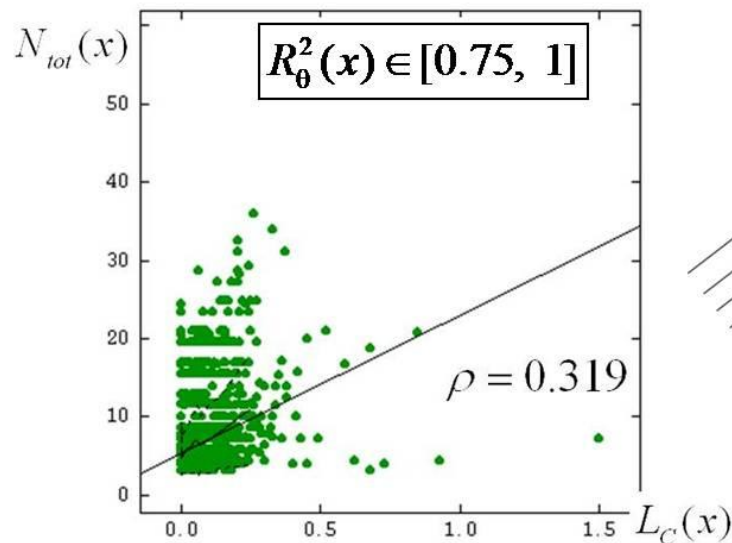
(b)



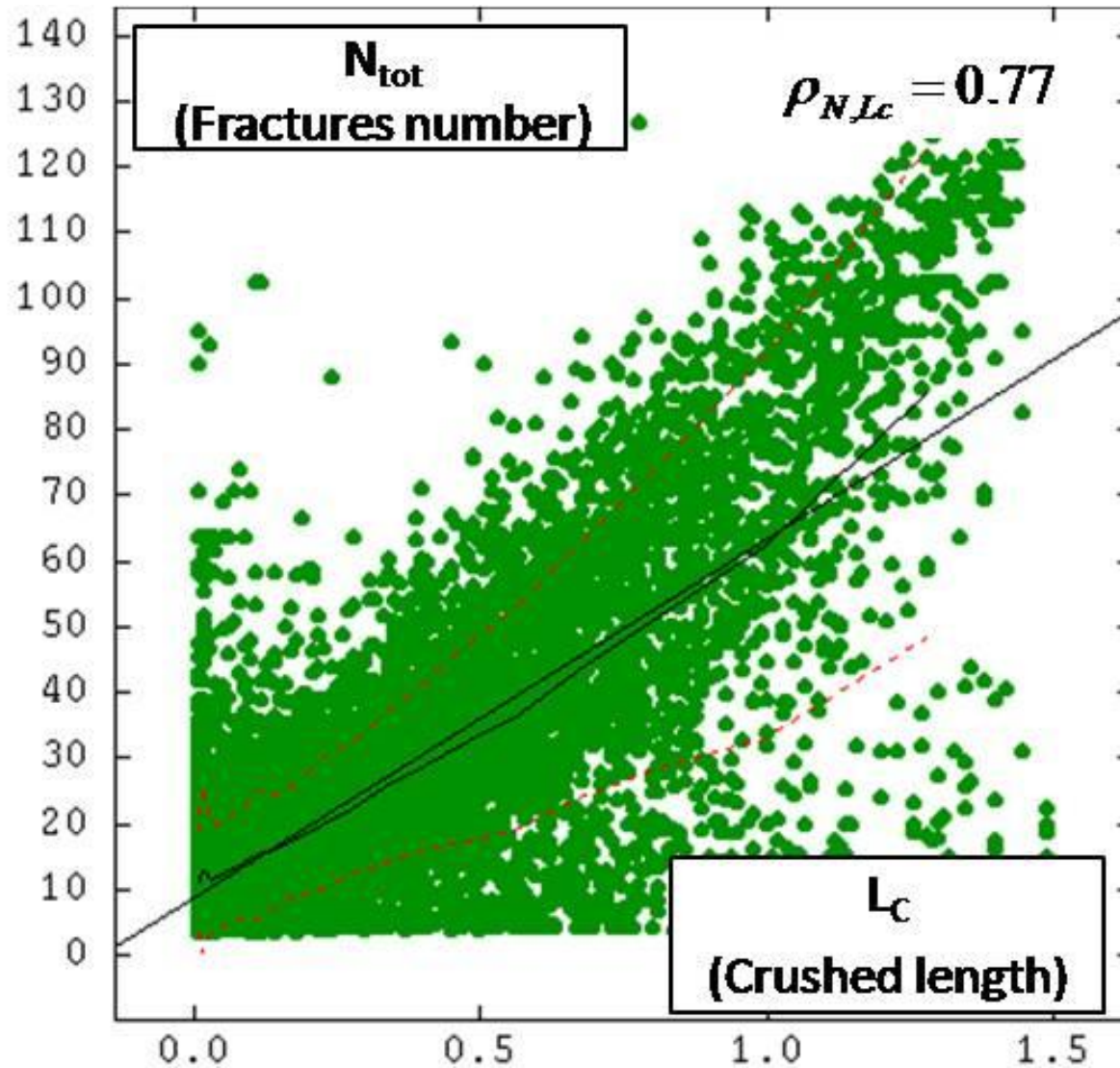
(c)



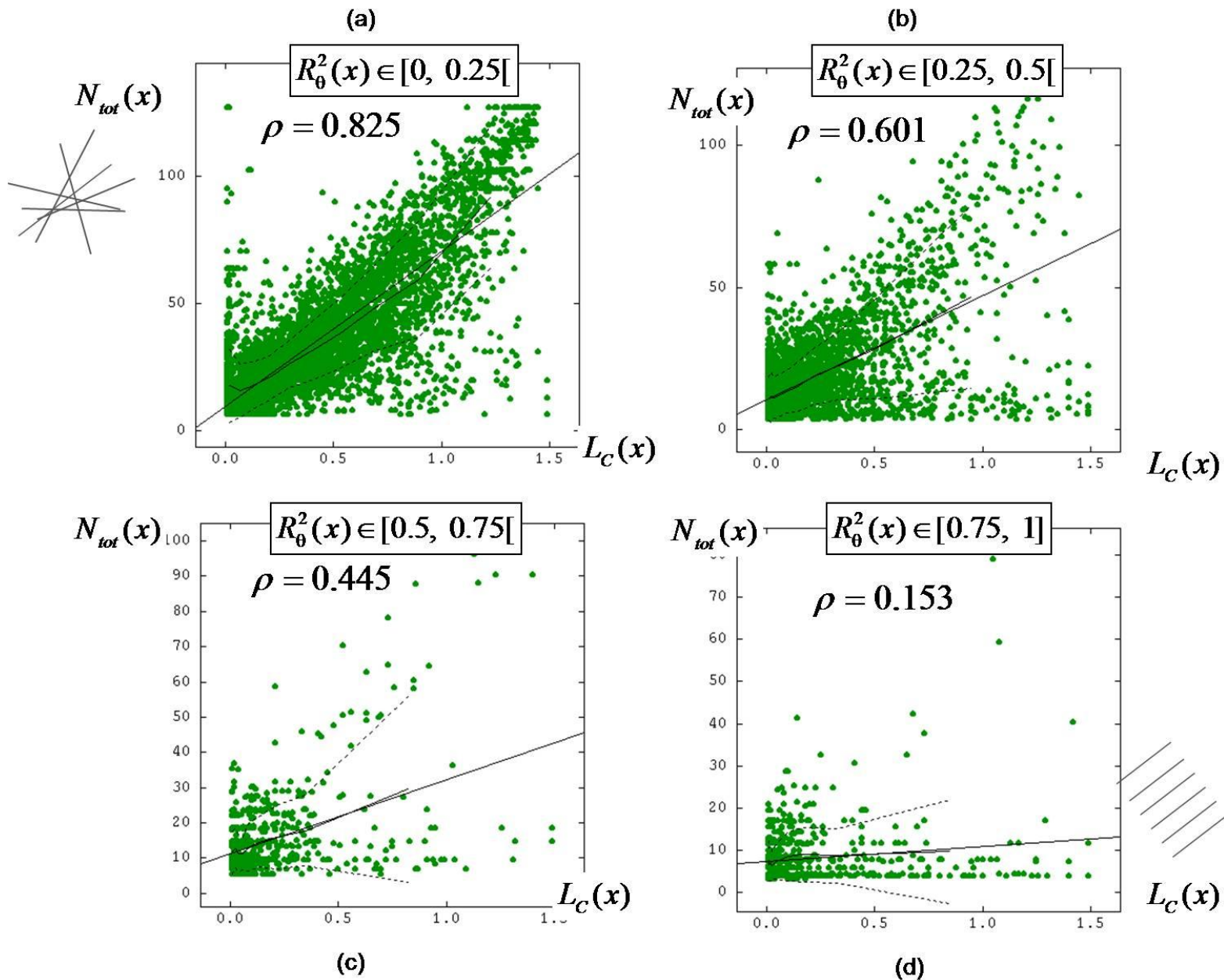
(d)



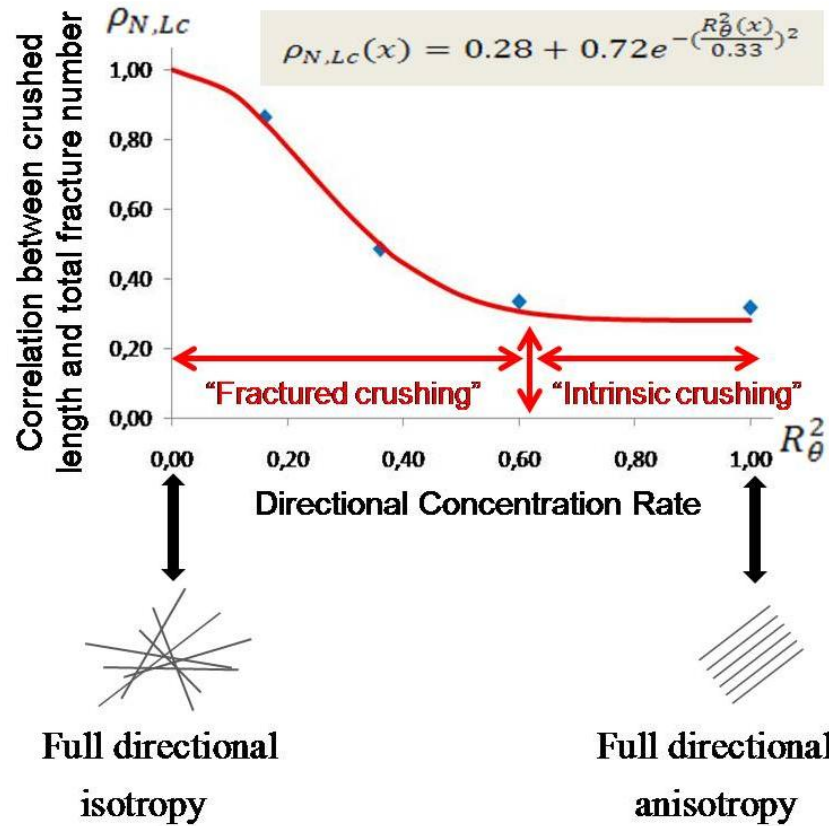
Another deposit



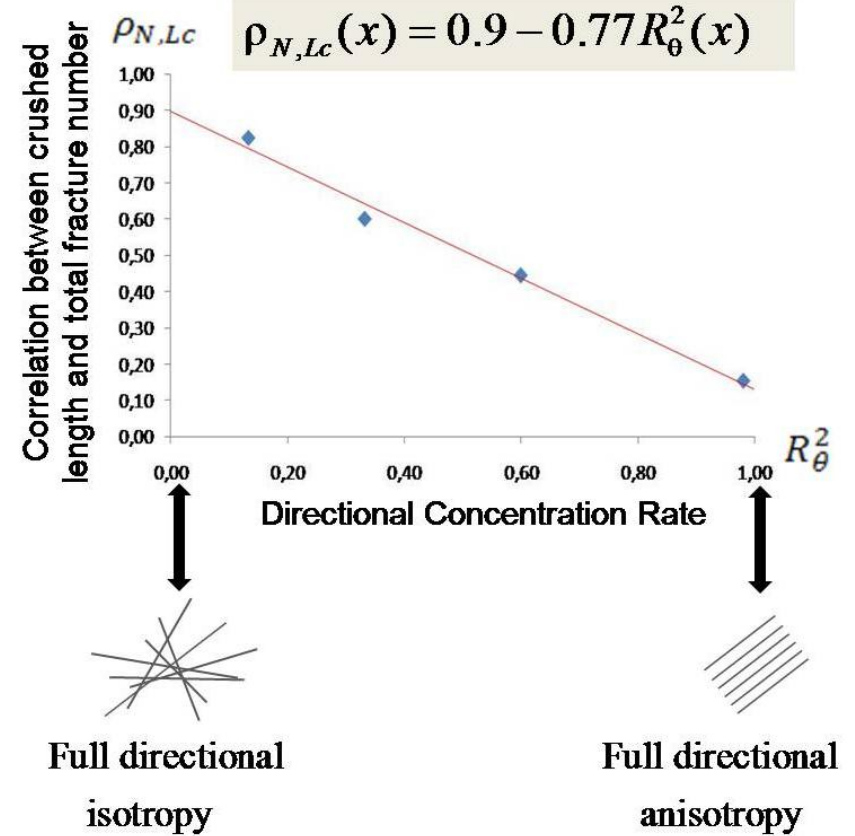
Another deposit



Deposit 1



Deposit 2



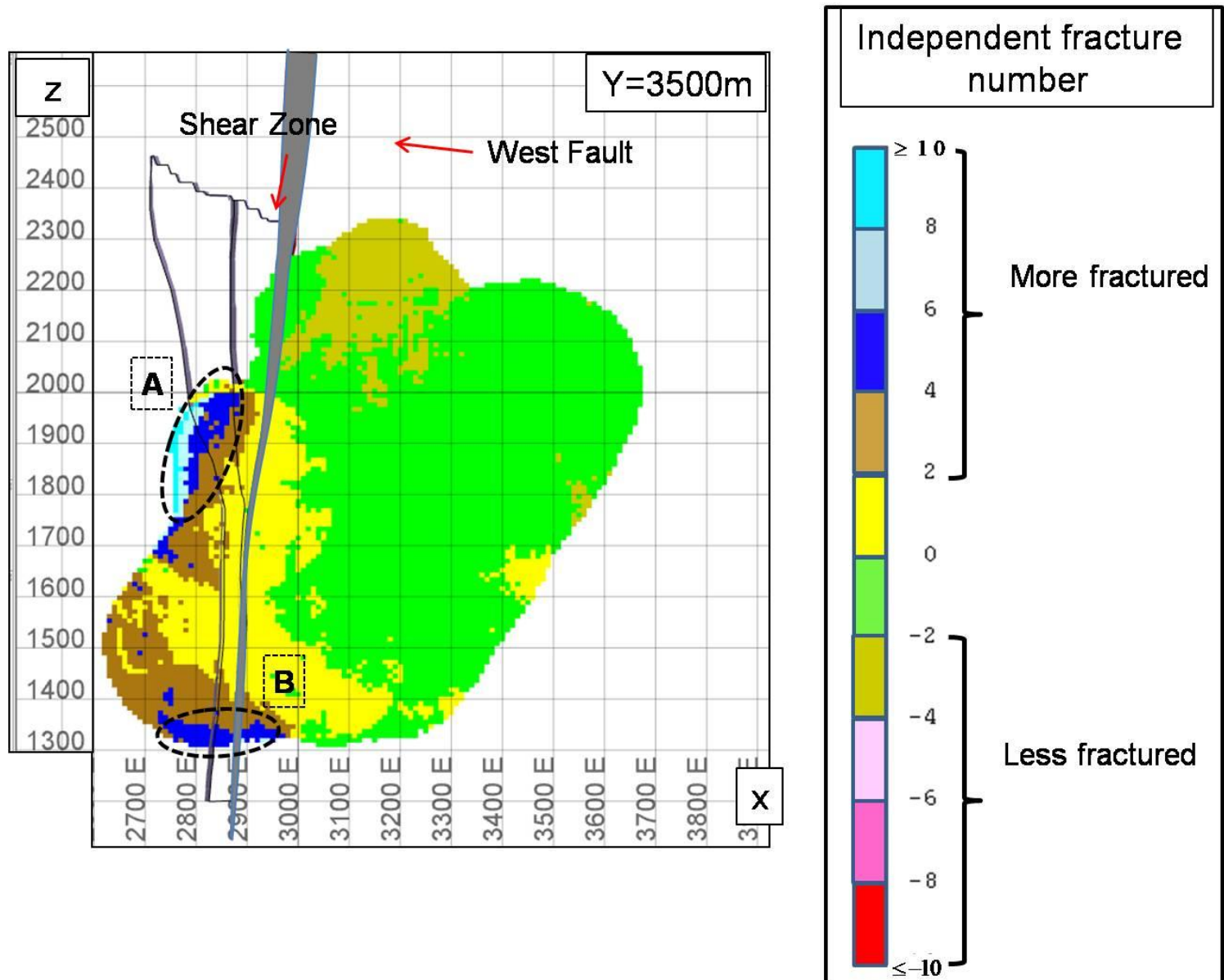
Residual model

$$N_{tot}(x) = \frac{\sigma_{Ntot}}{\sigma_{Lc}}(\rho_{N,Lc}(x)) \left(L_C(x) + \sqrt{1 - \rho_{N,Lc}(x)^2} RSD(x) \right) + C(\rho_{N,Lc}(x))$$

$$\forall x, N_{tot}(x) = N_{corr}(x) + N_{ind}(x)$$

Independent fractures

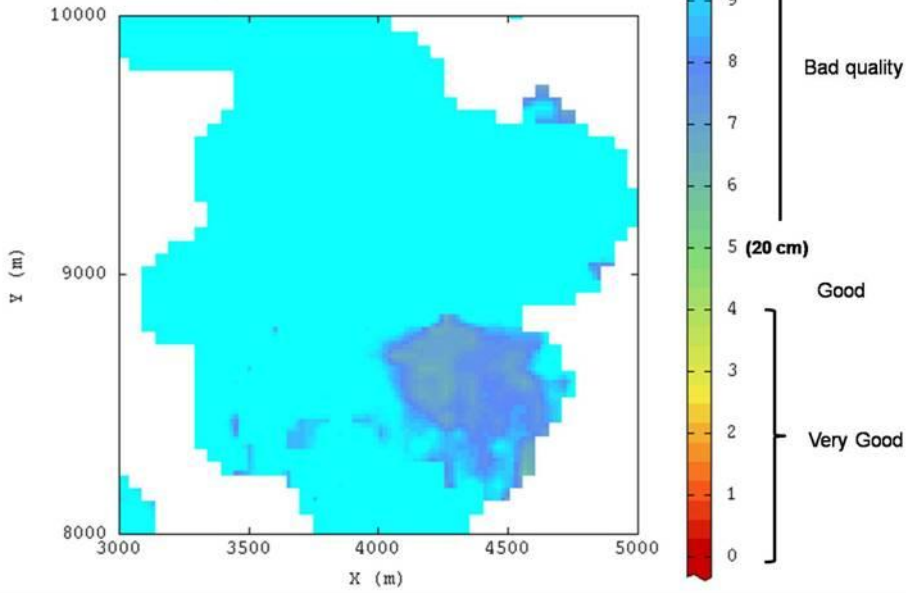
Deposit 1



Independent fractures Deposit 2

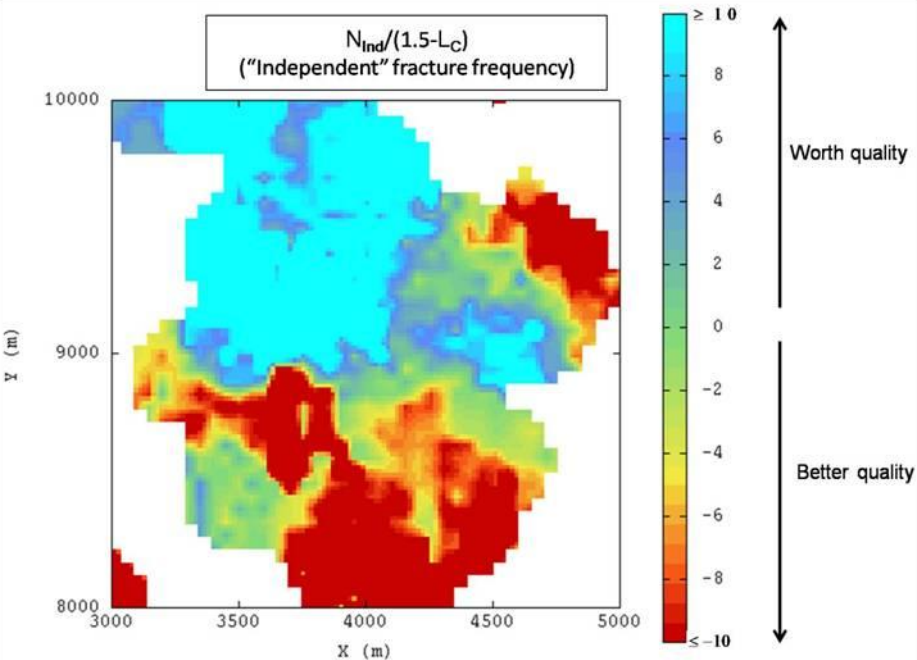
$$FF_{true} = N_{tot} / (1.5 - L_C)$$

(Fracture frequency)



$$N_{ind} / (1.5 - L_C)$$

("Independent" fracture frequency)



Conclusion

- Crushing, a useful regionalized variable
- Directional concentration, mutual organization of the fractures
- Spatial correlation between fracturing and crushing
- Useful in case of rock submitted to alteration

Fracturing, Crushing and Directional Concentration

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